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TOGETHER FOR BRIGHT FUTURE

Laser and Quantum Plasmas

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Outline

- **Introduction.**
 - **Plasma State**
 - **Solid State**
 - **Warm dense matter.**
- **Warm Dense Matter**
 - **Motivation behinde the study**
 - **Generation**
 - **Invistigation**
 - **Simulation**
- **Summary**

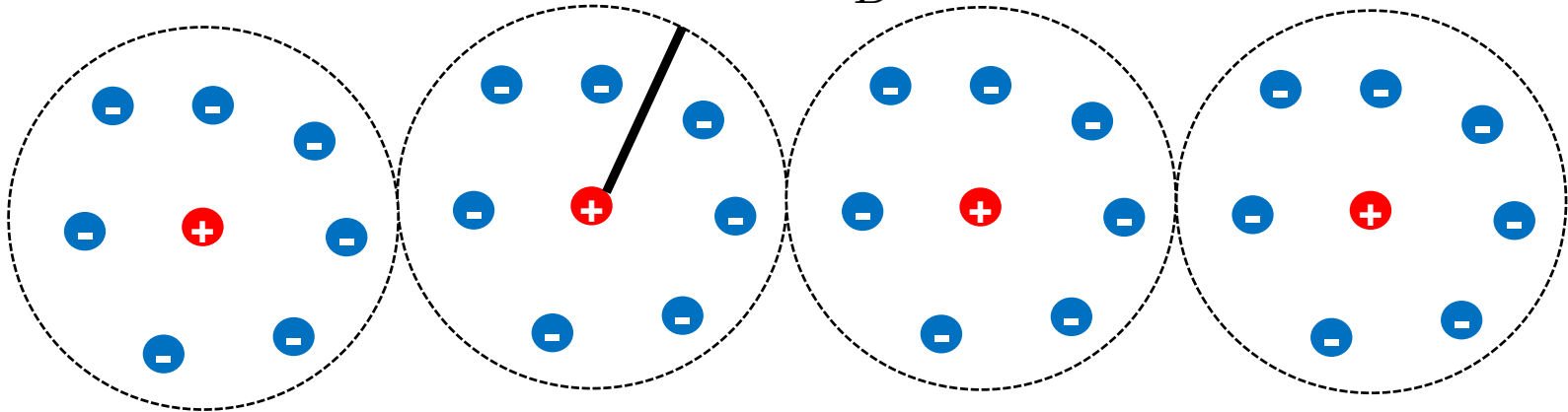




Debye length

- The Debye radius is the distance at which the potential of an ion charge is decreased by 0.37 of its value in free space.

$$r \approx \lambda_D$$



$$\lambda_D = \sqrt{\frac{\epsilon(K_B T_e + K_B T_i)}{Z e^2 n_0}} \quad \Lambda_D = \frac{1}{Z n_0} \left(\frac{\epsilon K_B T_e}{e^2} \right)^{3/2}$$

- In ideal plasma the number of charges Λ_D in the Debye sphere must be large.

Debye length



- In a plasma with electron temperature $T_e = 10000\text{eV}$ and electron density $n_e = 10^{14}\text{cm}^{-3}$, the number of particles in Debye sphere is 4×10^7 .
- In Hot Dense Plasma: the number of particles in Debye sphere is 4 when $T_e = 100\text{eV}$ and $n_e = 10^{22}\text{cm}^{-3}$.
- In Warm Dense plasma, the number of charges in Debye sphere might be less than 1.
- Note: WDM does not obey the plasma state theories.



Collision frequency

- In a simple model where ions are assumed to be immobile, the electron ion collision frequency is given as

$$\nu_{ei} = \frac{8\pi Z^2 e^2 n_i}{3^{3/2} m_e^{1/2} (K_B T_e)^{3/2}} \ln \Lambda_c$$

- Coulomb logarithm

$$\Lambda_c = \frac{(K_B T_e)^{3/2}}{2 Z e^2 \sqrt{4\pi e^2 n_i}}$$

- For WDM the collision frequency is negative value.



Conductivity I

- From the generalized Ohm's law

$$I = \frac{1}{R} V \quad \vec{J} = \sigma \vec{E}$$

- The current density in an ideal plasma is proportional to the applied electric field.

$$\sigma = \frac{e^2 n_e}{m_e \nu_{ie}} = \frac{3^{1/2}}{8\pi Z e^2 m_e^{1/2}} \frac{(K_B T_e)^{3/2}}{\ln(\Lambda_c)}$$

- At constant density:

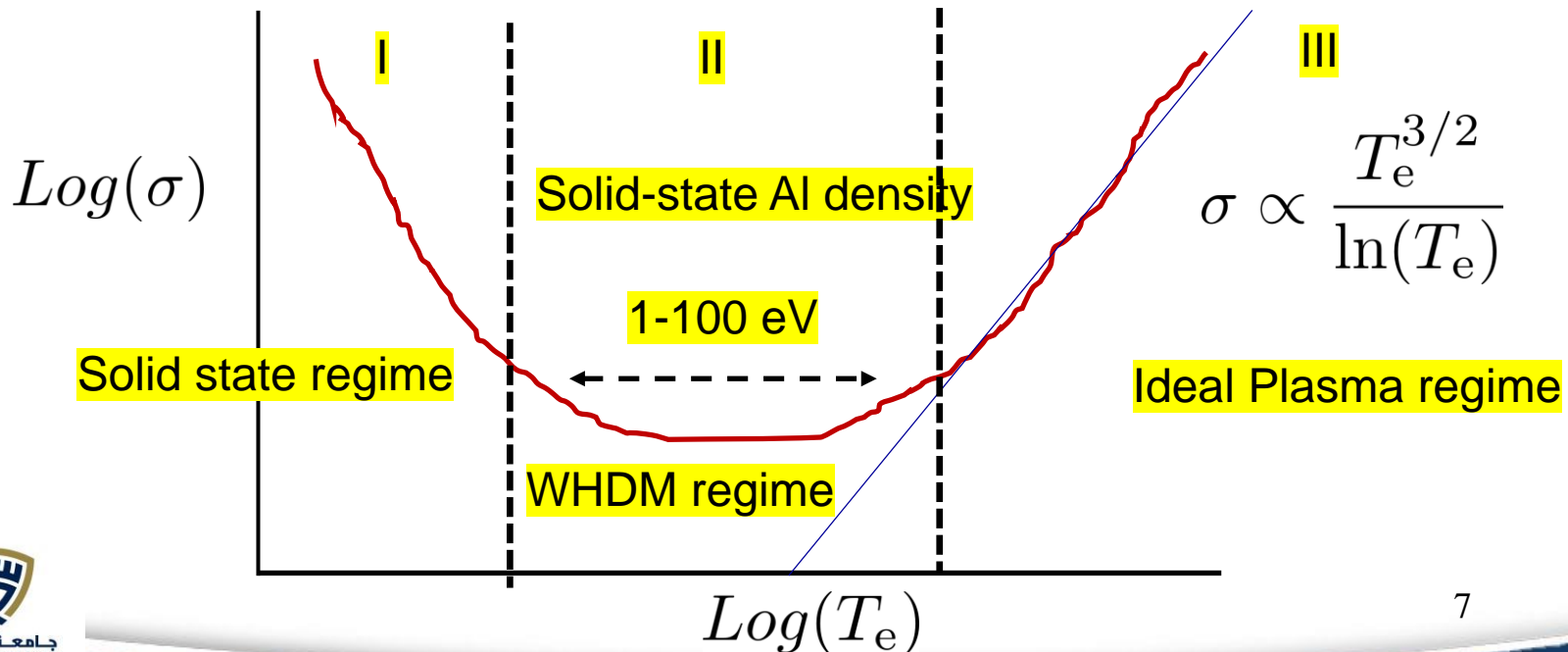
$$\sigma \propto \frac{T_e^{3/2}}{\ln(T_e)}$$

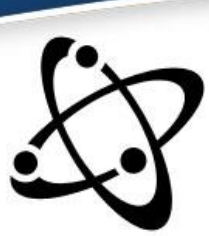


Conductivity II

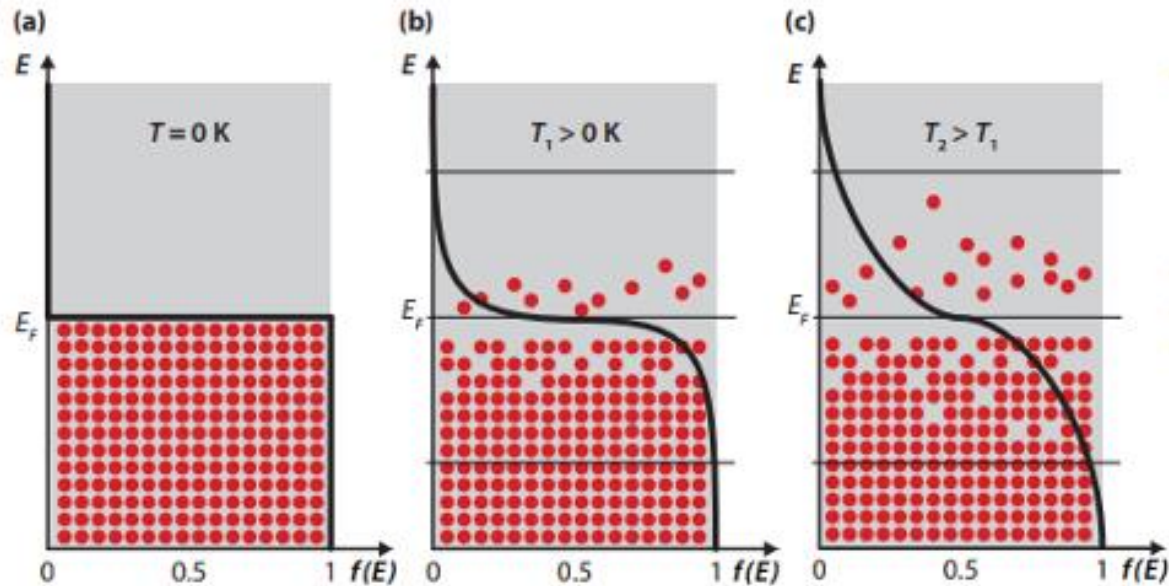
The plasma conductivity

$$\sigma = \frac{e^2 n_e}{m_e \nu_{ie}} = \frac{3^{1/2}}{8\pi Z e^2 m_e^{1/2}} \frac{(K_B T_e)^{3/2}}{\ln(\Lambda_c)}$$





Free electron gas theory



- Fermi-Dirac Distribution

$$f(E) = \frac{1}{e^{(E-E_f)} + 1} \quad E_f = \frac{\hbar^2}{2m} (3\pi^2 n)^{2/3}$$

