From Nature to Plasma Physics

Waleed Moslem

Outline

- Soliton
- Cnoidal
- Tsunami
- Envelope soliotn
- Rogue wave
- Mach Cones
- Wakefield
- Water droplet
- St. Elmo's fire
- AGN
- Sun & Stars
- Lightning
- Kelvin–Helmholtz
- Rayleigh–Taylor

Outline

- **Soliton**
- **Cnoidal**
- **Tsunami**
- **Envelope soliotn**
- **Rogue wave**
- **Mach Cones**
- **Wakefield**

Part (I)

Why Nature?

- Nature → (Matter & Motion & Energy & Force….) → Physics → How the Universe Behaves

- Why? Development of new products → Improvement/development our modern-day society

Soliton

- In 1834, while conducting experiments to determine the most efficient design for canal boats, he discovered a phenomenon that he described as the **wave of translation**
- Stable – Large distances – Speed(size) – Width(depth) – Never merge – Splits into two waves

John Scott Russell
(1808-1882)

Soliton, cont.

REPORT

OF THE

FOURTEENTH MEETING

OF THE

BRITISH ASSOCIATION

FOR THE

ADVANCEMENT OF SCIENCE;

HELD AT YORK IN SEPTEMBER 1844.

LONDON:

JOHN MURRAY, ALBEMARLE STREET.

1845.

Report on Waves. By J. SCOTT RUSSELL, *Esq., M.A., F.R.S. Edin., made to the Meetings in* 1842 *and* 1843.

Members of Committee { Sir JOHN ROBISON*, *Sec. R.S. Edin.* J. SCOTT RUSSELL, *F.R.S. Edin.*

A PROVISIONAL Report on this subject was presented to the Meeting held at Liverpool in 1838, and is printed in the Sixth Volume of the Transactions. That report was a partial one. It states that "the extent and multifarious nature of the subjects of inquiry have rendered it impossible to terminate the examination of all of them in so short a time; but it is their duty to report the progress which they have made, and the partial results they have already obtained, leaving to the reports of future years such portions of the inquiries as they have not yet undertaken."

The first of these subjects of inquiry is stated to have been "to determine the varieties, phænomena and laws of waves, and the conditions which affect their genesis and propagation."

It is this branch of the duty of the Committee which forms the subject of the present report. Ever since the date of that report, it has happened that the author of this has been so fully pre-occupied by inevitable duty, that it was not in his power to indulge much in the pleasures of scientific inquiry; and as the active part of the investigation necessarily devolved upon him, it was not practicable to continue the series of researches on the ample and systematic scale originally designed, so soon as he had anticipated, so that the former report has necessarily been left in a fragmentary state till now.

But I have never ceased to avail myself of such opportunities as I could contrive to apply to the furtherance of this interesting investigation. I have now fully discussed the experiments which the former report only registered. I have repeated the former experiments where their value seemed doubtful, I have supplemented them in those places where examples were wanting. I have extended them to higher ranges, and where necessary to a much larger scale. In so far as the experiments have been repeated and more fully discussed, they have tended to confirm the conclusions given in the former report, as well as to extend their application.

The results here alluded to are those which concern especially the velocity and characteristic properties of the solitary wave, that class of wave which the writer has called the great wave of translation, and which he regards as the primary wave of the first order. The former experiments related chiefly to the mode of genesis, and velocity of propagation of this wave. They led to this expression for the velocity in all circumstances,

$$v = \sqrt{g(h+k)},$$

k being the height of the crest of the wave above the plane of repose of the fluid, h the depth throughout the fluid in repose, and g the measure of gravity. Later discussions of the experiments not only confirm this result, but are themselves established by such further experiments as have been recently instituted, so that this formerly obtained velocity may now be regarded as the phænomenon characteristic of the wave of the first order.

The former series of experiments also contained several points of research not published in the former report, because not sufficiently extended to be of

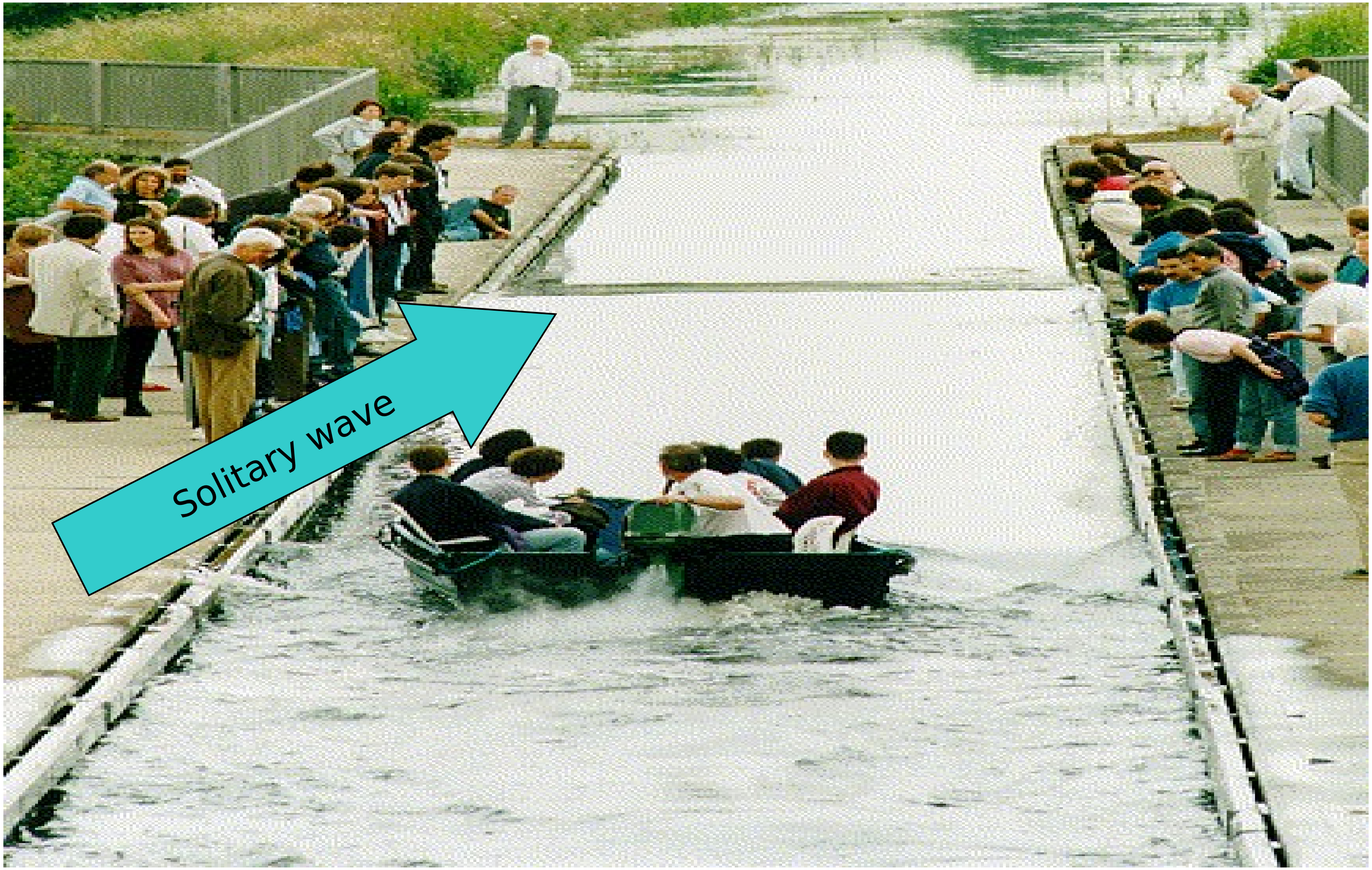
* I cannot allow these pages to leave my hands without expressing my deep regret that the death of Sir John Robison has suddenly deprived the Association of a zealous and distinguished office-bearer, and myself of a kind friend. In all these researches the responsible duties were mine, and I alone am accountable for them; but in forwarding the objects of the investigation I always found him a valuable counsellor and a respected and cordial cooperator.

Soliton, cont.

J. S. Russell Aqueduct

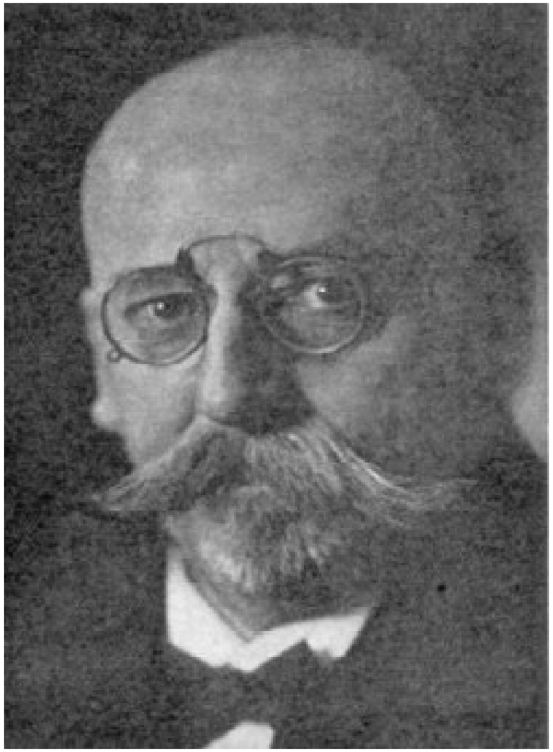
- 89.3 m long
- 4.13 m wide
- 1.52 m deep

Soliton, cont.



Soliton, cont.

Diederik Johannes Korteweg
(1848 – 1941)



Gustav de Vries
(1866 – 1934)

Soliton, cont.

$$\frac{\partial u}{\partial t} + \alpha u \frac{\partial u}{\partial x} + \beta \frac{\partial^3 u}{\partial x^3} = 0$$

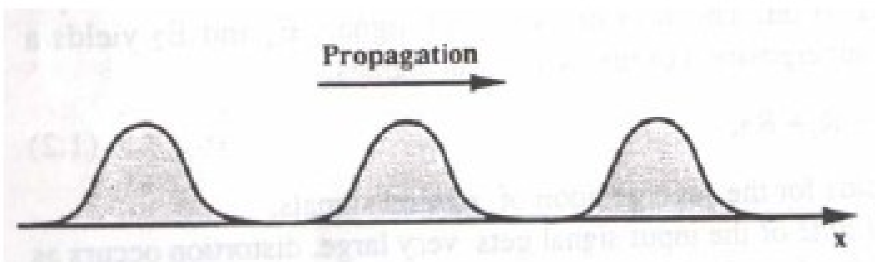
Nonlinearity

Dispersion

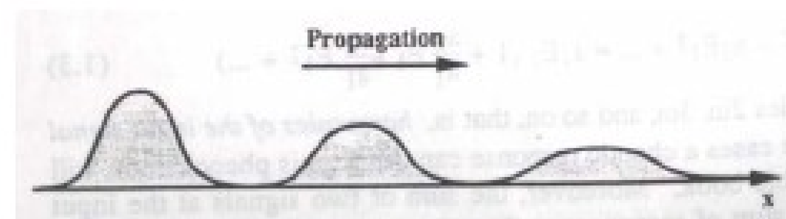
Korteweg-de Vries Equation
(1895)

Soliton, cont.

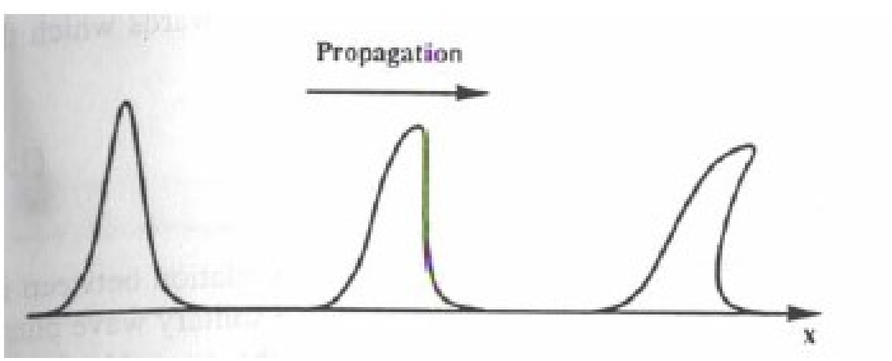
Linear & Nondispersive



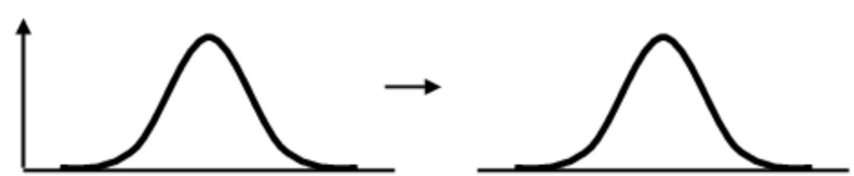
Linear & Dispersive



Nonlinear & Nondispersive



Nonlinear & Dispersive



Soliton, cont.

- Zabusky & Kruskal (1965) $\rightarrow$ numerically $\rightarrow$ solutions seemed to decompose at large times into a collection of "solitons"
- Soliton in: shallow-water waves, plasma, crystal lattice, biology, optical fiber
- Movie1 and Movie2

Soliton, cont.

VOLUME 17, NUMBER 19 PHYSICAL REVIEW LETTERS 7 NOVEMBER 1966

PROPAGATION OF ION-ACOUSTIC SOLITARY WAVES OF SMALL AMPLITUDE

Haruichi Washimi and Tosiya Taniuti
Institute of Plasma Physics, Nagoya University, Nagoya, Japan
(Received 5 August 1966)

VOLUME 25, NUMBER 1 PHYSICAL REVIEW LETTERS 6 JULY 1970

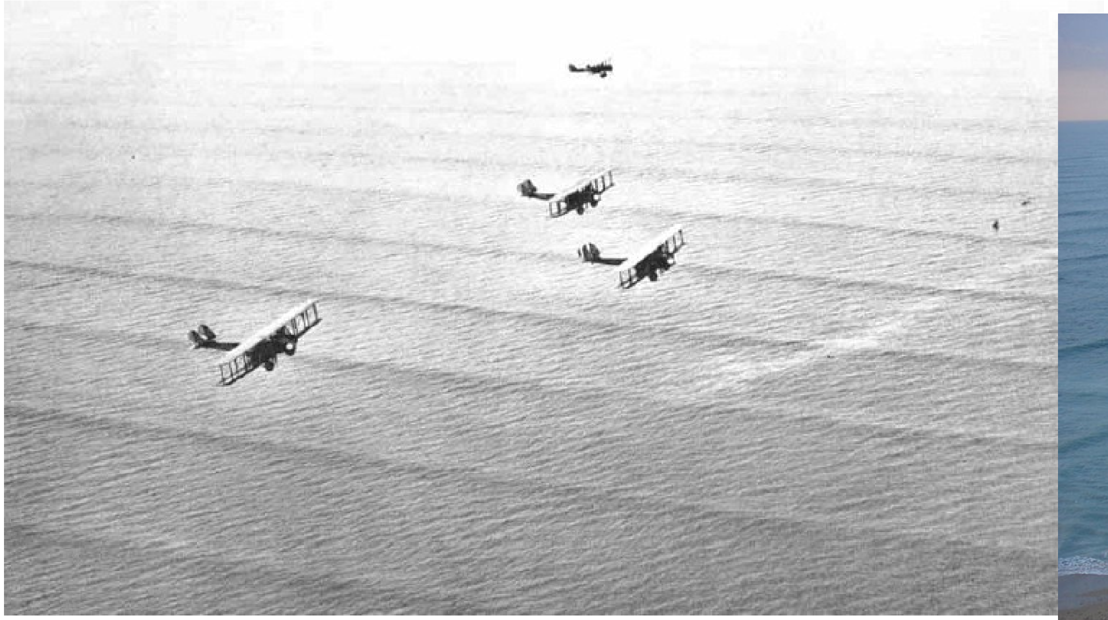
FORMATION AND INTERACTION OF ION-ACOUSTIC SOLITONS*

H. Ikezi,† R. J. Taylor,‡ and D. R. Baker
Department of Physics, University of California, Los Angeles, California 90024
(Received 11 May 1970)

Cnoidal

- Korteweg and de Vries → 1895 → KdV Eq.
- Jacobi elliptic function *cn*, which is why they are coined *cnoidal* waves
- In the limit of infinite wavelength → the cnoidal wave becomes a solitary wave.
- Surface water waves & Ion-acoustic waves in plasma physics & Optical fiber & Graphene-based superlattice & Solids & Traffic flow…….etc

Cnoidal, cont.



Cnoidal, cont.

PROCEEDINGS OF THE ROYAL SOCIETY A | MATHEMATICAL, PHYSICAL & ENGINEERING SCIENCES

On cnoidal waves and bores

By T. B. Benjamin

Department of Engineering, University of Cambridge

and M. J. Lighthill, F.R.S.

Department of Mathematics, University of Manchester

(*Received* 13 *February* 1954)

Journal of the Physical Society of Japan, Vol. 46, No. 6, June, 1979

Propagation of Ion Acoustic Cnoidal Wave

Kimiaki Konno, Teruo Mitsuhashi†
and Yoshi H. Ichikawa††

Department of Physics, College of Science and Technology, Nihon University, Tokyo

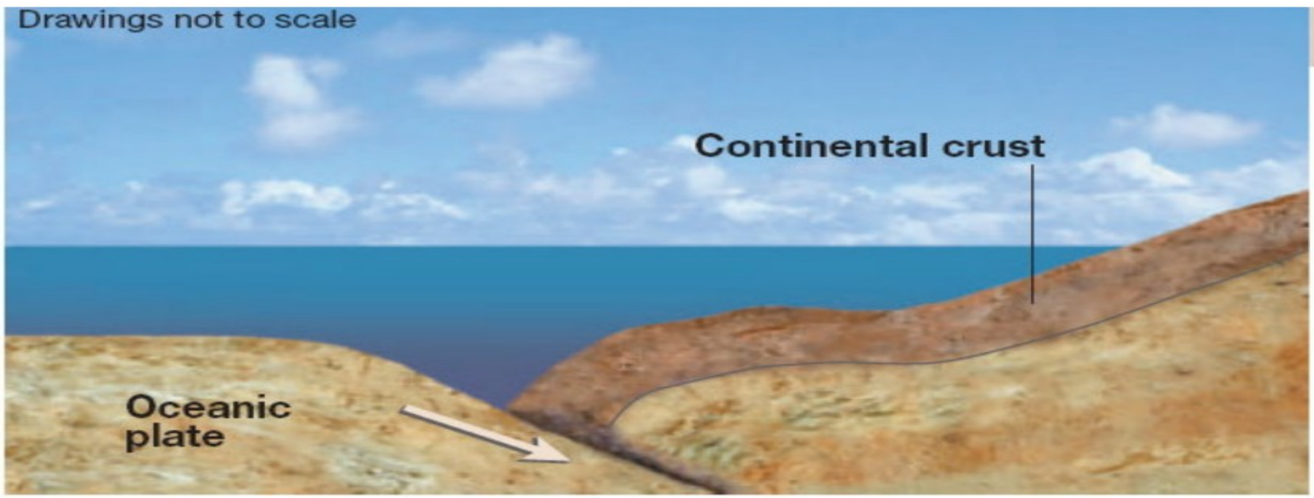
†*Shiroyama Senior High School, Shiroyama, Kanagawa*

††*Institute of Plasma Physics, Nagoya University, Nagoya*

(Received February 5, 1979)

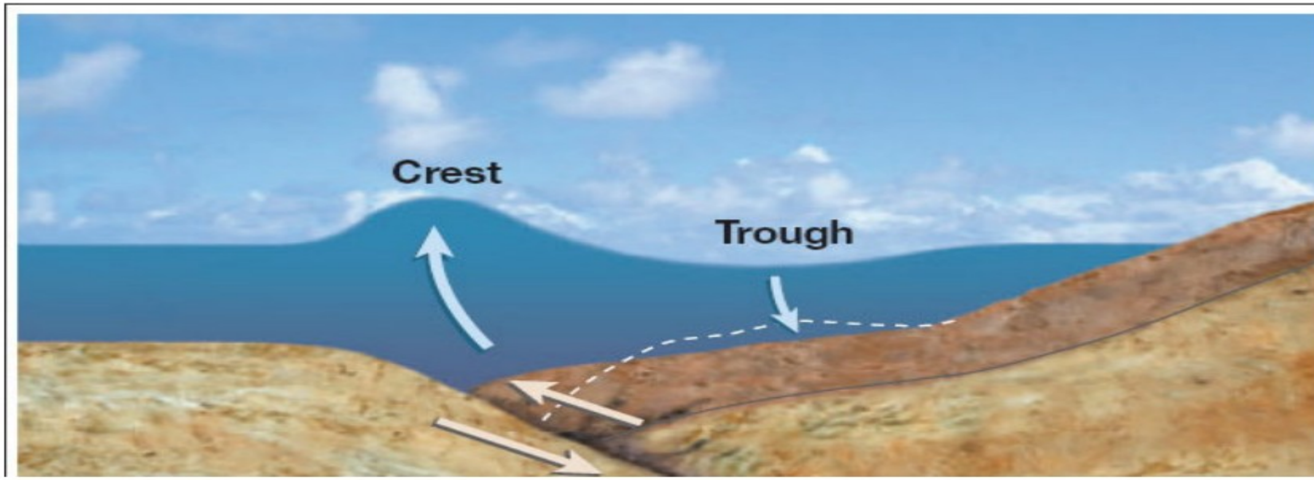
Tsunami

- What do you do if you're at the beach and the sea is receding farther than usual?



1 Before the earthquake

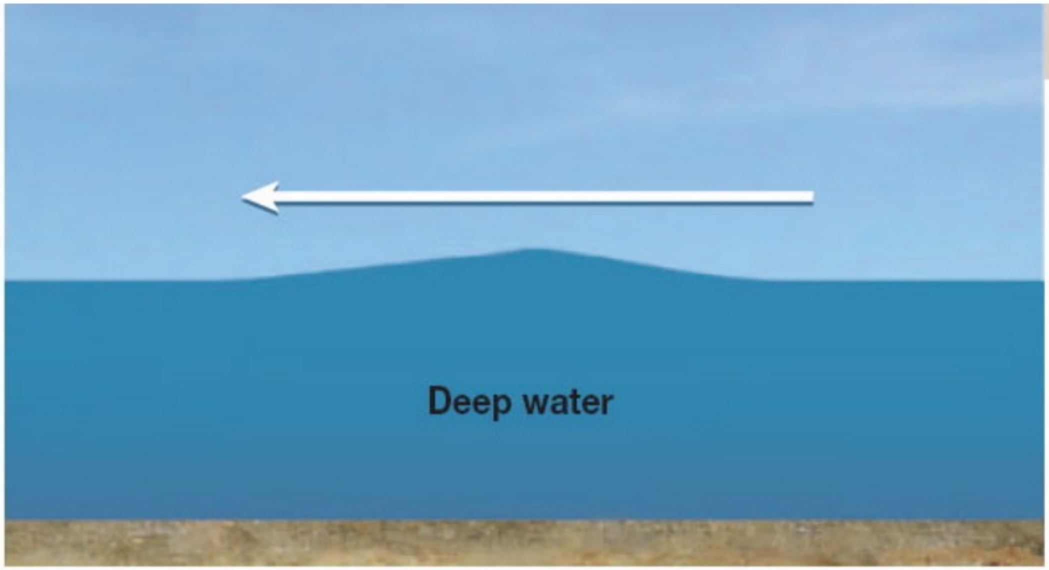
The plate holding the Indian Ocean was sliding under the continental plate (holding Indonesia and much of Asia) at about 6 cm per year. The continental crust was bent thanks to the constant pressure of collision.