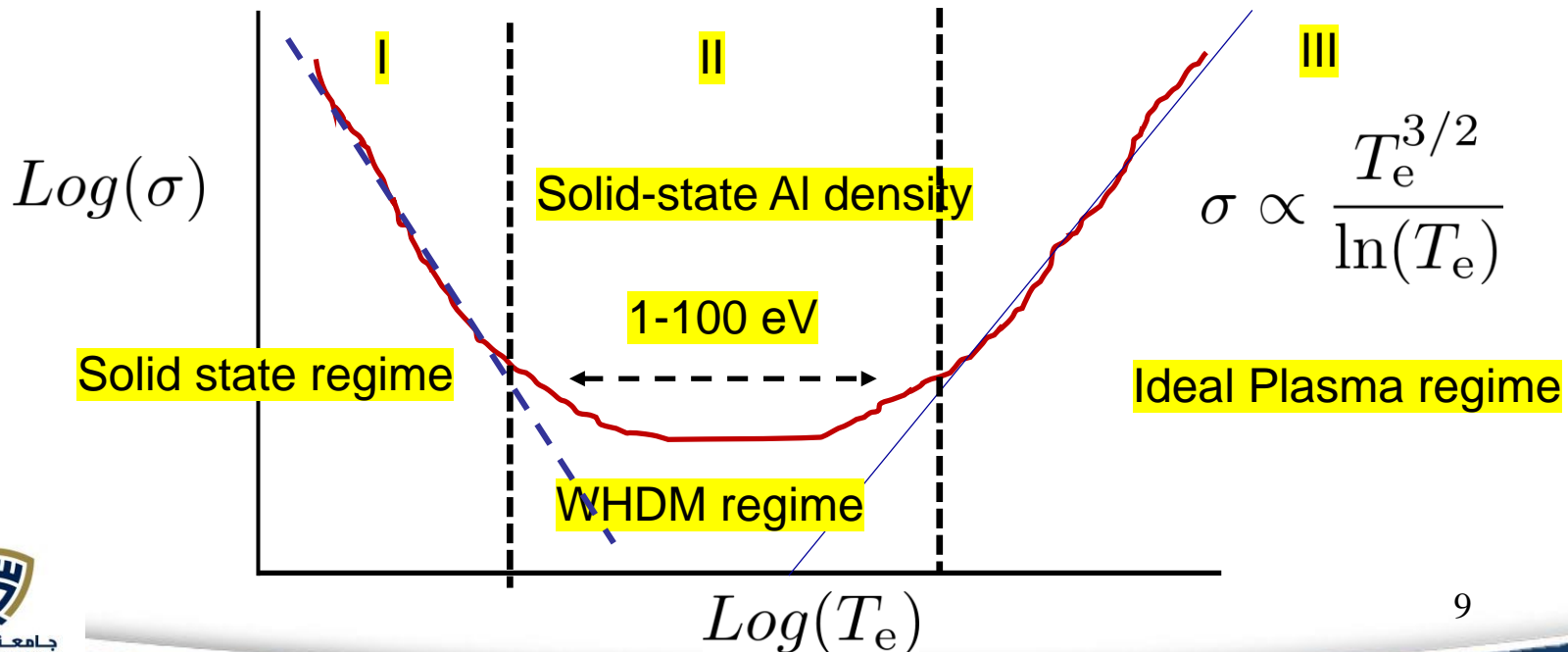
- For solid state density: $E_f \approx 2.2eV$



Conductivity III

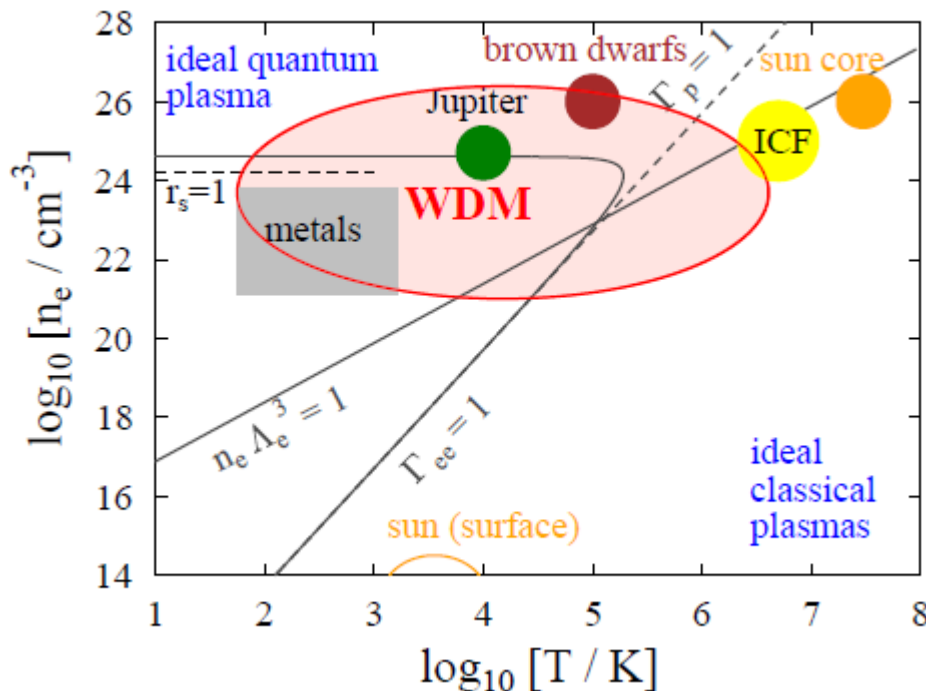
- The conductivity of a metal decreases by increasing the temperature.

$$\sigma = \frac{e^2 n_e}{m_e \nu_{ie}} \propto \frac{1}{T}$$





Warm Dense Matter



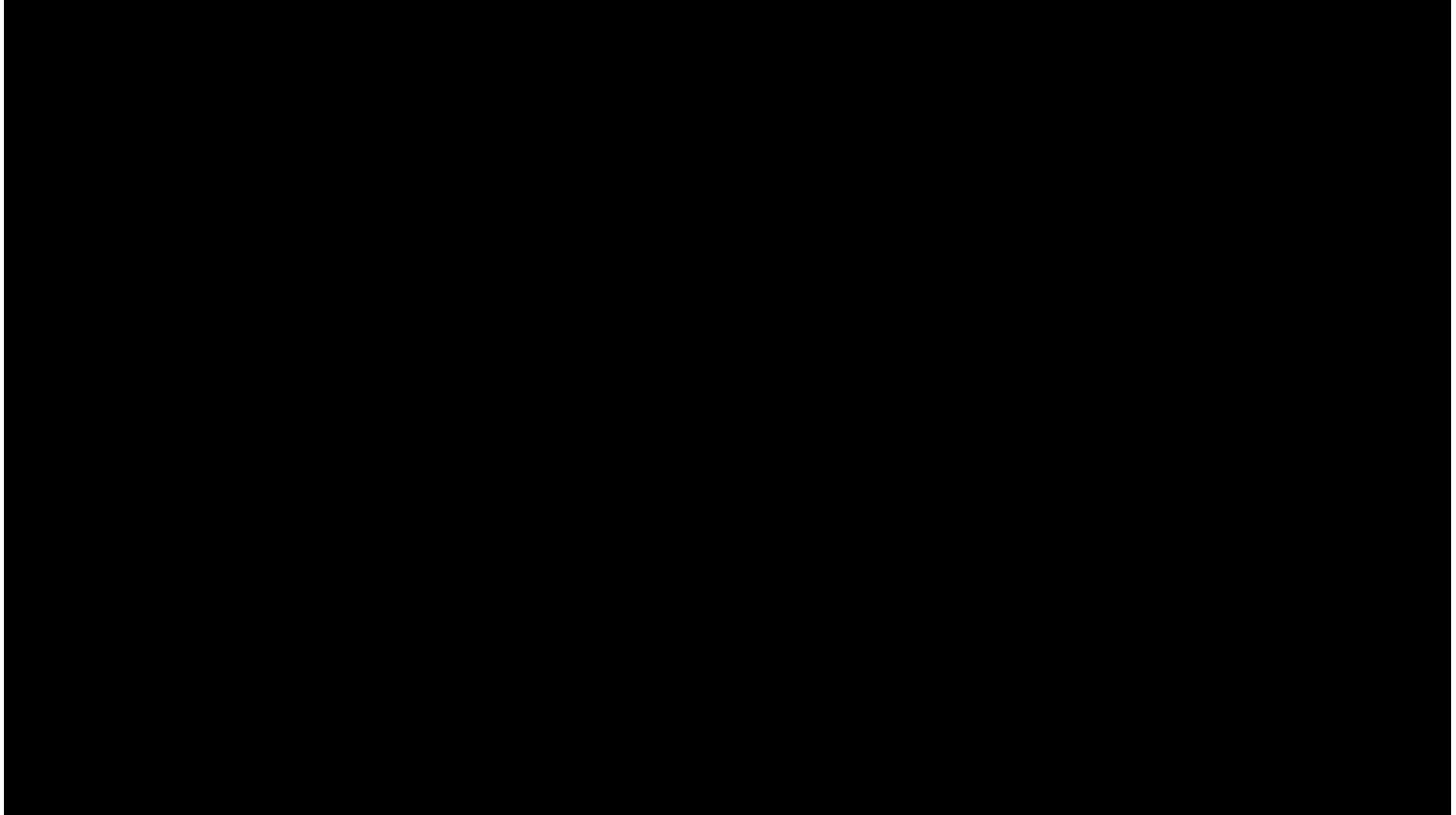
K. Wünsch

- WDM:
 - Temperature of few electronvolts
 - Solid state density and beyond
- ICF, shock experiments, giant planets, and brown dwarfs
- Theories of solid, condensed matter, or ideal plasma are not valid
- No single theoretical model describes the behavior of WDM
 - Partial ionization
 - Arbitrary degeneracy
 - Strong ionic correlations

Glenzer et al PRL 98 065002(2007)