2 During the quake

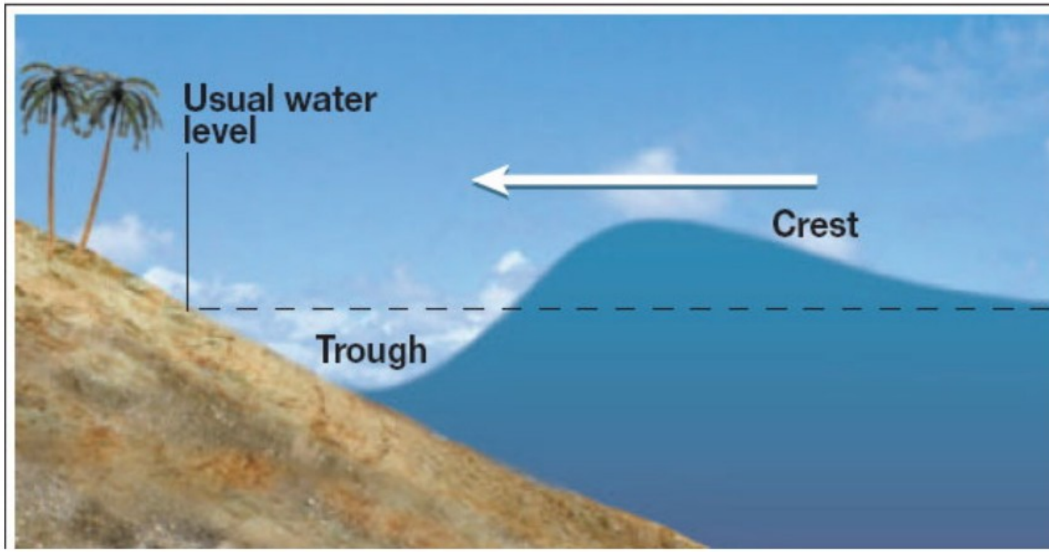
The fault ruptured violently, allowing the continental crust to unbend and causing portions of the sea floor to move up or down by several metres. The water above the fault responded in kind, creating a wave crest and trough.

Tsunami, cont.



3 The wave travels

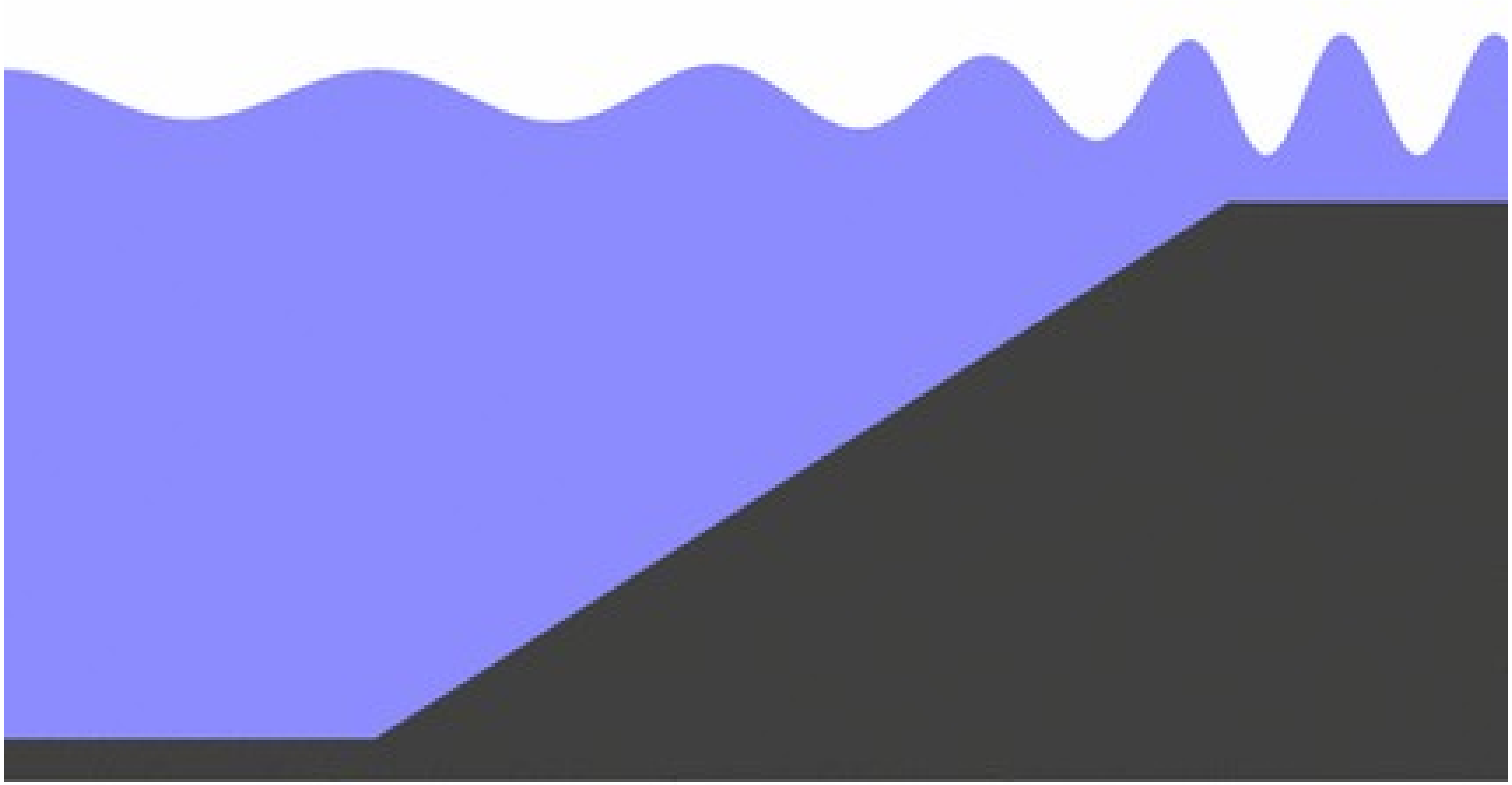
One wave crashed towards the nearby shore of Indonesia. Another barrelled westwards at about 800 km per hour in deep water, with a wavelength of 100 km and an average wave height of just tens of centimetres.



4 Collision

When the wave entered shallow waters, it slowed to tens of kilometres per hour, its wavelength shortened to about 5 km, and its height is thought to have soared to more than ten metres. The trough of the wave often hits before the crest (as shown).

Tsunami, cont.



Movie

Tsunami, cont.

- **Mathematics** predicting to reduce their dangers
- **Modeling** ocean tsunami wave creation and propagation
- Clarifying tsunami wave **characteristics**
- **Engineers** design early warning systems

Tsunami, cont.

A Letters Journal Exploring the Frontiers of Physics

November 2009

EPL, 88 (2009) 45001
doi: 10.1209/0295-5075/88/45001

www.epljournal.org

Steepening of solitons (tsunami effect) in complex plasmas

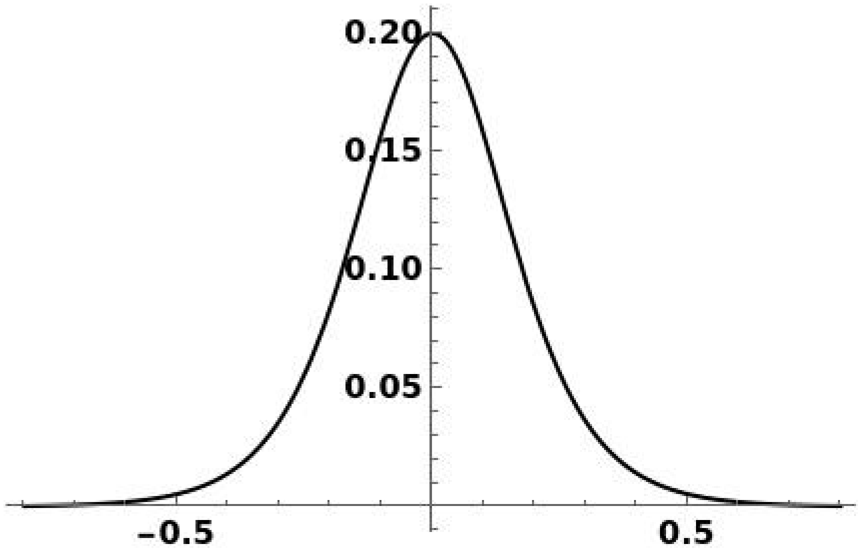
C. Durniak[1(a)], D. Samsonov[1], S. Zhdanov[2] and G. Morfill[2]

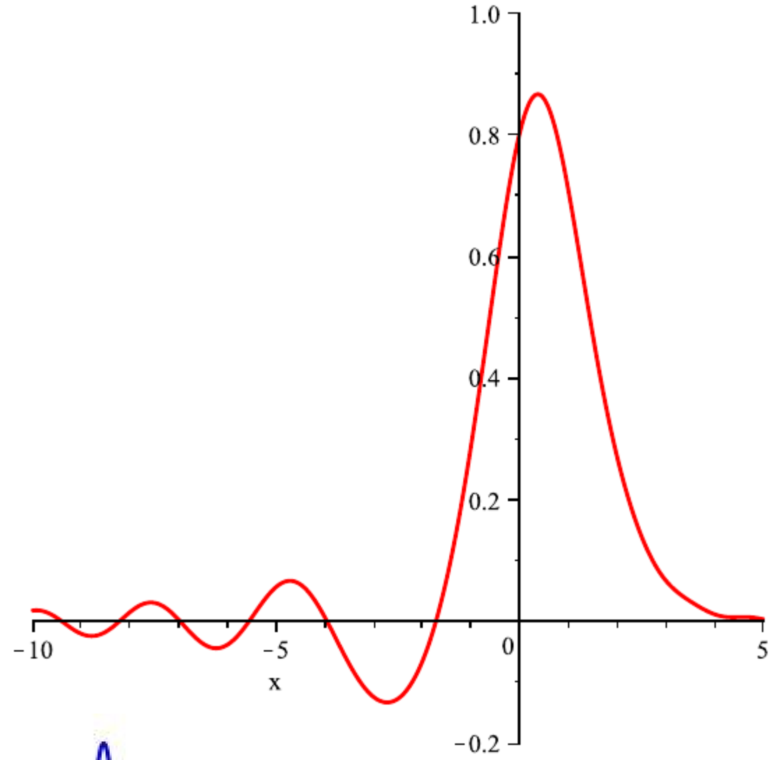
IEEE TRANSACTIONS ON PLASMA SCIENCE, VOL. 39, NO. 11, NOVEMBER 2011

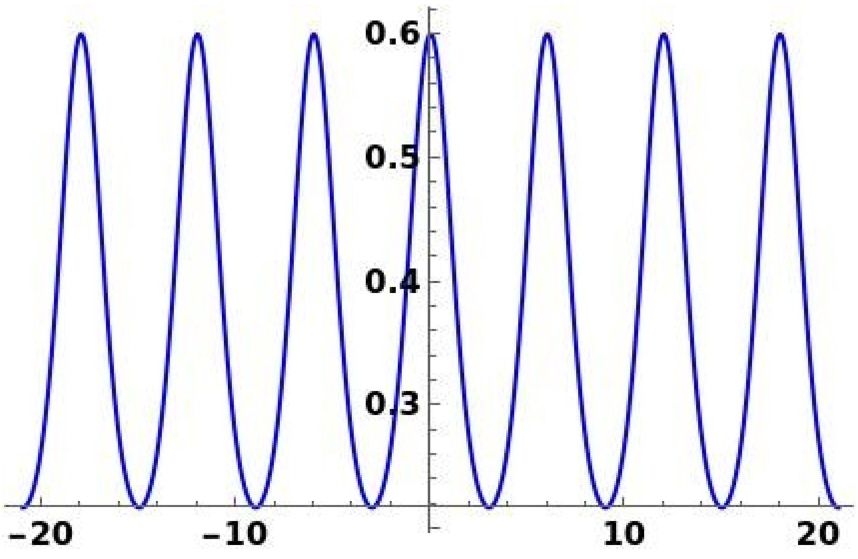
Tsunami in a Complex (Dusty) Plasma

D. Samsonov, C. Durniak, S. Zhdanov, and G. Morfill

Soliton & Cnoidal & Tsunami



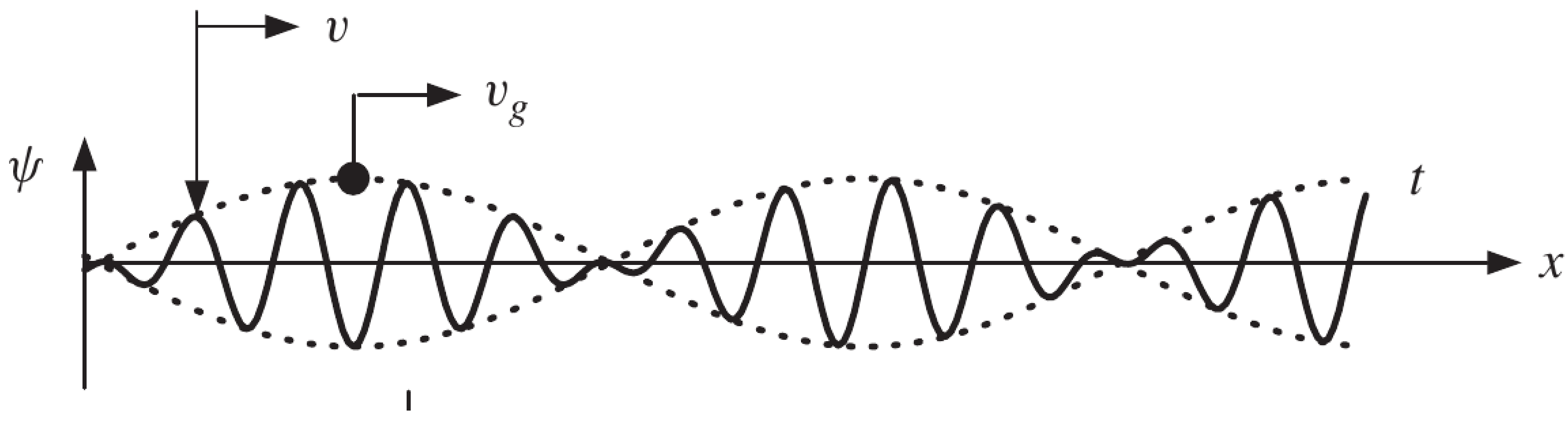




Envelope Soliotn

$$\psi_1 = A\cos(k_1 x - \omega_1 t), \qquad \psi_2 = A\cos(k_2 x - \omega_2 t)$$

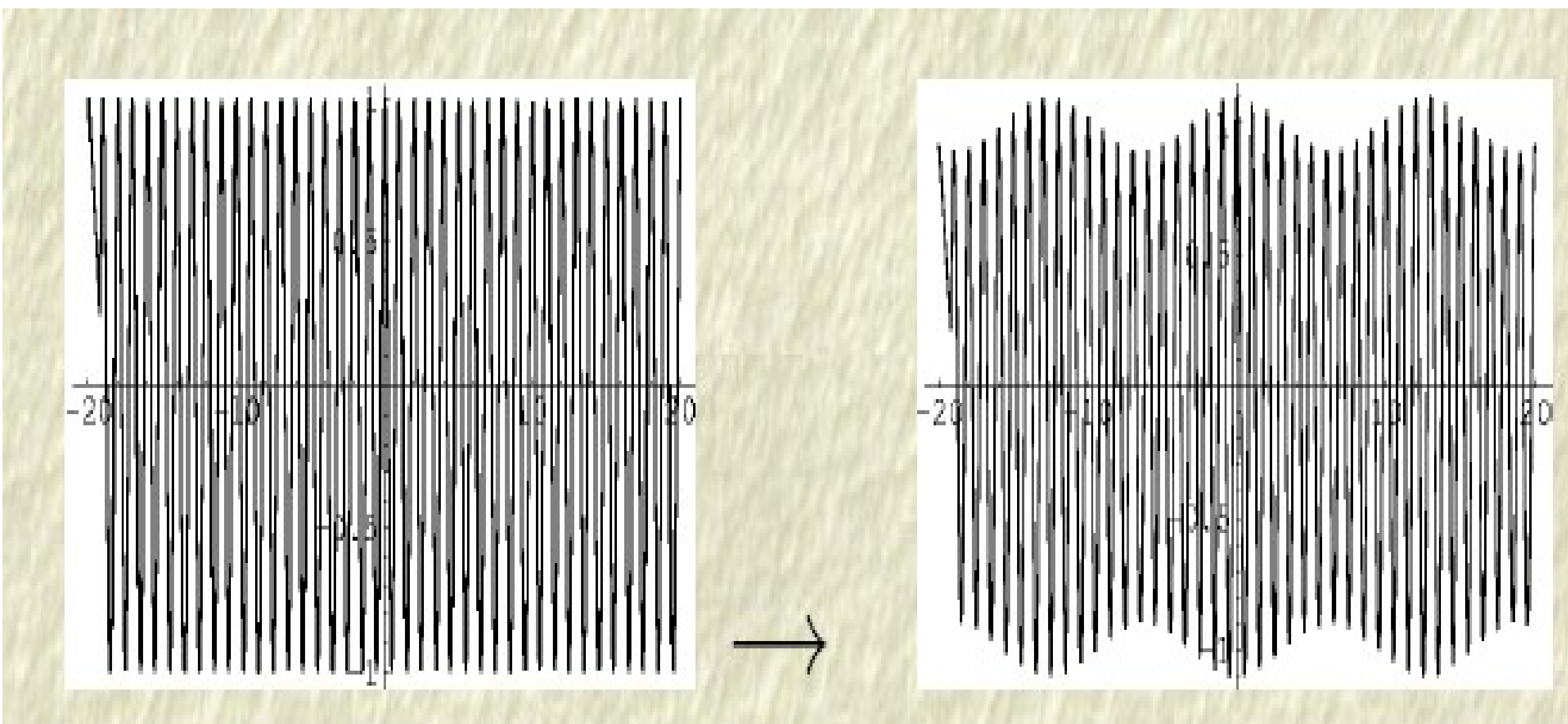
$$\psi = A(x, t)\cos(k_o x - \omega_o t)$$



Movie

Envelope Soliotn, cont.

- The amplitude of the harmonic wave may vary in space and time
- **Time scales. How many time scales?**

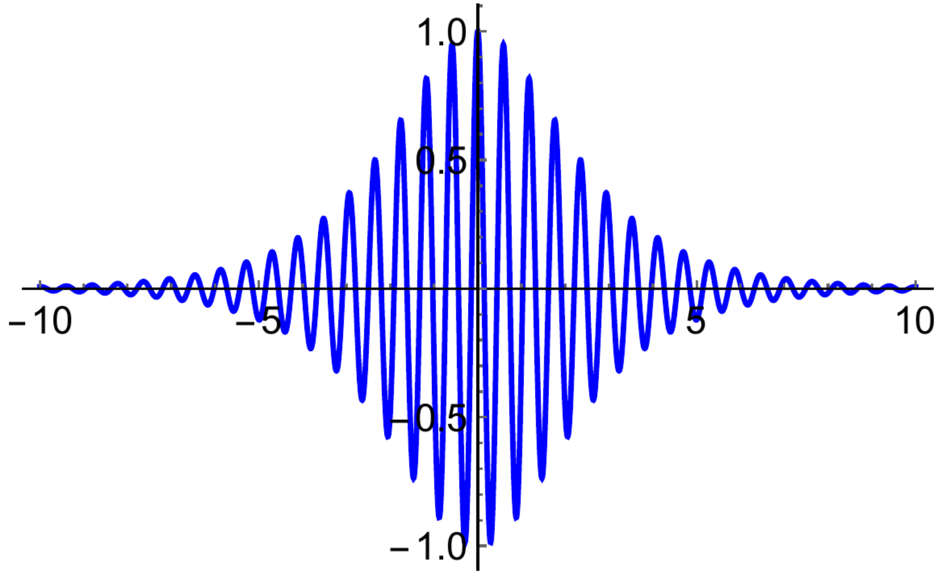


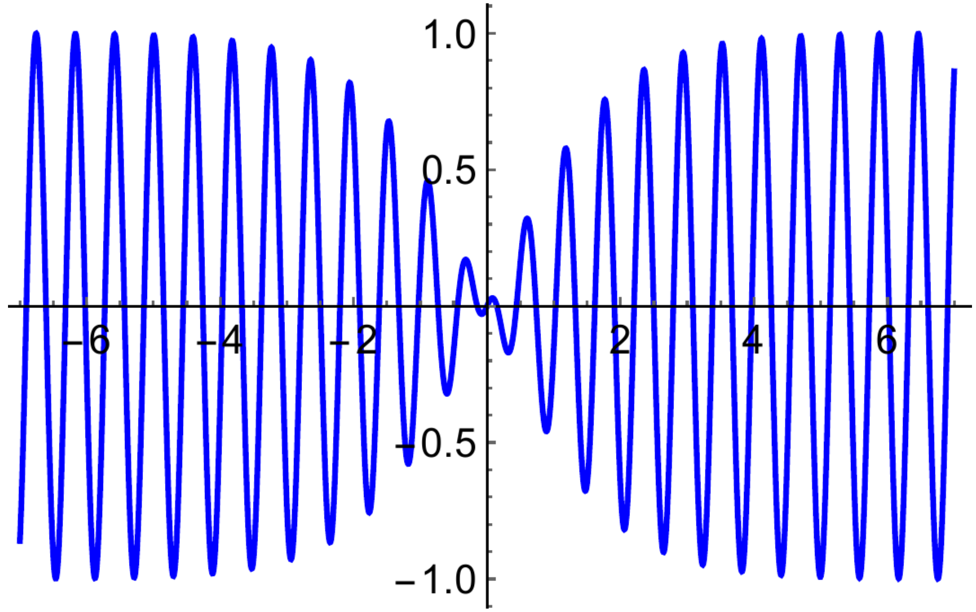
Envelope Soliotn, cont.

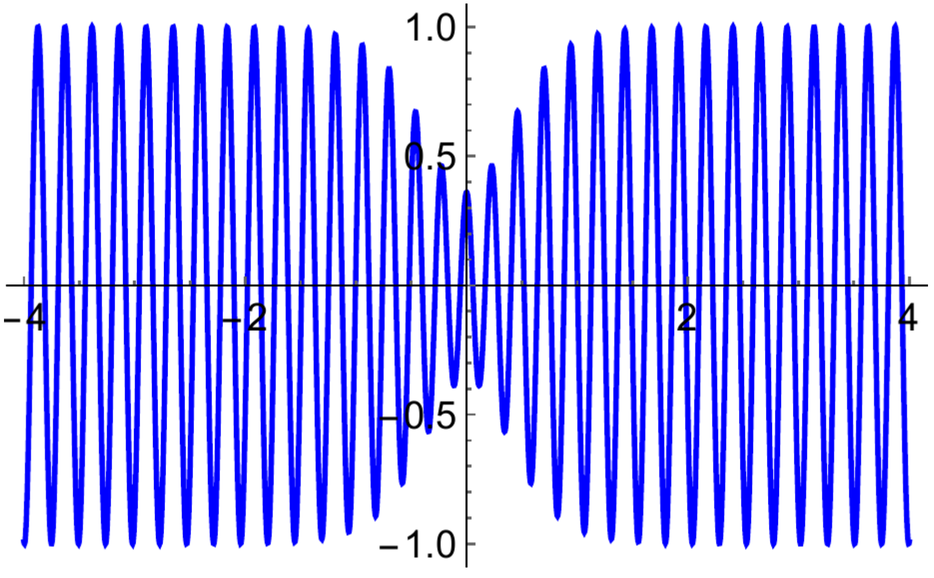
- This modulation due to nonlinearity may be strong enogh to lead to the formation of envelope soliton
- Three forms of envelope: bright, dark, and Gray
- Evloution equation → Nonlinear Schrödinger Eq.

$$i\frac{\partial\psi}{\partial\tau}+P\frac{\partial^2\psi}{\partial\zeta^2}+Q\left|\psi\right|^2\psi=0$$

Envelope Soliotn, cont.