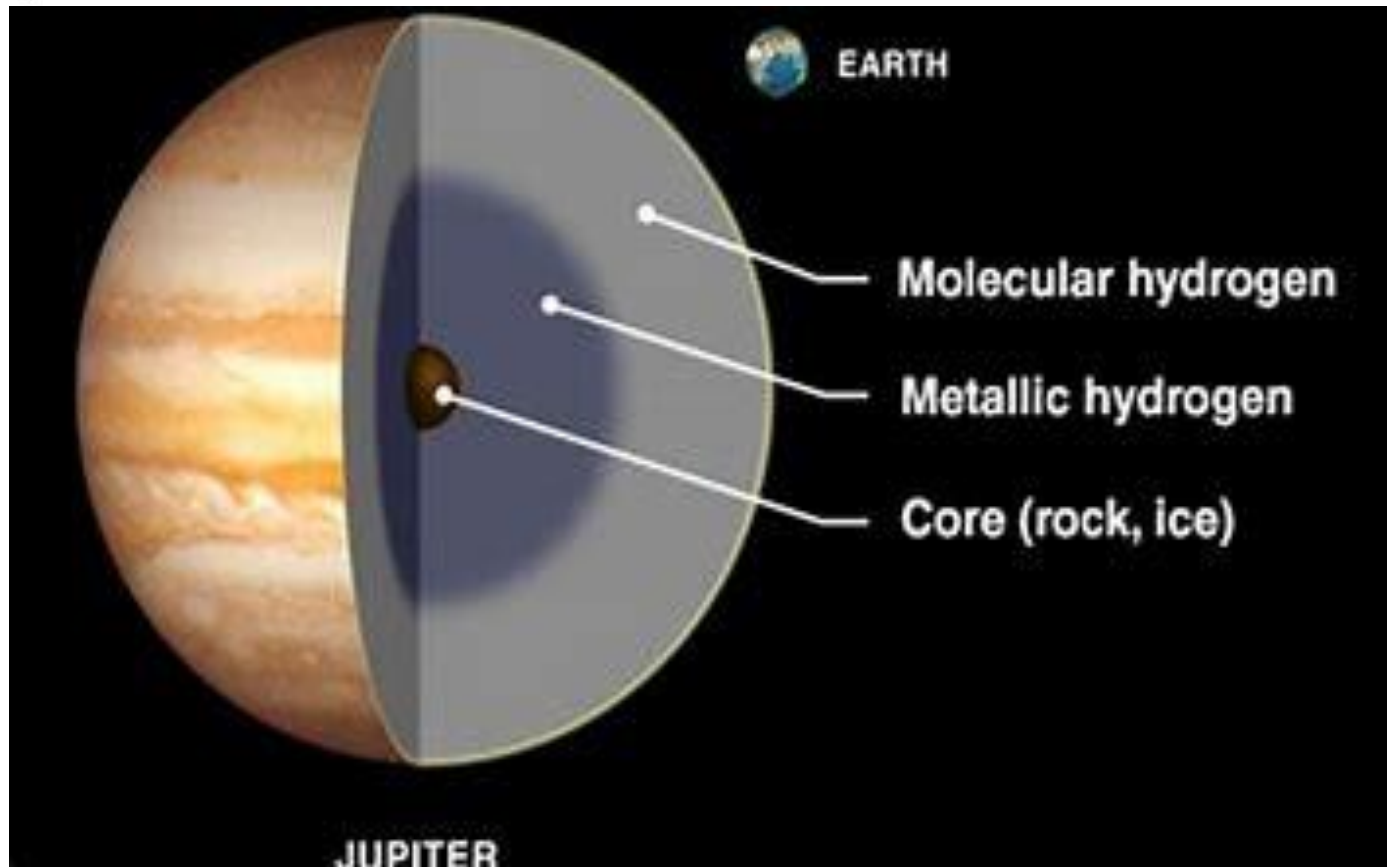


WDM in Laboratory



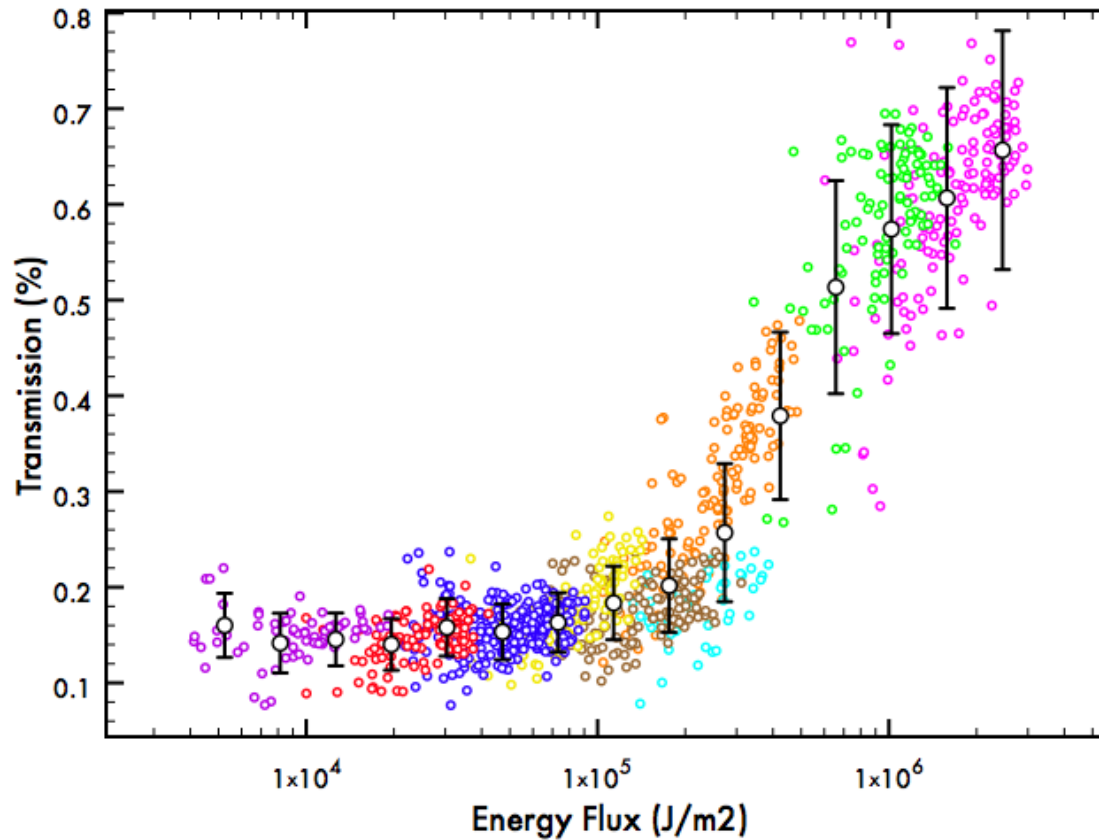


Metallic Hydrogen in Jupiter



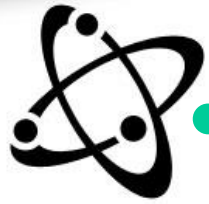


Transparent Aluminum



1986

Nagler et al, nature physics 5, 693(2009)



WDM parameters I

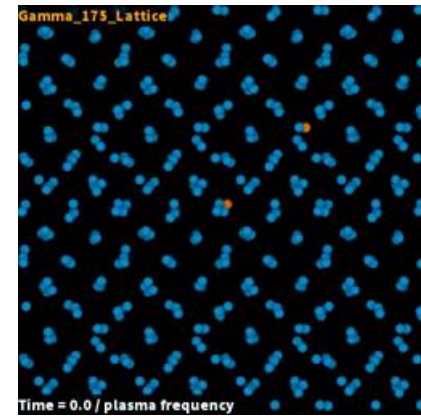
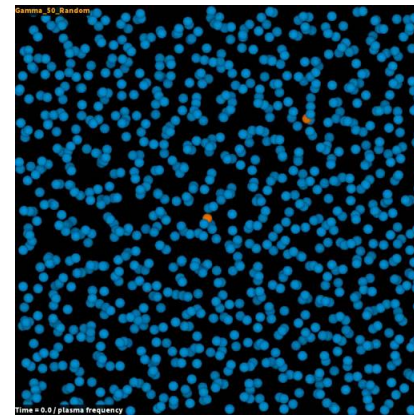
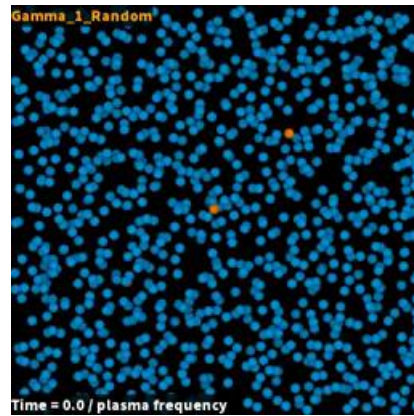
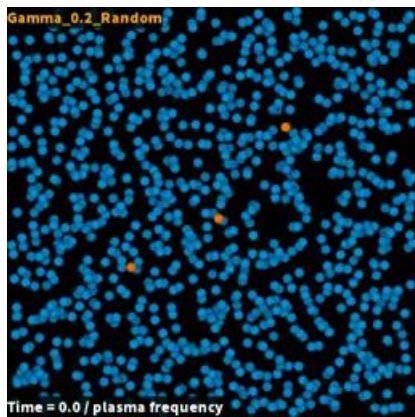
● The coupling factor:
$$\Gamma = \frac{P.E.}{K.E.} = \frac{e^2}{4\pi\epsilon_0 K_B T_e} \left(\frac{4\pi n_e}{3} \right)^{1/3}$$

$\Gamma = 0.1$

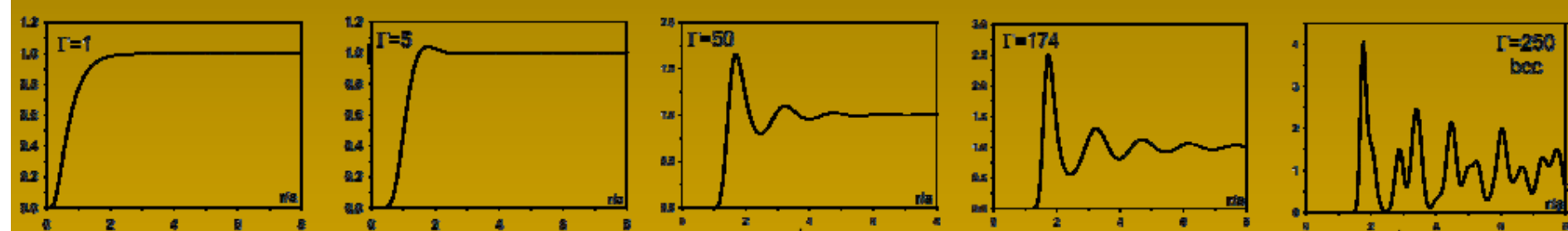
$\Gamma = 1$

$\Gamma = 50$

$\Gamma = 175$



pair distribution function $g(r)$





WDM parameters II

- The degeneracy factor:

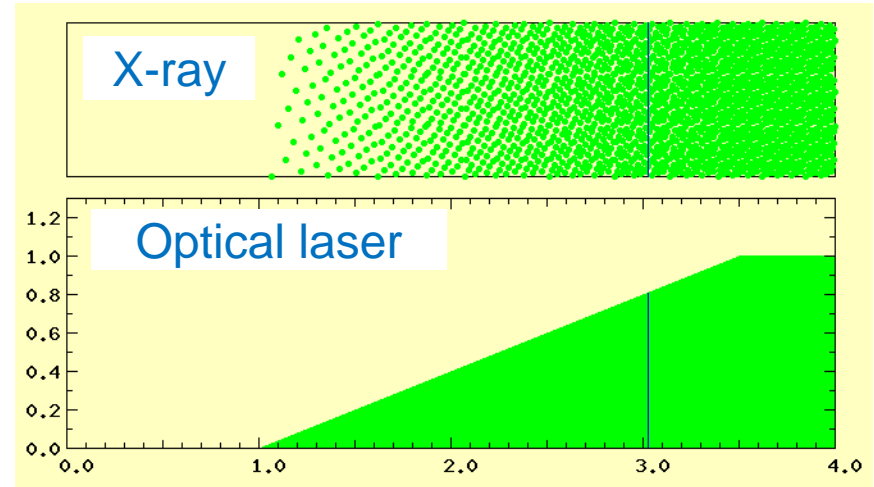
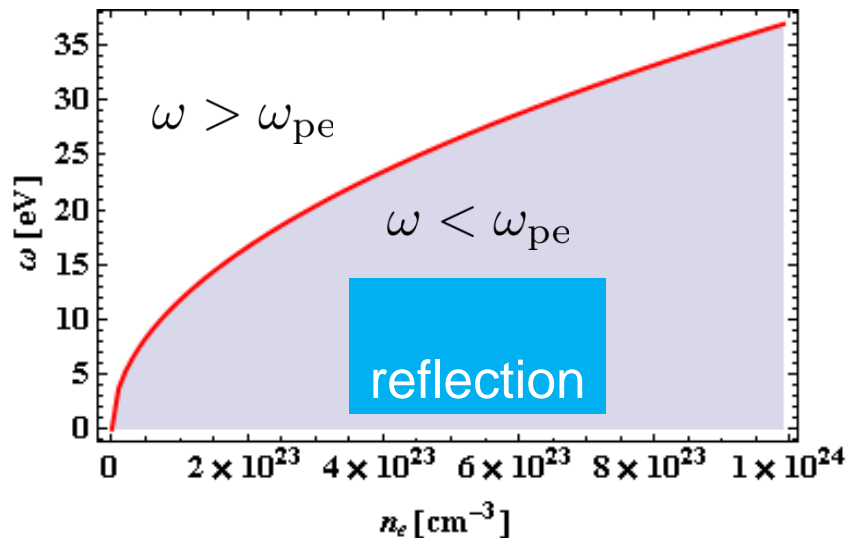
$$\theta_e = \frac{K_B T_e}{E_f} = \frac{2m_e K_B T_e}{\hbar^2} (3\pi^2 n_e)^{-2/3}$$

- When $\theta_e < 1$, most electrons populate states in Fermi sea. Quantum effects are important.
- The screening length or Debye length must be calculated from Fermi distribution not from Maxwell-Boltzmann distribution like in ideal plasma.

$$\lambda_D^{-2} = \frac{e^2 m_e^{3/2}}{\sqrt{2}\pi^2 \epsilon_0 \hbar^3} \int dE E^{-1/2} f(E)$$