Envelope Soliotn, cont.

JOURNAL OF THE PHYSICAL SOCIETY OF JAPAN, Vol. 27, No. 5, NOVEMBER, 1969

A Nonlinear Theory of Two-Stream Instability

Tsuguhiro WATANABE

PERTURBATION
METHODS

ALI HASAN NAYFEH

Professor of Engineering Science and Mechanics
Virginia Polytechnic Institute and State University
Blacksburg, Virginia 24061

Envelope Soliotn, cont.

J. Plasma Physics (1975), *vol.* 14, *part* 2, *pp.* 353–364

Ion-acoustic solitons excited by a single grid

By S. WATANABE

J. Plasma Physics (1976), *vol.* 15, *part* 1, *pp.* 67–81

Effect of wave–particle interaction on recurrence of a nonlinear ion wave

By S. WATANABE

Envelope Soliotn, cont.

- 1973: Akira Hasegawa of AT&T Bell Labs was the first to suggest that envelope solitons could exist in optical fibers
- 1973: Robin Bullough made the first mathematical report of the existence of optical solitons → suggest its application in optical telecommunications
- 1987: Emplit et al. made the first experimental observation of the propagation of a dark soliton, in an optical fiber
- 1970's: Starting the Nonlinear Plasma Physics Era

Rogue wave

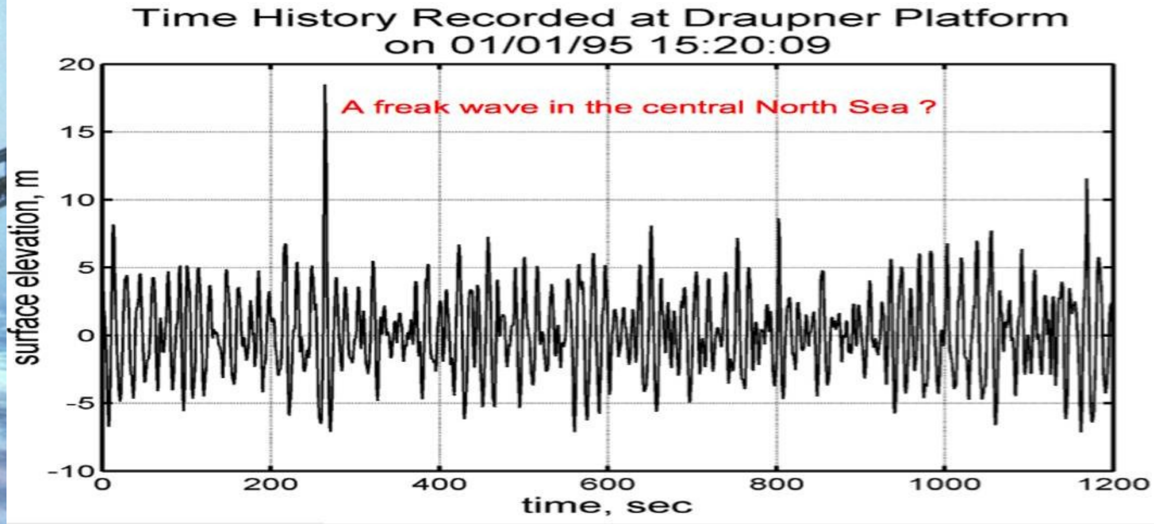
Freak waves

Rogue waves

Giant waves

Extreme waves

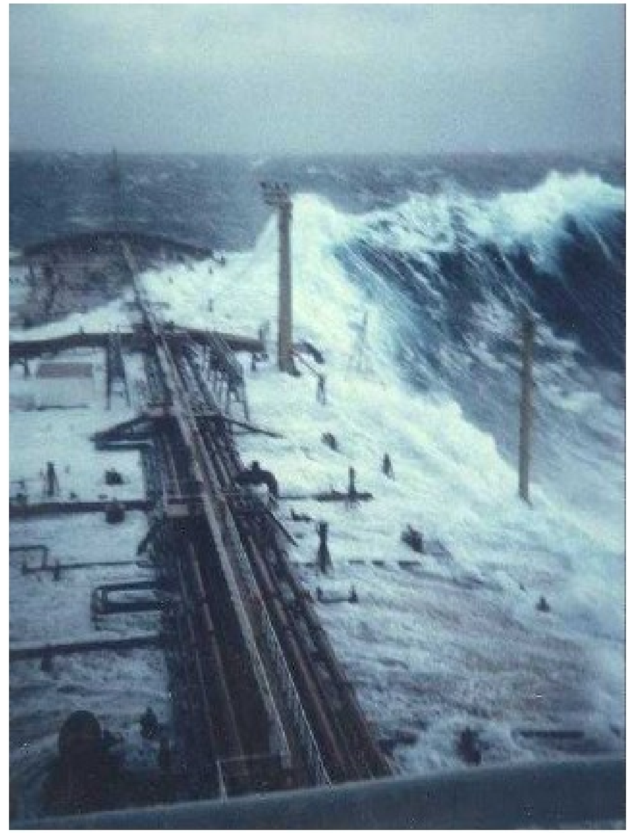
Rogue waves



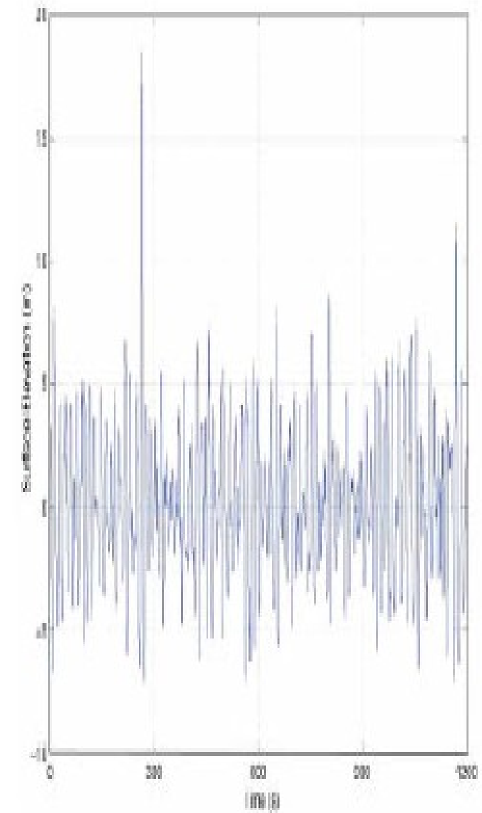
- H_{max}=25.6 m & 1 in 200,000 waves
- Extreme waves → appear from nowhere → high-energy → high amplitude (3 times the average amplitude) → carry dramatic impact
- How this wave exist? → Use & Avoid
- Movie

Rogue waves

(a) Norwegian tanker Wilstar, Agulhas current (1974)



(b) Oil freighter Esso Languedoc, coast of Durban (1980)



(c) Draupner Platform, the North Sea (New Year's Day 1995)

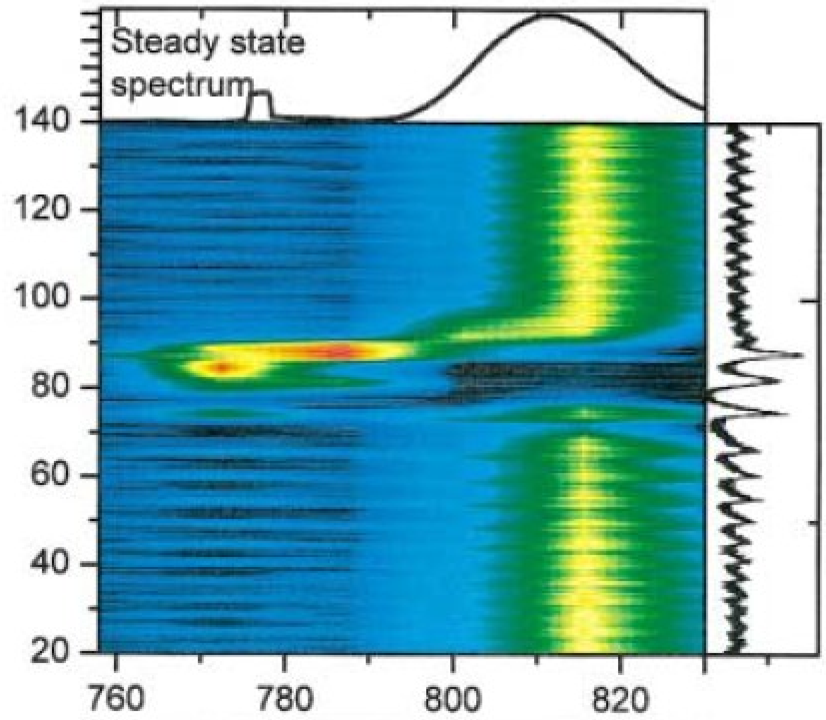
Rogue waves, cont.

VOLUME 88, NUMBER 7 PHYSICAL REVIEW LETTERS 18 FEBRUARY 2002

Experimental Evidence for Soliton Explosions

Steven T. Cundiff,[1,*] J. M. Soto-Crespo,[2] and Nail Akhmediev[3]

We show, experimentally and numerically, that Ti:sapphire mode-locked lasers can operate in a regime in which they intermittently produce exploding solitons. This happens when the laser operates near a critical point. Explosions happen spontaneously, but external perturbations can trigger them. In stable operation, all explosions ha … eristics of the explosions depend on the intracavity …



Rogue waves, cont.

Eur. Phys. J. Special Topics **185**, 169–180 (2010)

DOI: 10.1140/epjst/e2010-01247-6

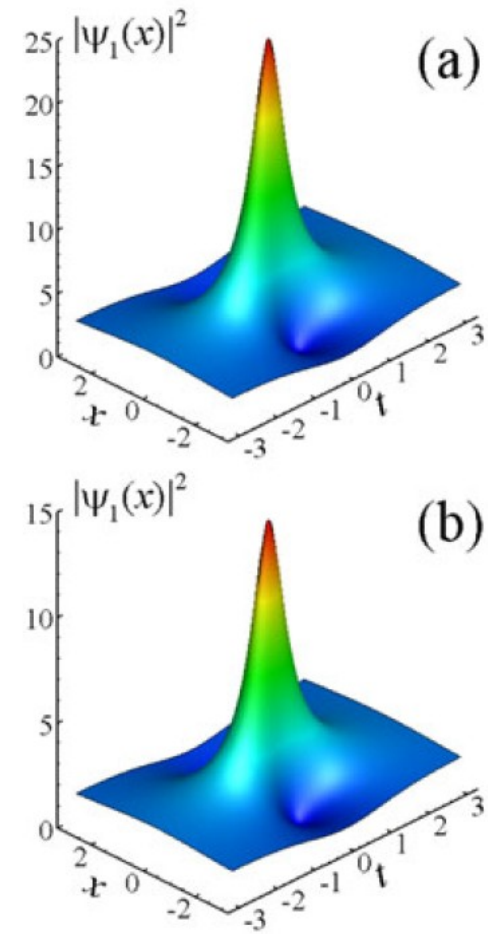
THE EUROPEAN PHYSICAL JOURNAL SPECIAL TOPICS

Regular Article

Vector rogue waves in binary mixtures of Bose-Einstein condensates

Yu.V. Bludov[1,a], V.V. Konotop[2,b], and N. Akhmediev[3,c]

Abstract. We study numerically rogue waves in the two-component Bose-Einstein condensates which are described by the coupled set of two Gross-Pitaevskii equations with variable scattering lengths. We show that rogue wave solutions exist only for certain combinations of the nonlinear coefficients describing two-body interactions. We present the solutions for the combinations of these coefficients that admit the existence of rogue waves.