Dispersion relation of EM in WDM



Warwick UK

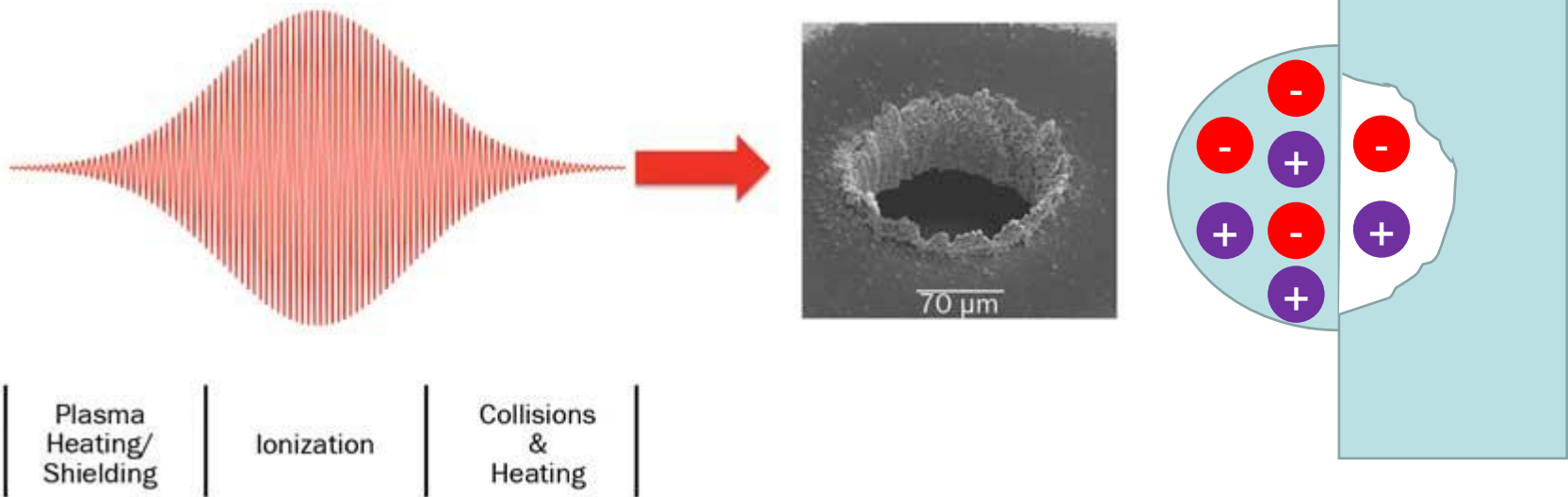
- At the natural plasma oscillation: $\omega_{pe} = \omega \rightarrow k = 0$
- At the cut off, the wave is reflected: $\omega_{pe} > \omega \rightarrow k = i\kappa$
- WDM is transparent in x-ray regime:

$$n_e = 10^{24} \text{cm}^{-3} \rightarrow \lambda \leq 33 \text{nm}$$



Plasma creation over solid targets

- The first seed of electrons are generated via MPI, Tunnel ionization, or , BSI.
- The free electrons gain energy from the laser electric field, then make further ionization by collision with neutral particles in the target.

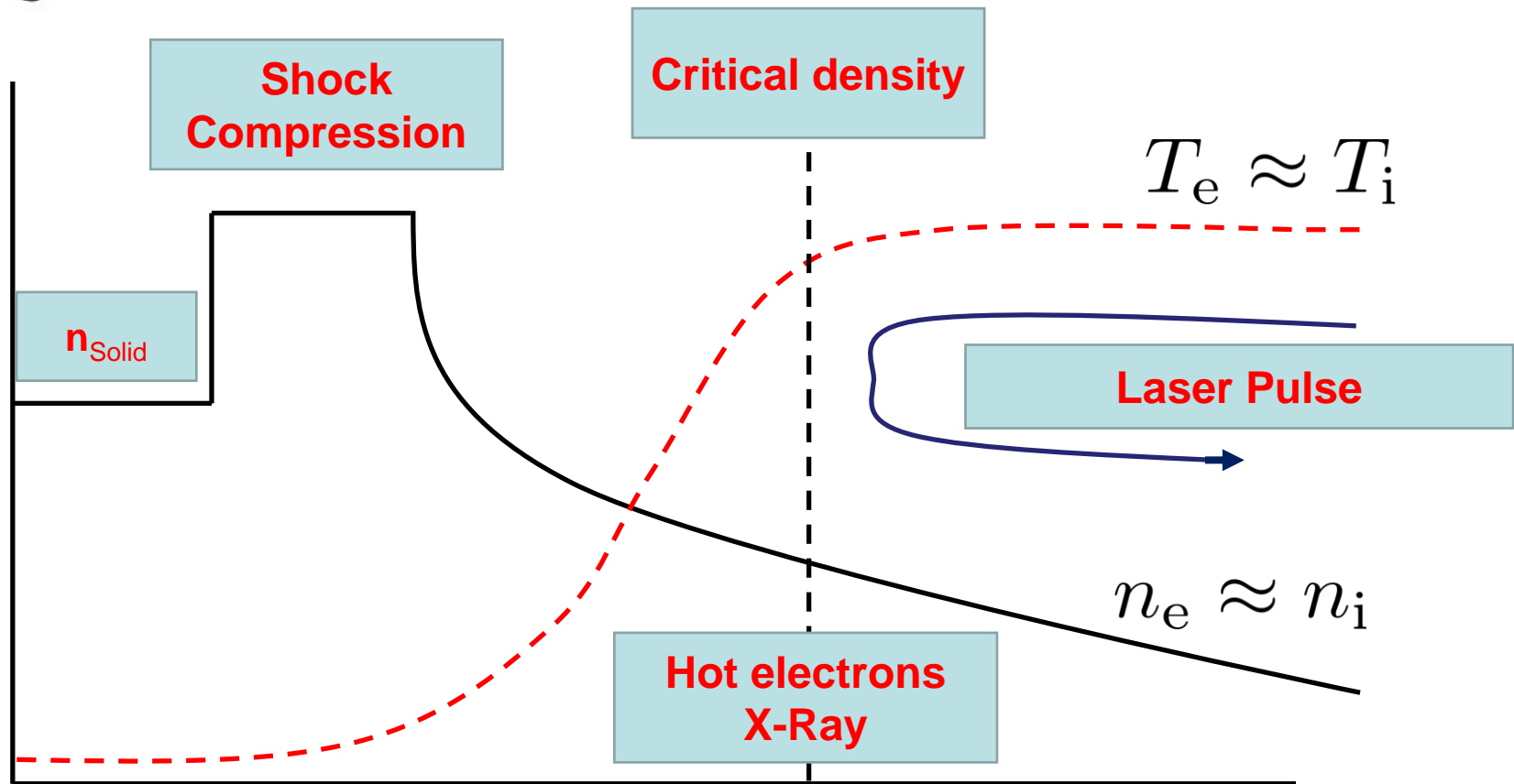


Photonics.com



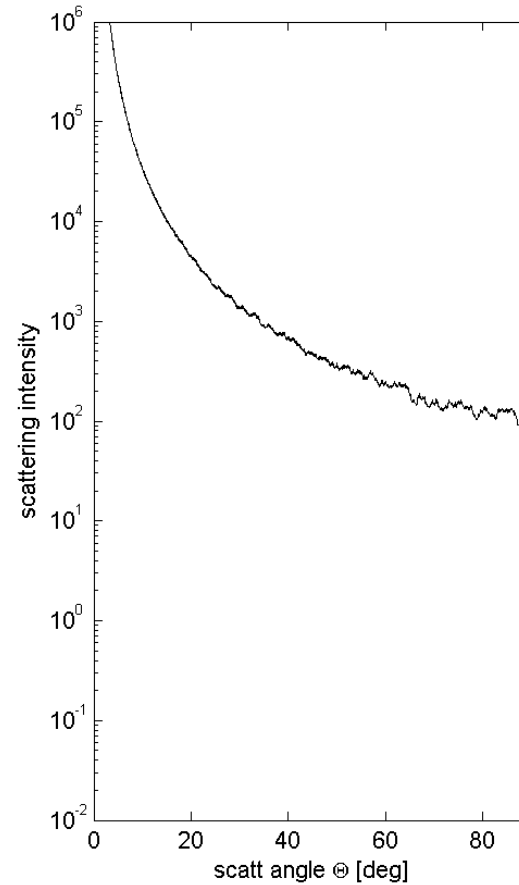
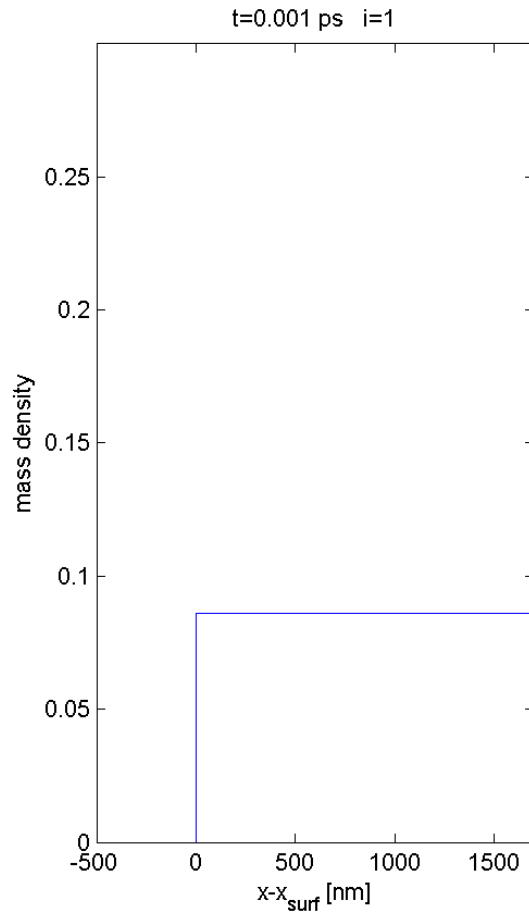


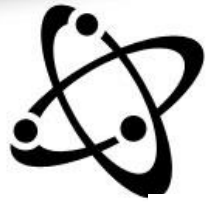
Nano-second optical laser



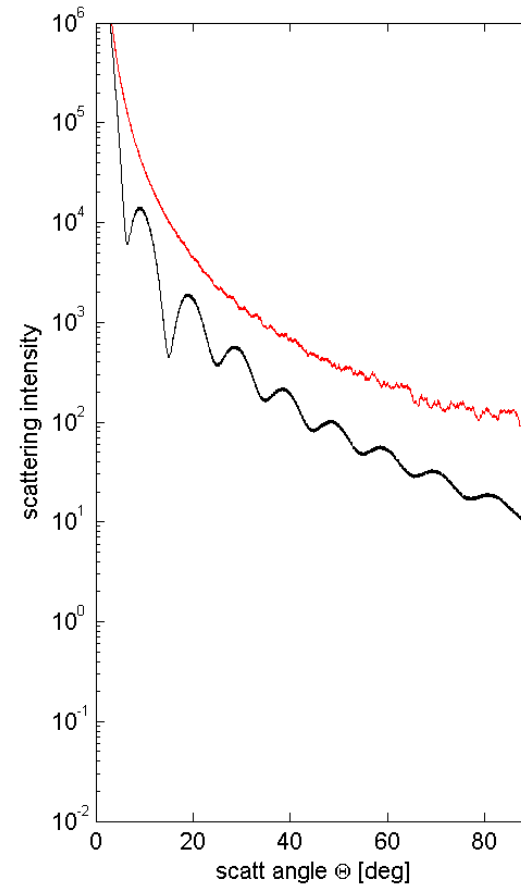
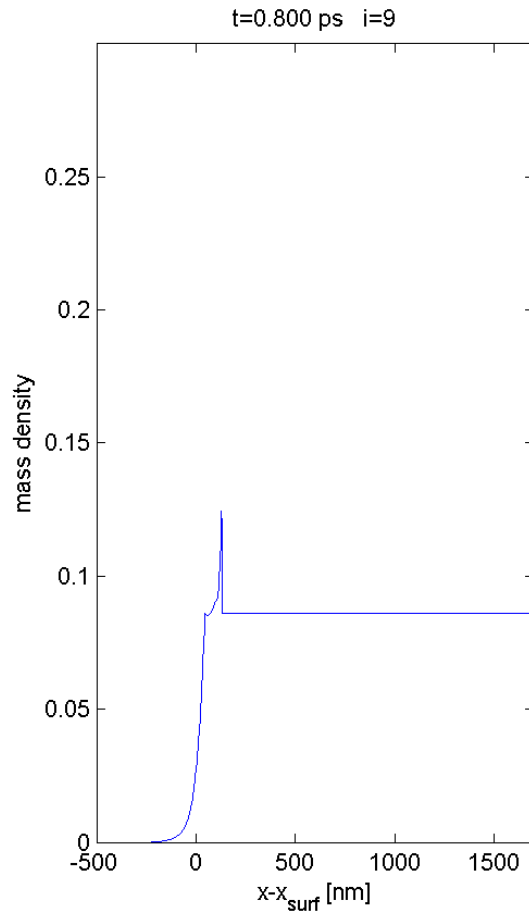