Rogue waves, cont.

Commun. Theor. Phys. (Beijing, China) **54** (2010) pp. 947–949

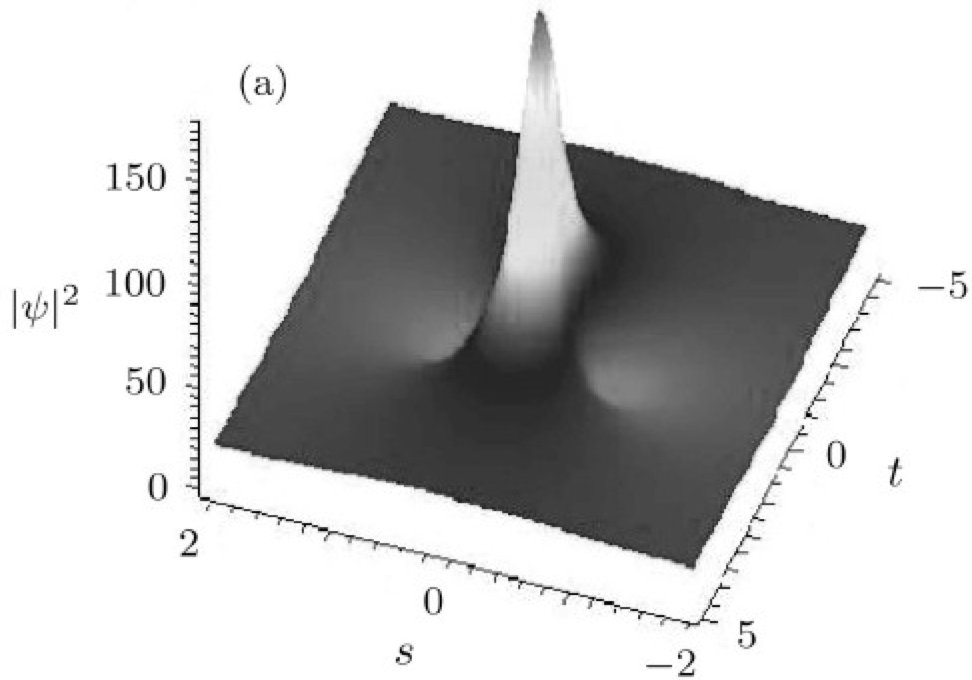
Vol. 54, No. 5, November 15, 2010

Financial Rogue Waves*

YAN Zhen-Ya (闫振亚)†

Key Laboratory of Mathematics Mechanization, Institute of Sy
Beijing 100190, China

(Received June 4, 2010)



Abstract *We analytically give the financial rogue waves in the nonlinear option pricing model due to Ivancevic, which is nonlinear wave alternative of the Black–Scholes model. These rogue wave solutions may be used to describe the possible physical mechanisms for rogue wave phenomenon in financial markets and related fields.*

Rogue waves, cont.

Eur. Phys. J. Special Topics **185**, 57–66 (2010)

DOI: 10.1140/epjst/e2010-01238-7

THE EUROPEAN PHYSICAL JOURNAL SPECIAL TOPICS

Regular Article

Freak waves in laboratory and space plasmas

Freak waves in plasmas

M.S. Ruderman[a]

School of Mathematics and Statistics, University of Sheffield, Hounsfield Road, Hicks Building, Sheffield S3 7RH, UK

Received in final form and accepted 15 June 2010
Published online 23 August 2010

Rogue waves, cont.

PRL 106, 204502 (2011) PHYSICAL REVIEW LETTERS week ending 20 MAY 2011

Rogue Wave Observation in a Water Wave Tank

A. Chabchoub,[1,*] N. P. Hoffmann,[1] and N. Akhmediev[2]

[1]*Mechanics and Ocean Engineering, Hamburg University of Technology, Eißendorfer Straße 42, 21073 Hamburg, Germany*

[2]*Optical Sciences Group, Research School of Physics and Engineering, The Australian National University, Canberra ACT 0200, Australia*

(Received 28 February 2011; published 16 May 2011)

Movie

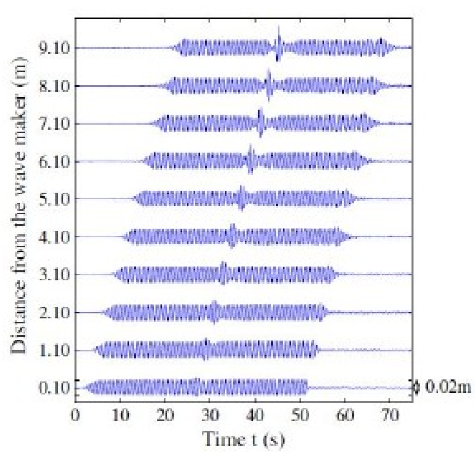
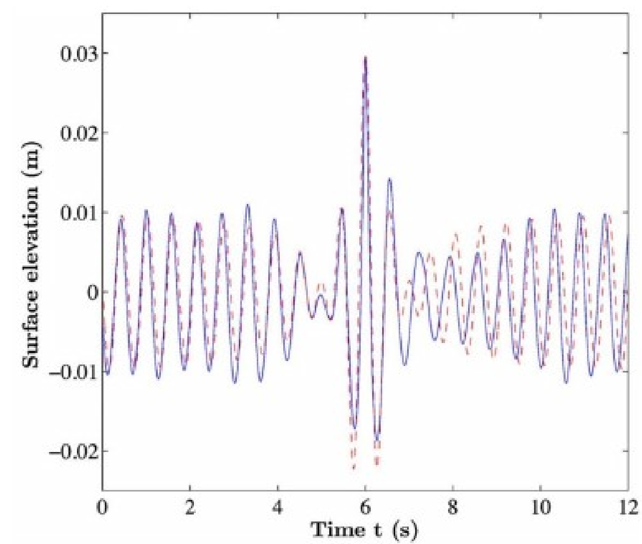


FIG. 3 (color online). Temporal evolution of the water surface height at various distances from the wave maker.



Rogue waves, cont.

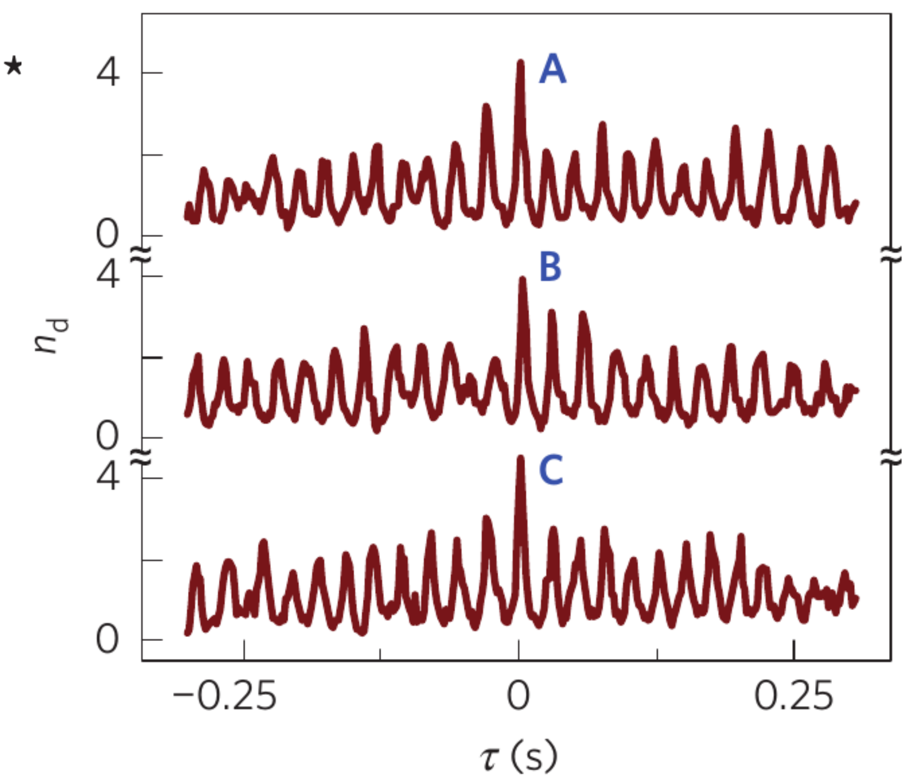
nature physics

LETTERS

PUBLISHED ONLINE: 29 FEBRUARY 2016 | DOI: 10.1038/NPHYS3669

Generation of acoustic rogue waves in dusty plasmas through three-dimensional particle focusing by distorted waveforms

Ya-Yi Tsai, Jun-Yi Tsai and Lin I*



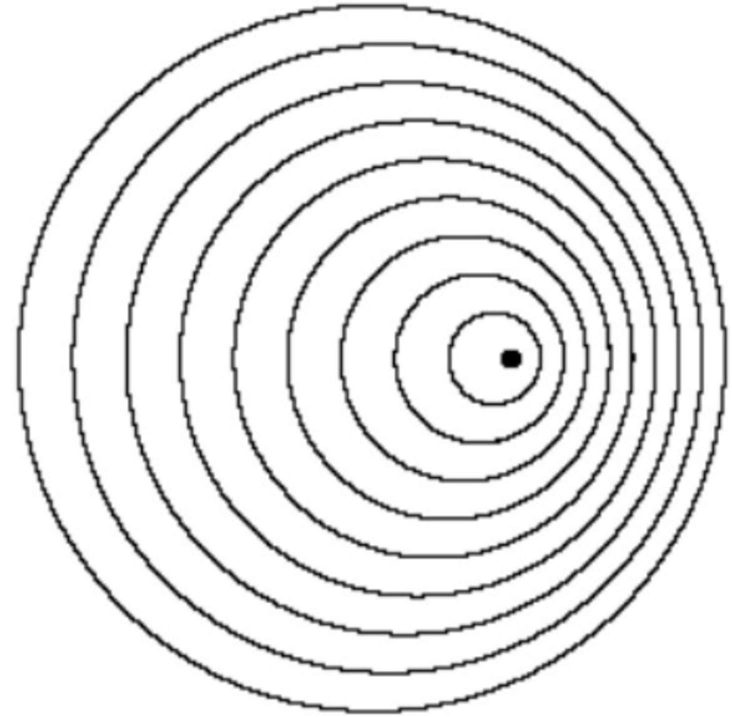
Rogue waves, cont.