Shock waves and compression



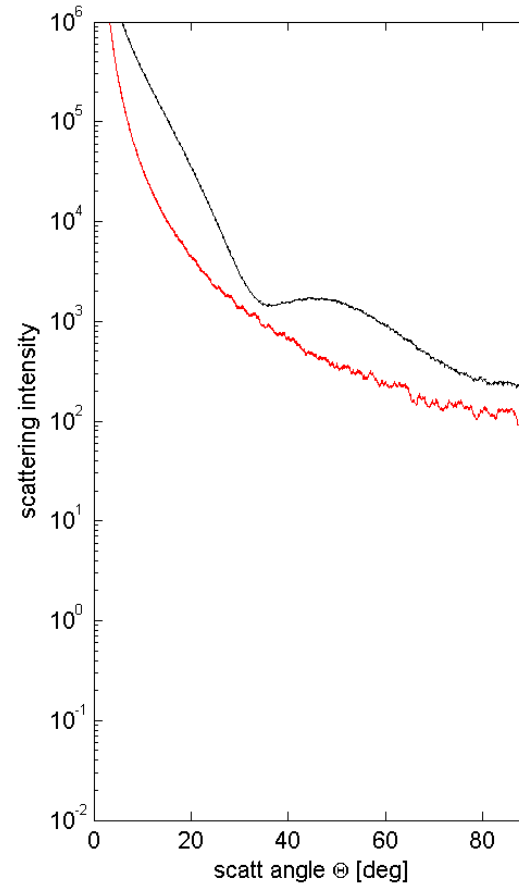
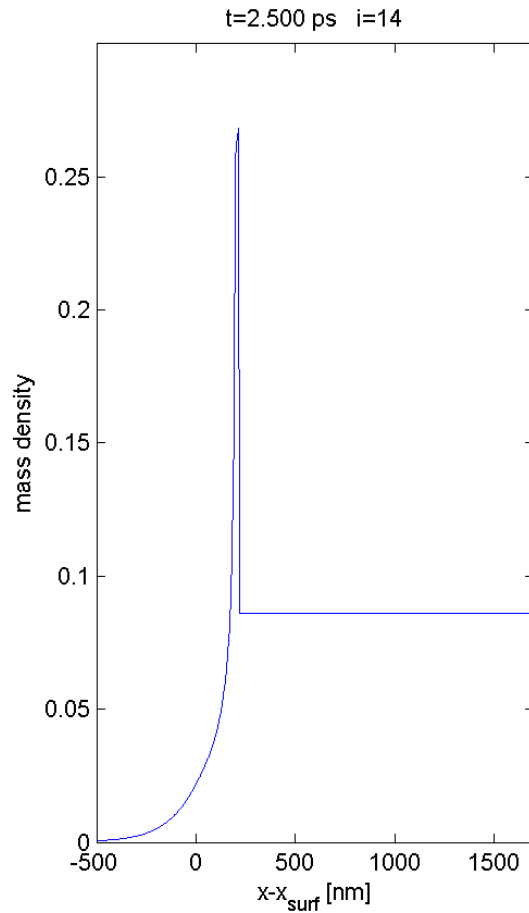


Shock waves and compression



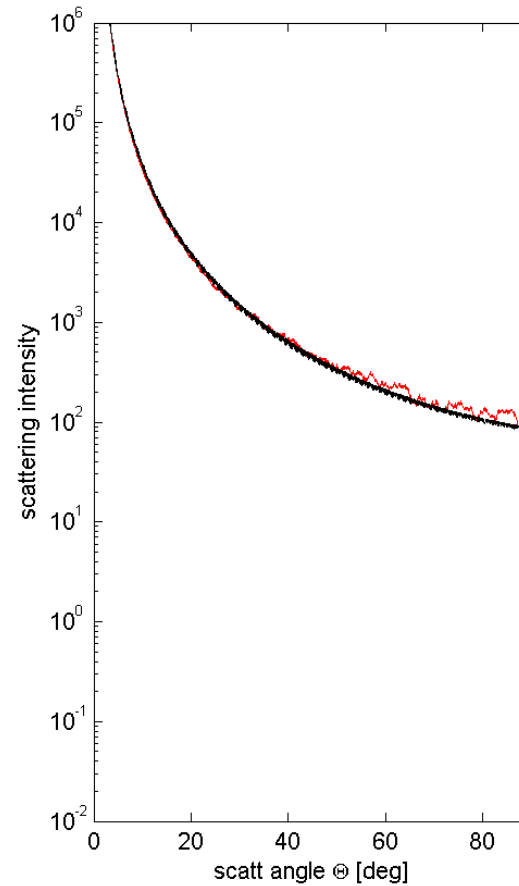
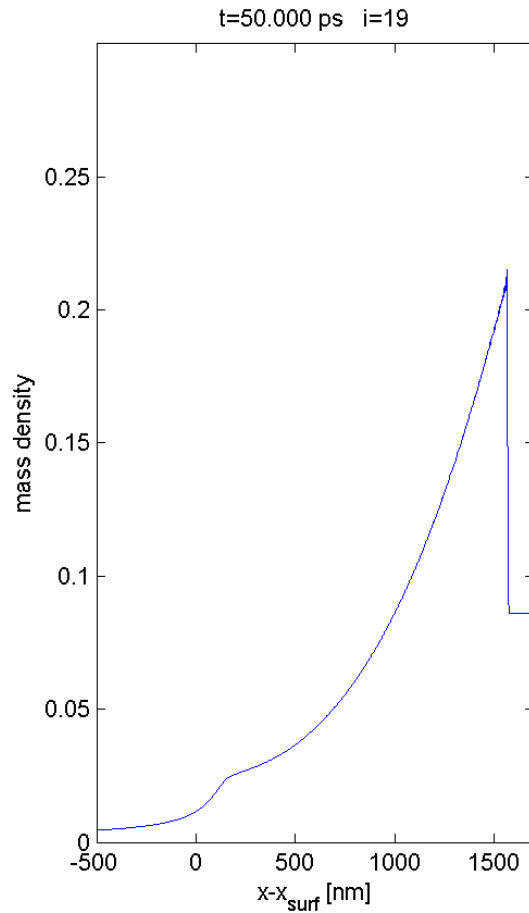


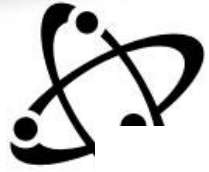
Shock waves and compression



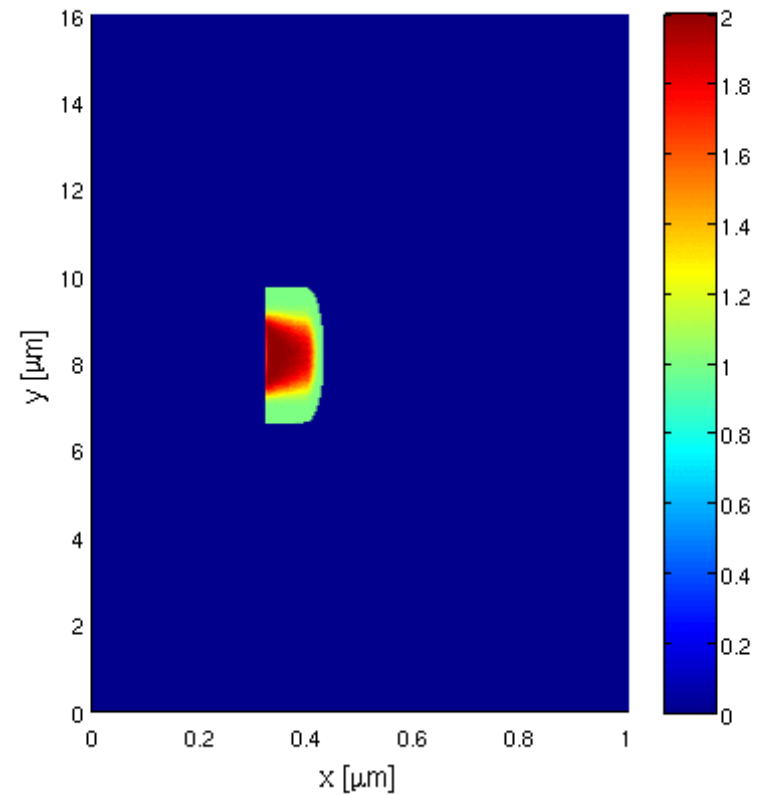
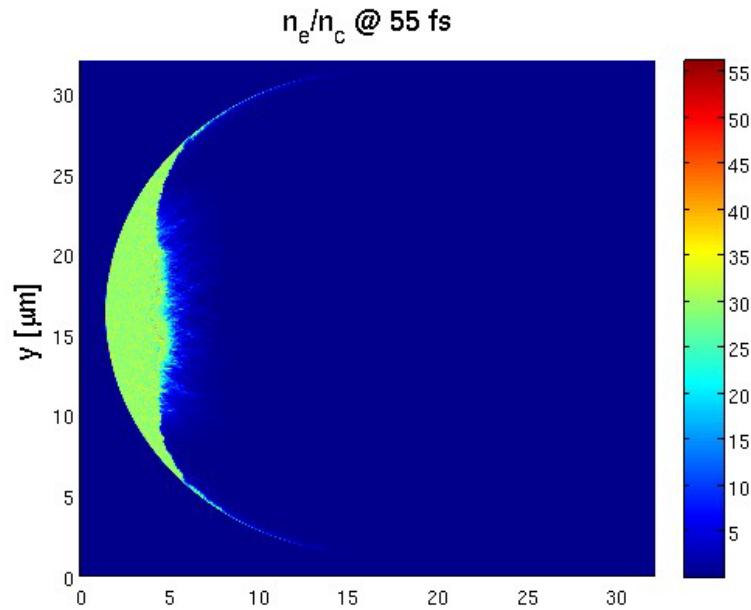


Shock waves and compression



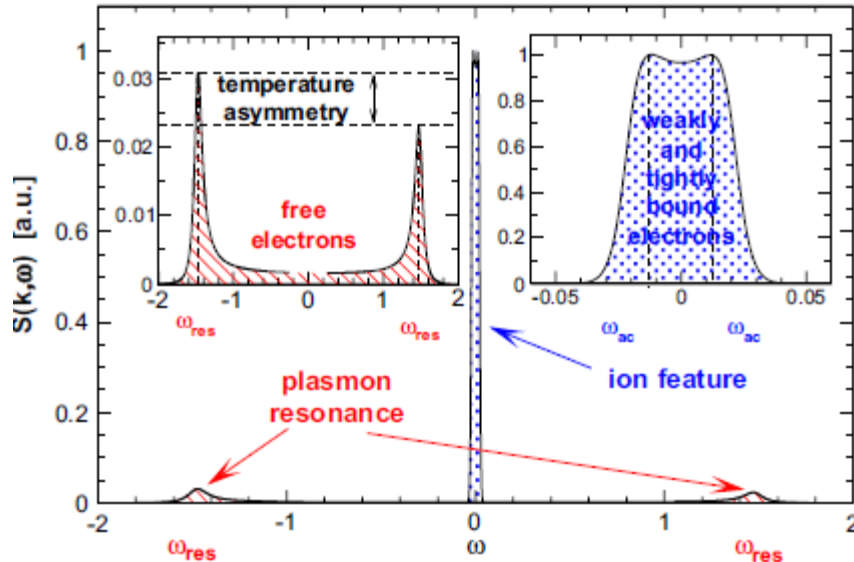


Surface waves





X-ray Thomson scattering



A. Höll et al., HEDP 3, 120(2007)

- Thomson scattering has two distinct features:

- Inelastic scattering (frequency shifted) from free electrons and bound free transitions
- Unshifted Rayleigh peak (elastic) due to electrons co-moving with the ions

- The electrons in partially ionized system can be split into bound and free electrons

$$\rho_e = \rho_b + \rho_f$$

- Intermediate scattering function

$$N_e F_{ee}^{tot} = \langle \rho_b(\vec{k}, t) \rho_b(-\vec{k}, t) \rangle + 2 \langle \rho_f(\vec{k}, t) \rho_b(-\vec{k}, t) \rangle + \langle \rho_f(\vec{k}, t) \rho_f(-\vec{k}, t) \rangle$$



Born-Mermin approximation

- Fluctuation-dissipation theorem :

$$S_{ee}^0(k, \omega) = -\frac{\epsilon_0 \hbar k^2}{\pi e^2 n_e} \frac{\text{Im} \epsilon^{-1}(k, \omega)}{1 - \exp(-\hbar \omega / k_B T_e)}$$

- RPA given by Lindhard:

$$\epsilon^{\text{RPA}}(\vec{k}, \omega) = 1 - \frac{1}{\epsilon_0 \Omega_0 k^2} \sum_p e^2 \frac{f_{p+k/2}^e - f_{p-k/2}^e}{\Delta E_{p,k}^e - \hbar(i\omega + i\eta)}$$

- Mermin ansatz :

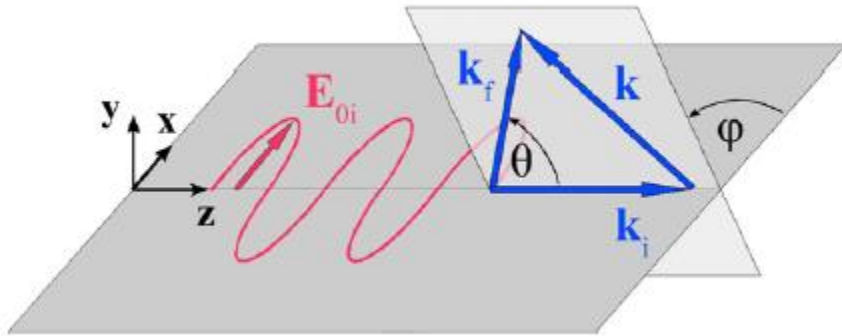
$$\epsilon_M(k, \omega) = 1 + \frac{\left(1 + \frac{i\nu(\omega)}{\omega}\right) [\epsilon^{\text{RPA}}(k, \omega + i\nu(\omega)) - 1]}{1 + i \frac{\nu(\omega)}{\omega} \frac{\epsilon^{\text{RPA}}(k, \omega + i\nu(\omega)) - 1}{\epsilon^{\text{RPA}}(k, 0) - 1}}$$

- $\nu(\omega)$ is the dynamic collision frequency via Born approximation.

Glenzer and Redmer, RMP 81, 1625(2009)



Back and forward scattering



- The momentum transfer depends on the scattering angle

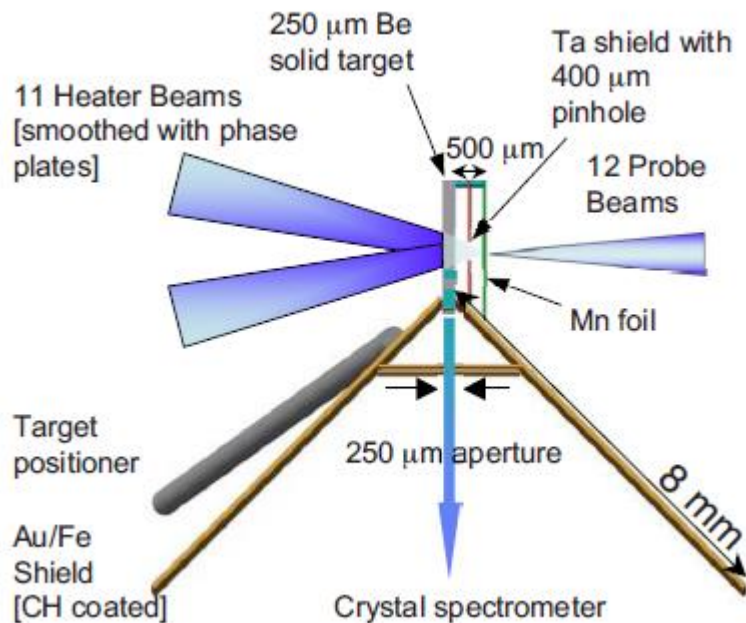
$$k = |k_f - k_i| = \frac{4\pi}{\lambda_i} \sin(\theta/2)$$

- Dimensionless scattering parameter $\alpha = \frac{1}{k\lambda_{sc}} = \frac{l}{2\pi\lambda_{sc}}$
 - l is the electron density fluctuation
 - λ_{sc} is the screening length
- Collective scattering: ($\alpha > 1$)
 - the scattering reflects the electron density fluctuations
 - Plasmon features
- Non-collective scattering: ($\alpha < 1$)
 - the scattering reflects the velocity distribution of electrons
 - Compton features

Glenzer and Redmer, RMP 81, 1625(2009)



Set up of an experiment

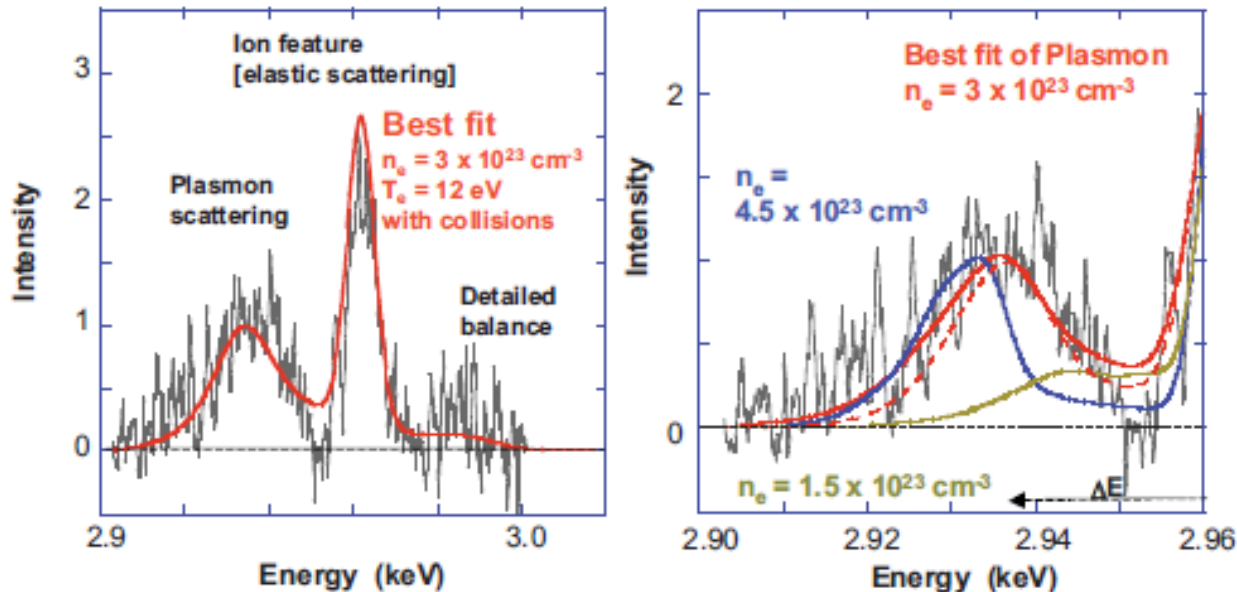


- The target is heated and compressed via laser beams
- Laser beams launch shock waves
- Pressure inside the target in the range of $20 < P < 35$ Mbar
- A backlighters (probe laser pulse) irradiate a Mn target to produce a Mn-He- α line
- x-ray (6.2 KeV) penetrates the target and scattered off the target

H.J. Lee et al., PRL 102, 115001 (2009)



Experimental results and

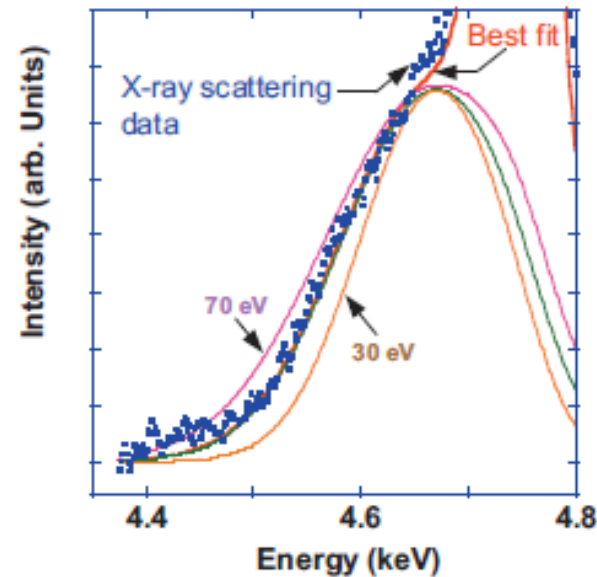
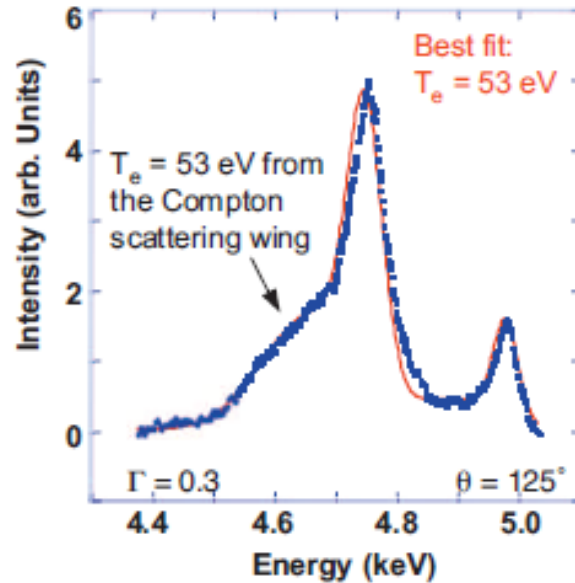


- **Forward scattering:** collective behavior
- Dispersion relation determines the electron density
- Detailed balance gives the electron temperature

Glenzer et al., PRL 98, 065002(2007)



Experimental results and synthetic spectra II

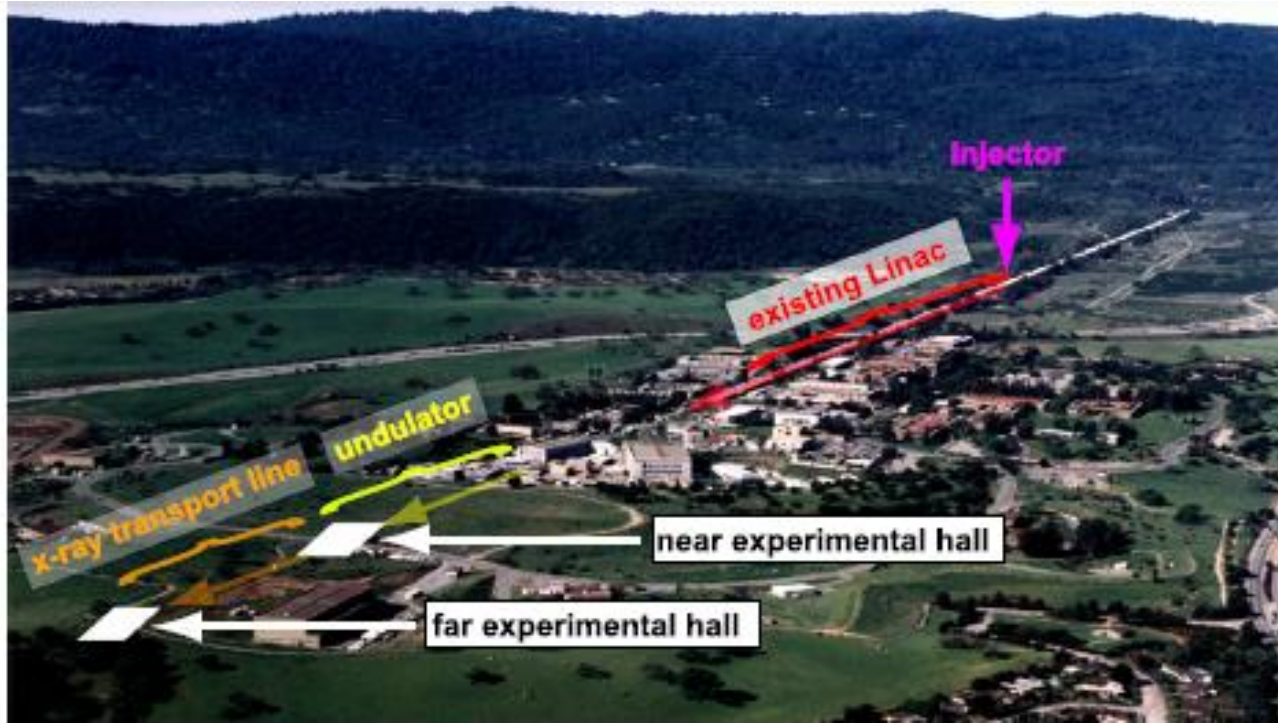


- **Back scattering:**
 - Compton scattering
 - Non-collective behavior
 - Line width \propto Fermi energy