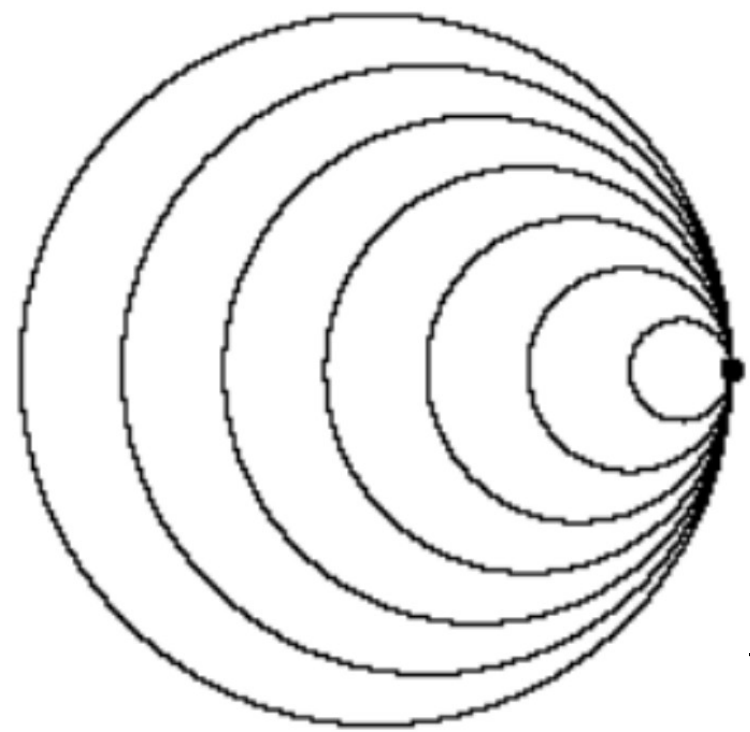
Questions need to be addressed:

- Is this the case in a nonlinear medium?
- Is Rogue wave a critical phenomena?
- Is Rogue wave unpredictable phenomena, i.e. Probabilistic phenomena or Deterministic phenomena?
- What is the mechanism of formation?
- What are the conditions of the existence?

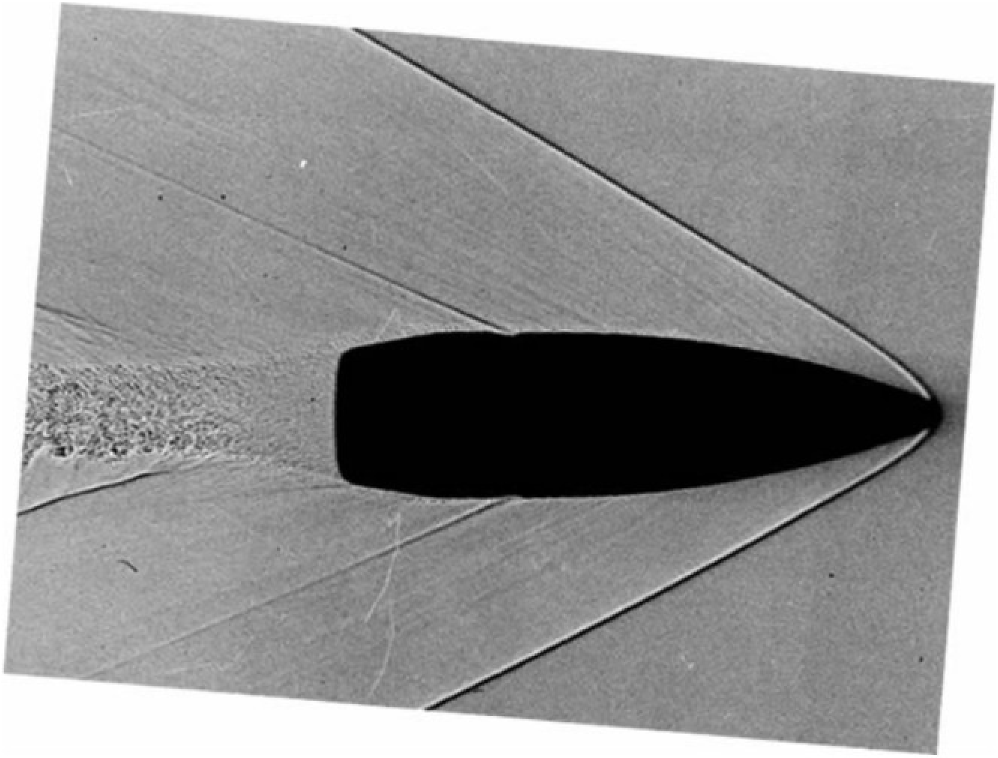
Mach Cones

- When an object moves through the air it pushes the air in front of it away, creating a pressure wave.
- This pressure wave travels away from the object at the speed of sound.
- If the object itself is travelling at the speed of sound then these pressure waves build up on top of each other to create a shock wave



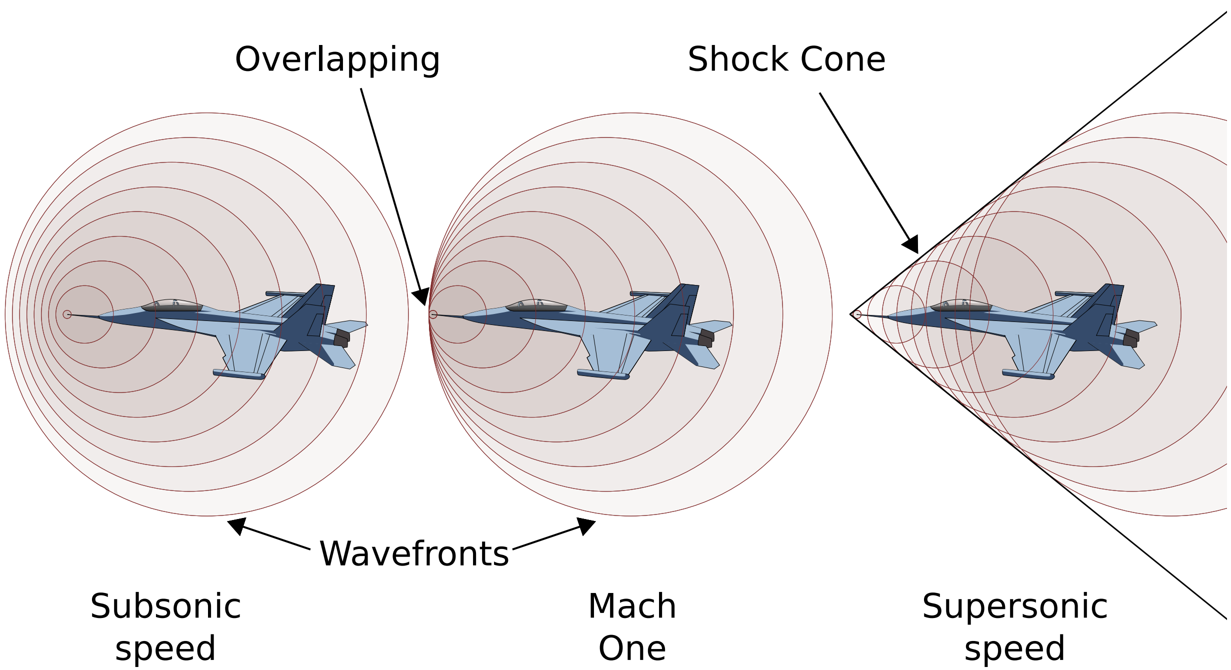


Mach Cones, cont.



In the photograph above the Mach cone angle is 28° and therefore the bullet must have been travelling at Mach 2.1 or 720 metres per second (assuming the speed of sound is 340 m/s).

Mach Cones, cont.



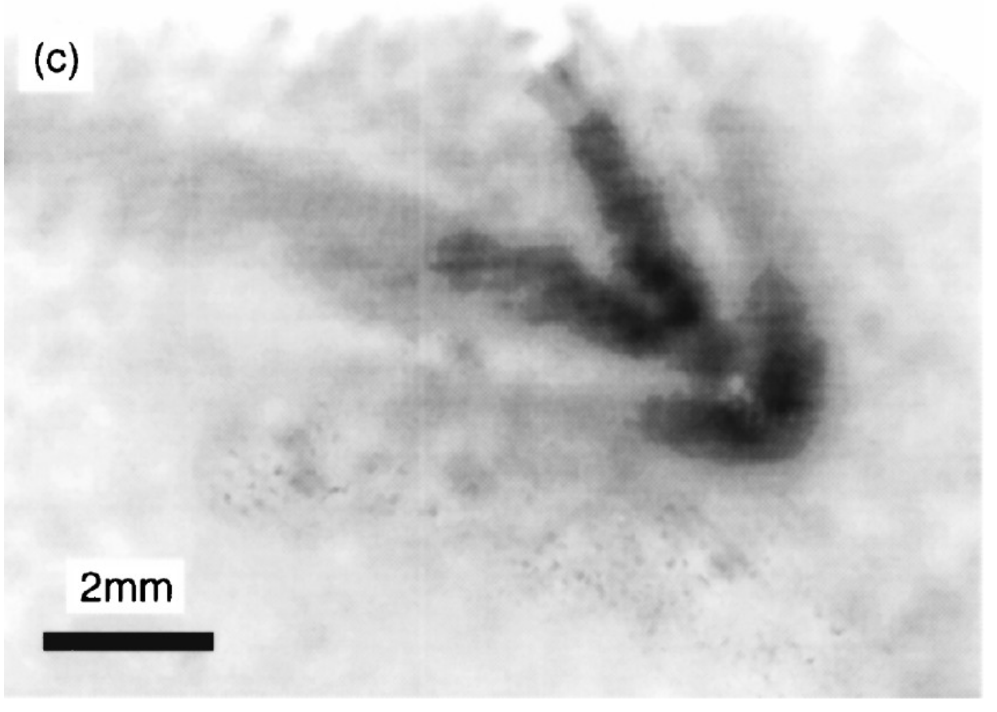
Mach Cones, cont.

VOLUME 83, NUMBER 18 PHYSICAL REVIEW LETTERS 1 NOVEMBER 1999

Mach Cones in a Coulomb Lattice and a Dusty Plasma

D. Samsonov, J. Goree,* Z. W. Ma, and A. Bhattacharjee
Department of Physics and Astronomy, The University of Iowa, Iowa City, Iowa 52242

H. M. Thomas and G. E. Morfill
Max Planck Institut für extraterrestrische Physik, 85740 Garching, Germany



Mach Cones, cont.

PHYSICAL REVIEW E VOLUME 61, NUMBER 5 MAY 2000

Mach cone shocks in a two-dimensional Yukawa solid using a complex plasma

D. Samsonov* and J. Goree†
Department of Physics and Astronomy, The University of Iowa, Iowa City, Iowa 52242

H. M. Thomas and G. E. Morfill
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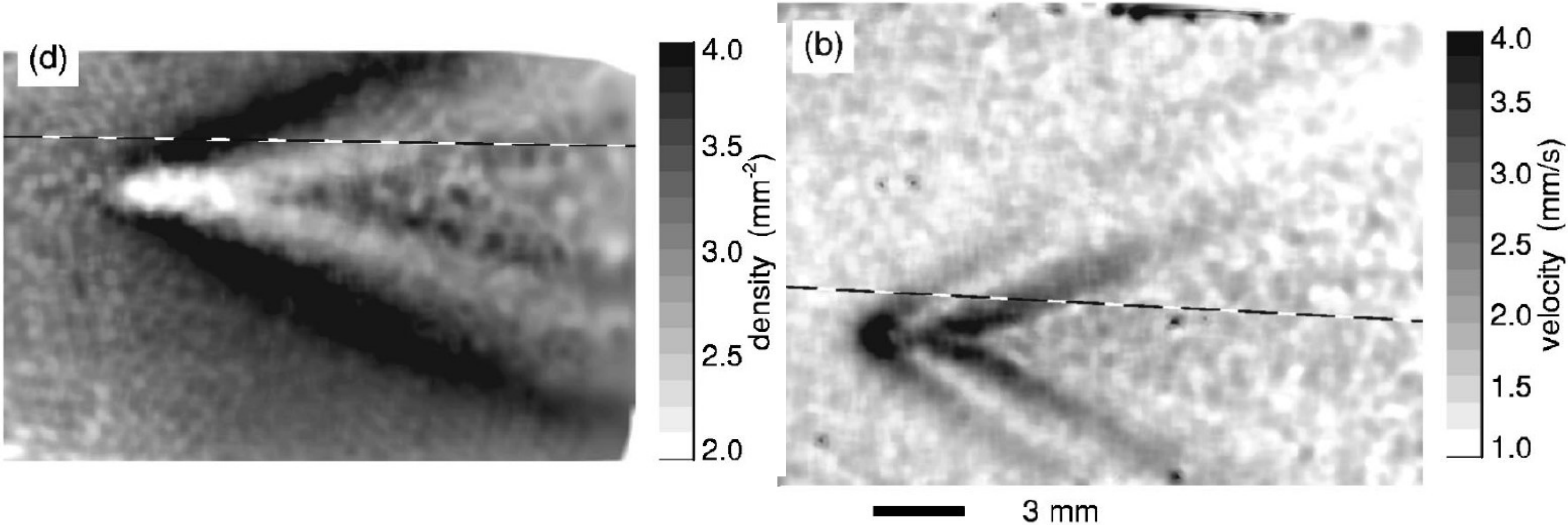
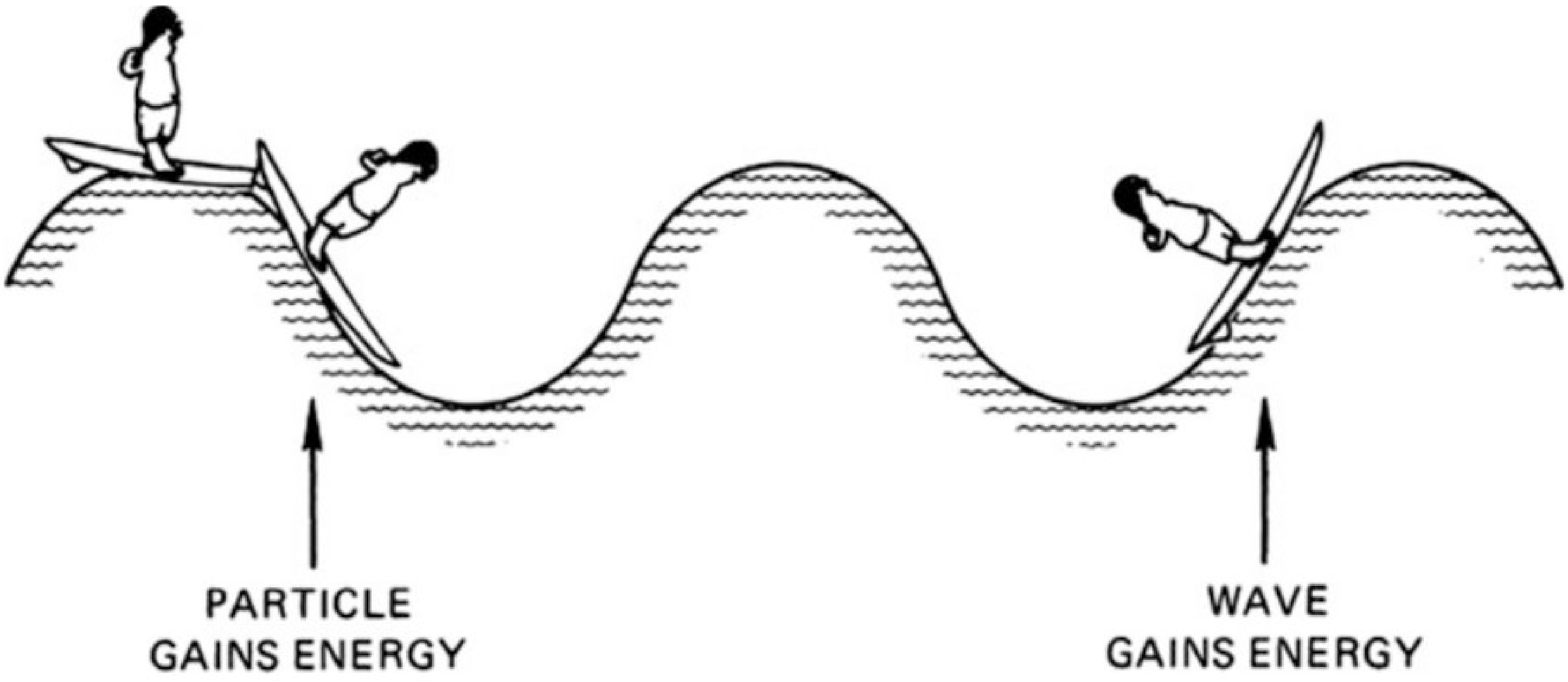


Wakefield

- In 1979 John Dawson, in a paper with T. Tajima, proposed that Landau damping effect could be used to accelerate particles
- In plasma, there are electrons both faster and slower than the wave.

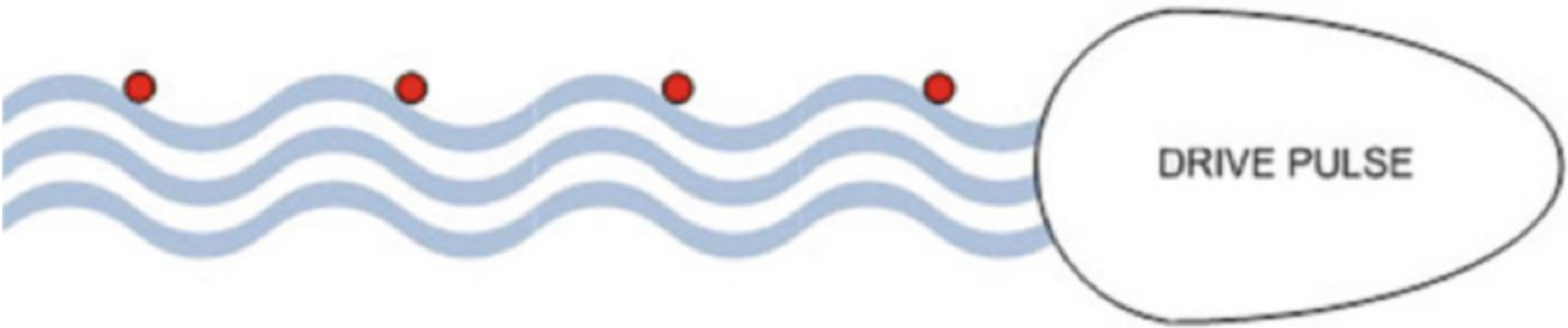


Wakefield, cont.

Wakefield, cont.

Wakefield, cont.

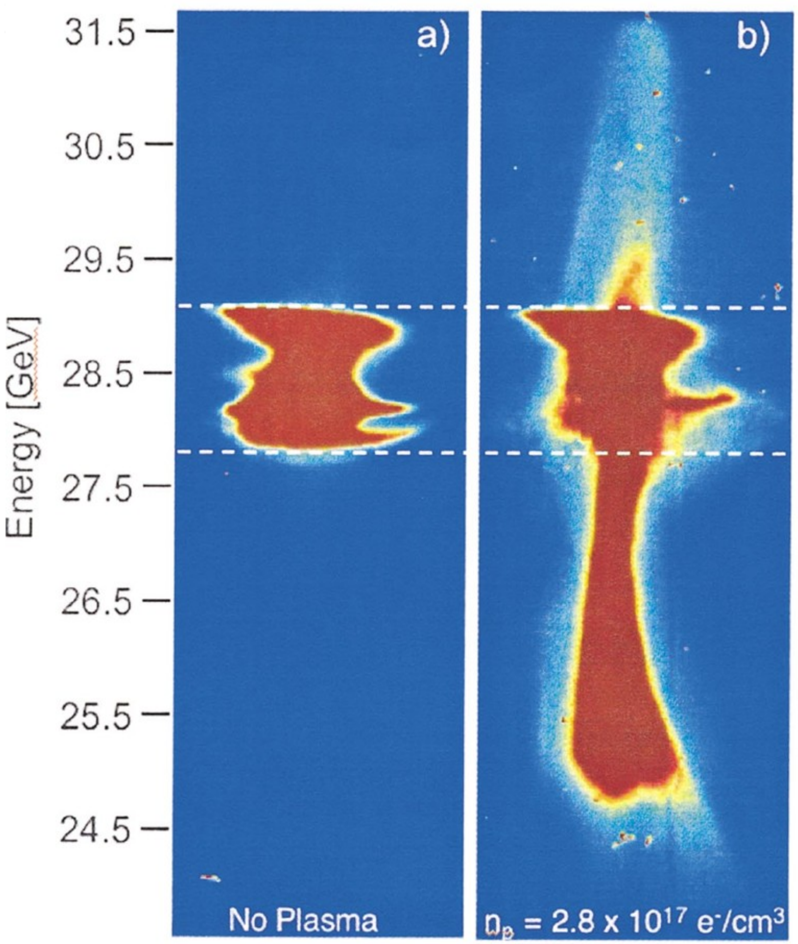
- There were two early ideas on plasma accelerators: *beatwave* and *wakefield*.



Wakefield, cont.

PRL **95,** 054802 (2005) PHYSICAL REVIEW LETTERS week ending 29 JULY 2005

Multi-GeV Energy Gain in a Plasma-Wakefield Accelerator



J. Decker,[1] S. Deng,[3] P. Emma,[1] C. Huang,[2] R. H. Iverson,[1] D. K. Johnson,[2] Lu,[2] K. A. Marsh,[2] W. B. Mori,[2] P. Muggli,[3] C. L. O'Connell,[1] E. Oz,[3] R. H. Siemann,[1] and D. Walz[1]

a) No Plasma → Only electron beam with 1 GeV energy.

b) 10 cm long lithium plasma → the core of the electron bunch has lost energy driving the plasma wake while particles in the back of the bunch have been accelerated to 2.7 GeV

Wakefield, cont.

Phys. Fluids, Vol. 28, No. 7, July 1985

Attractive potential between resonant electrons

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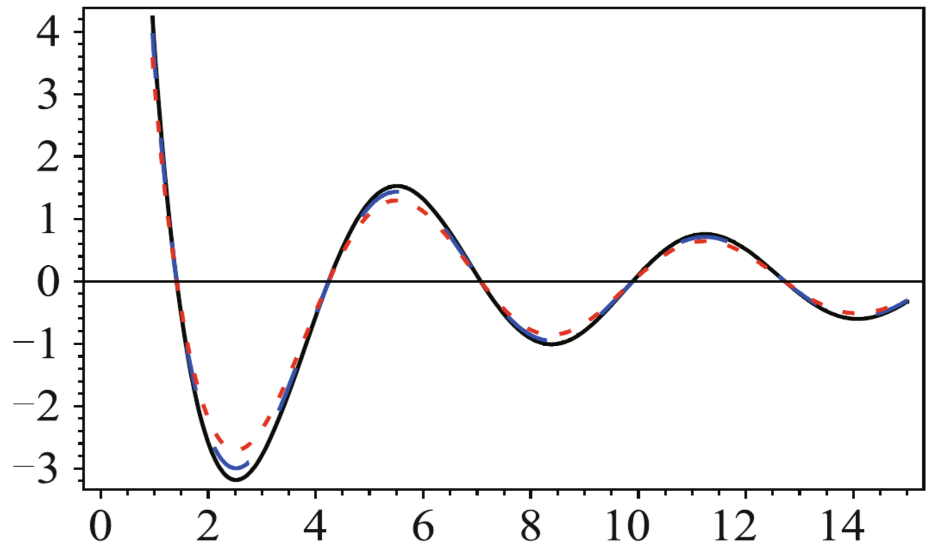
Physics Letters A 203 (1995) 40–42

Attractive forces between charged particulates in plasmas

Mitsuhiro Nambu, Sergey V. Vladimirov [1], Padma K. Shukla [2]

The charged particles having the same polarity can attract each other...!!

Wakefield, cont.



- **Vph ~ Cs**
- Appearing long-range **oscillatory wakefield**
- The background **positive ions are trapped** in the negative part of the oscillatory wake potential.
- The **negative charges are attracted** to each other as they are **glued by positive ions** in a linear chain