Glenzer et al., PRL 90, 175002(2003)



XRFEL experiment

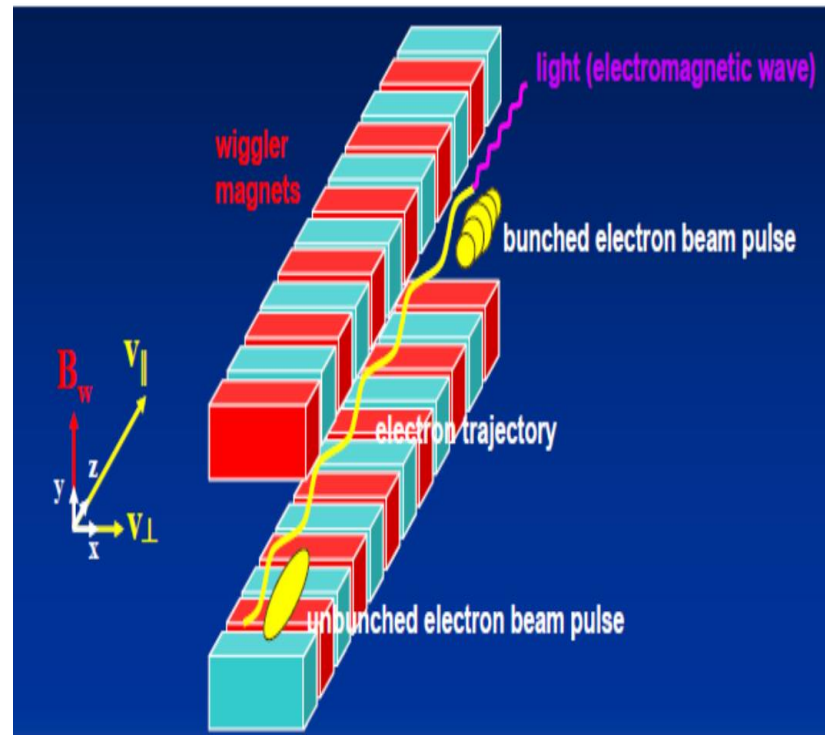


S.H. Glenzer et al., (2016): Stanford University



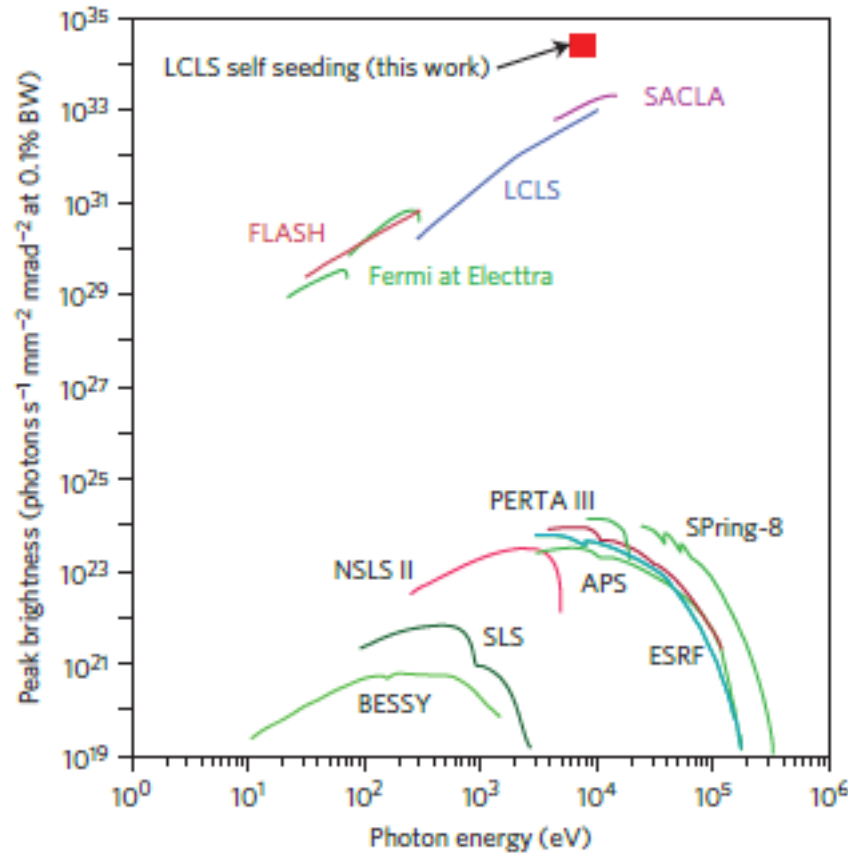
Free electron laser

- ❖ The free electron laser (FEL) is a device that transforms the kinetic energy of a relativistic electron beam into electromagnetic (EM) radiation.
- ❖ Electrons in an FEL are not bound to atoms or molecules.
- ❖ The “free” electrons traverse a series of alternating magnets, called a “wiggler,” and radiate light at wavelengths depending on electrons’ energy, wiggler period and magnetic field.





Tremendous XFEL intensity



Fletcher et al, Nature Photonics 2015



Density Functional Theory

- **1920:** Introduction of the Thomas-Fermi model.
- **1964:** Hohenberg-Kohn paper proving existence of exact DF.
- **1965:** Kohn-Sham scheme introduced.
- **1970 and early 80s:** LDA. DFT becomes useful.
- **1985:** Incorporation of DFT into molecular dynamics (Car-Parrinello)
(Now one of PRL's top 10 cited papers).
- **1988:** Becke and LYP functionals. DFT useful for some chemistry.
- **1998:** Nobel prize awarded to Walter Kohn in chemistry for development of DFT.



Motivation

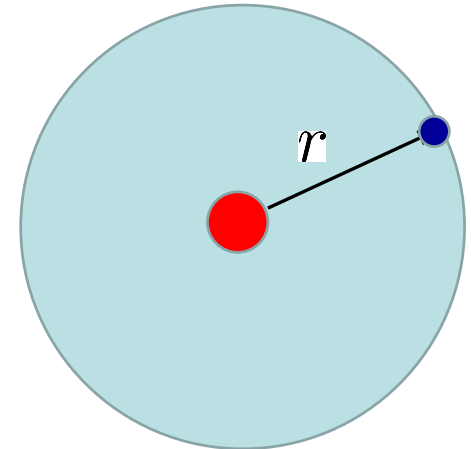
- Have you solved Schrodinger equation for Hydrogen Atom?

$$H\psi(r, \theta, \phi) = E\psi(r, \theta, \phi)$$

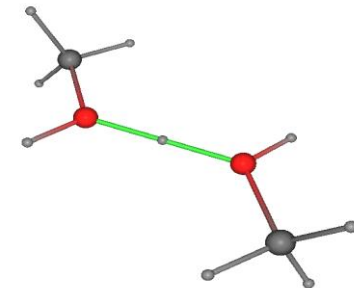
$$\left(\frac{-\hbar^2}{2m} \nabla^2 + V(r) \right) \psi(r, \theta, \phi) = E\psi(r, \theta, \phi)$$

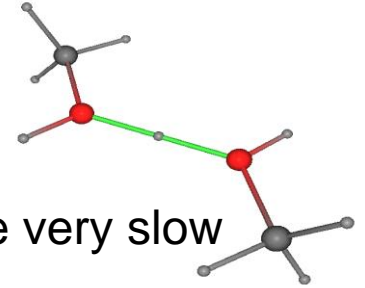
- | | | |
|--|------|------|
| | K.E. | P.E. |
|--|------|------|

$$V(r) = \frac{-e^2}{4\pi\epsilon_0 r}$$



- Is there an exact solution for complex systems?





- In a molecule we have many electrons and many nuclei.
- According to **Born-Openheimer** approximations: nuclei are very slow and their kinetic motion are negligible.
- The Hamiltonian should contain
 - The kinetic energy of electrons
 - Potential energy due to electron-electron interactions.
 - Potential energy due to electron-nucleus interactions.

$$H = \sum_{i=1}^N \frac{-\hbar^2}{2m} \nabla_i^2 + \sum_{i=1}^N \sum_{j \neq i}^N \frac{e^2}{4\pi\epsilon_0(r_i - r_j)} - \sum_{i=1}^N \sum_k^{N_0} \frac{Ze^2}{4\pi\epsilon_0(r_i - r_k)}$$

- K.E. e-e e-n

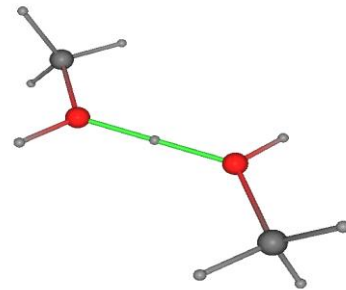
- Is there an exact solution for complex systems?



Hohenberg Kohn Theory

- We cannot have two different systems with the same Ground State density.
- The ground state density is a unique function of the nuclei distribution. It is one-to-one relationship.

$$V_{ext} = - \sum_{i=1}^N \sum_k^{N_0} \frac{Ze^2}{4\pi\epsilon_0(r_i - r_k)}$$



- The electrons will be distributed according to the nuclei distribution.
- The ground state density is related to the minimum energy of the system.





Kohn-Sham Scheme

- The potential energy

$$V_s = V_{ext} + V_{ee}$$

$$V_s = V_{ext}[n(r)] + \int \frac{e^2 n(r) d^3 r}{4\pi\epsilon_0 |r - r'|} + V_{xc}[n(r)]$$

- Schrodinger equation

$$\left(-\frac{\hbar^2}{2m} \nabla^2 + V_s\right) \psi(r) = E \psi(r)$$

- The ground state density

$$n(r) = |\psi|^2$$

The ground state is related to minimum energy

- Functional: function of a function



Kohn-Sham Scheme

- Guess an initial density $n(r) = n^{in}(r)$

$$V_s = V_{ext}[n(r)] + \int \frac{e^2 n(r) d^3 r}{4\pi\epsilon_0 |r - r'|} + V_{xc}[n(r)]$$

- Solve Schrodinger equation for ψ and E .

$$\left(-\frac{\hbar^2}{2m}\nabla^2 + V_s\right)\psi(r) = E\psi(r)$$

- Calculate the density state **Is it ground state?**

$$n(r) = |\psi|^2$$

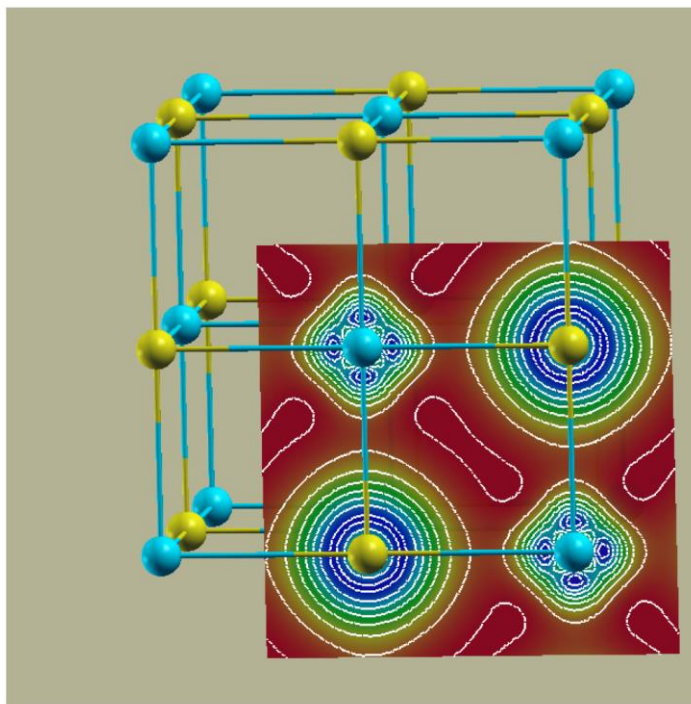
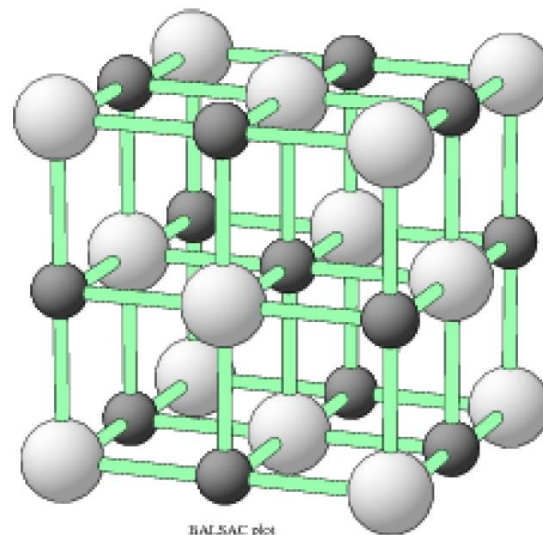
The ground state is related to minimum energy

- Functional: function of a function



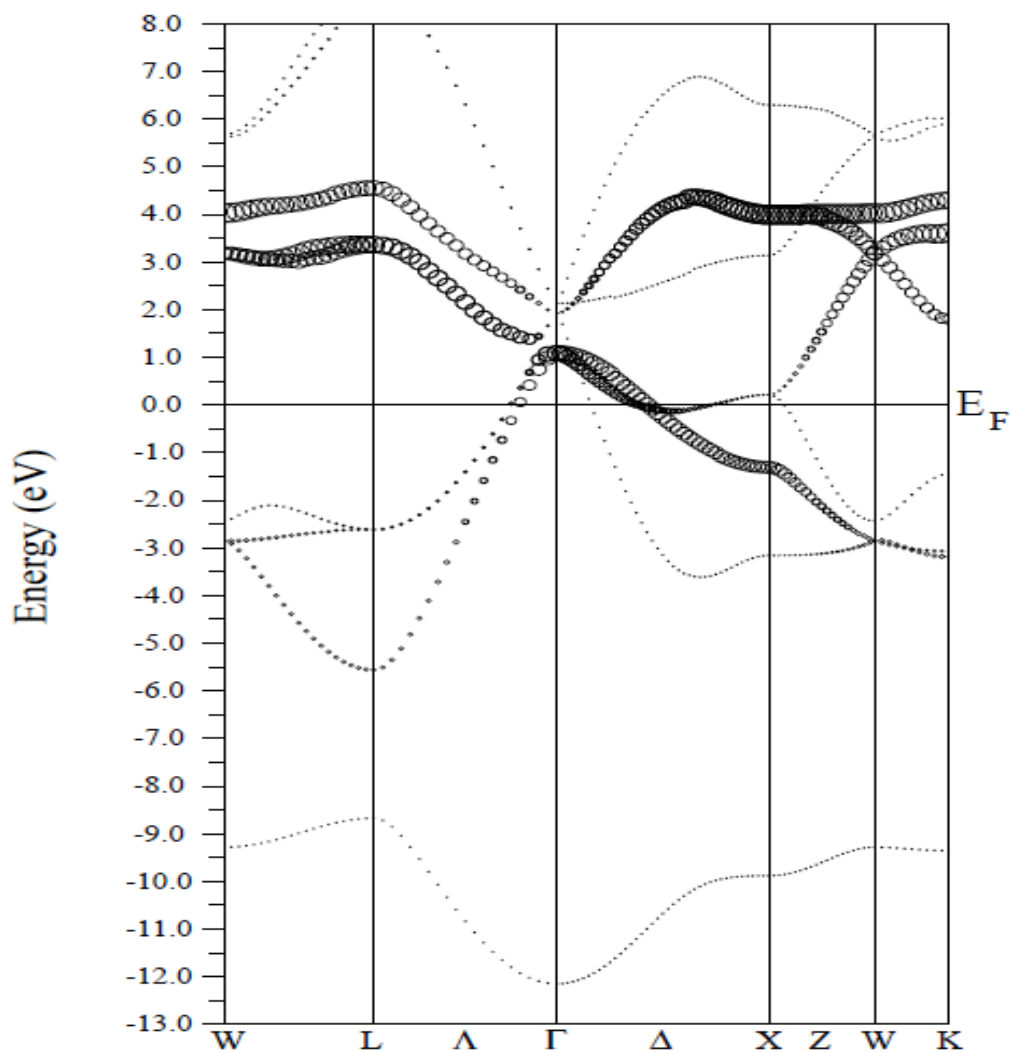
Wien2K software

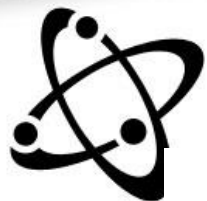
- TiC in the sodium chloride structure
- The electron density of TiC in (110)



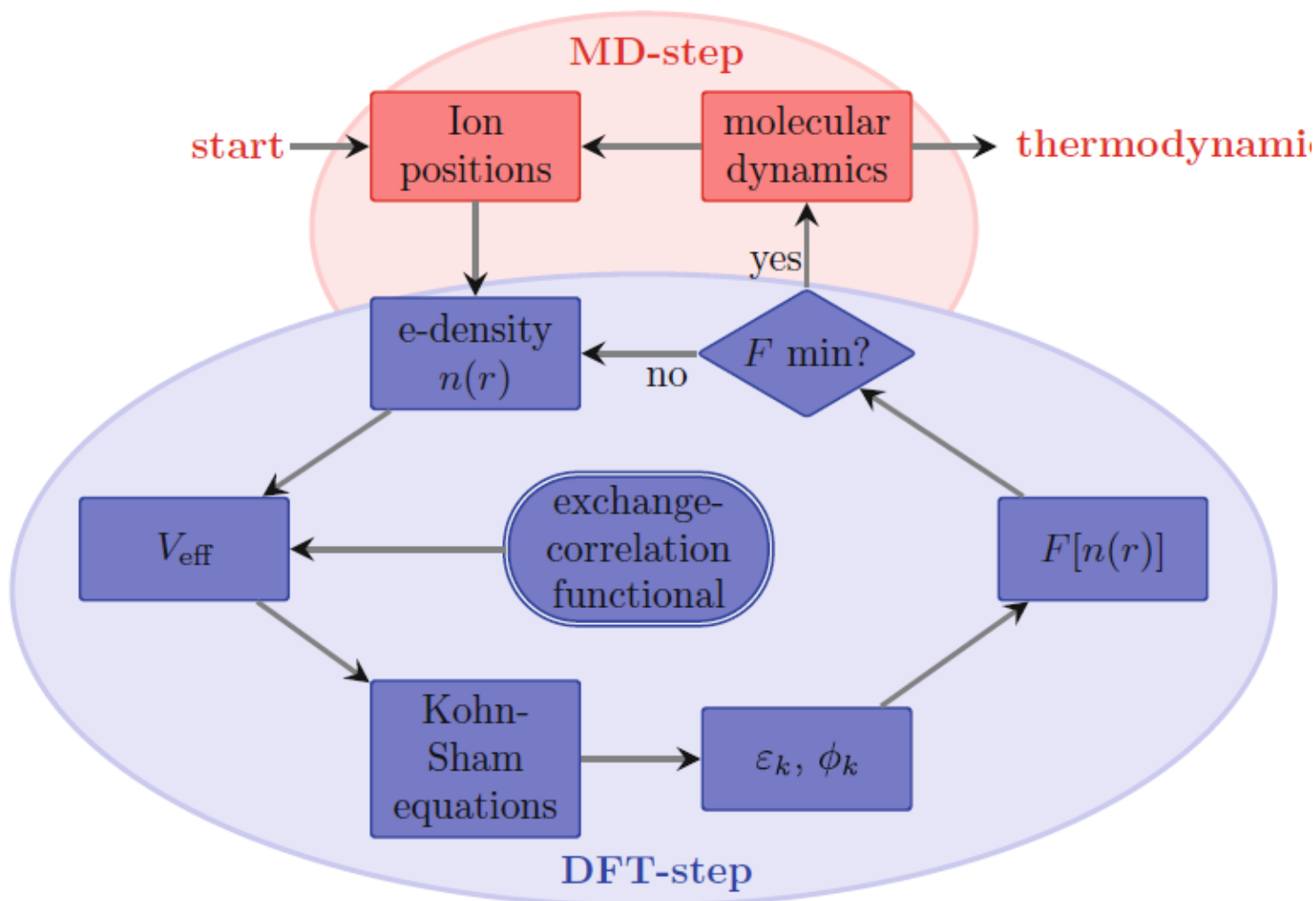


Wien2K software



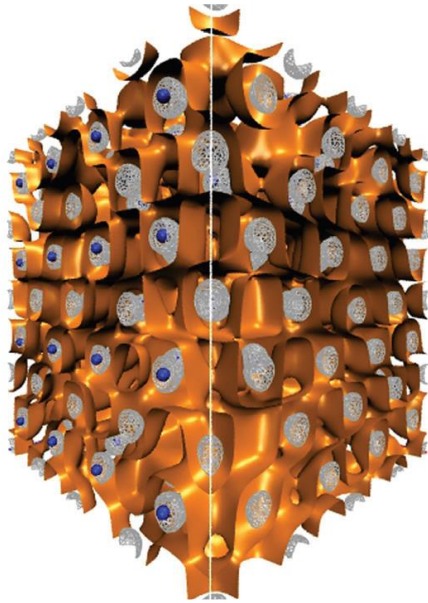


DFT-MD

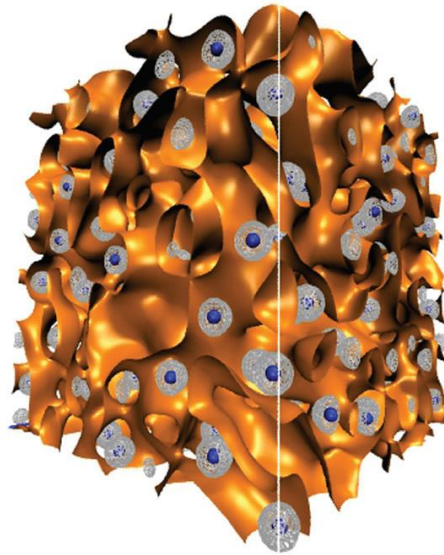




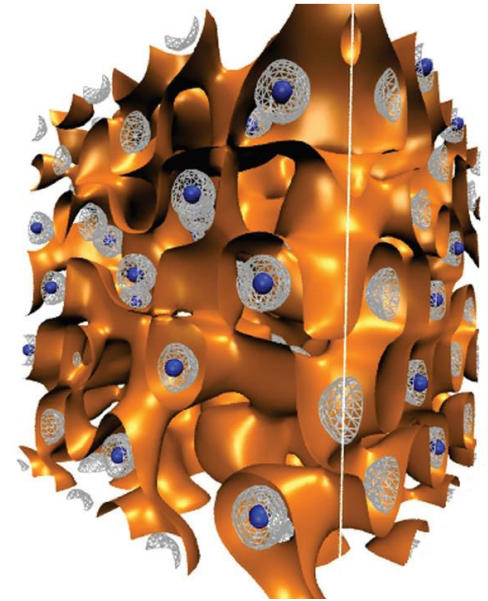
DFT-MD



Solid Aluminum



Melting Phase



WDM



Thanks!