

# Linear Analysis of Electrostatic Waves in the Earth's Magnetopause

**Presented by**

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**Supervisors**

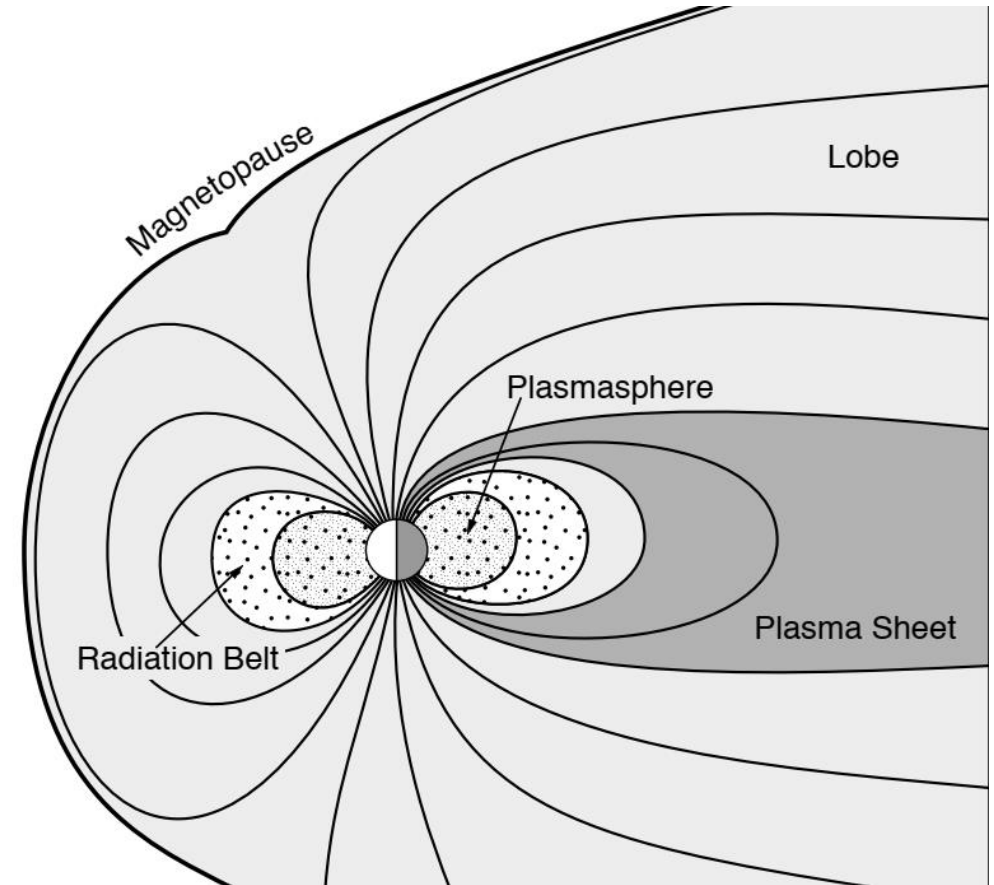
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# Plasma inside the magnetosphere

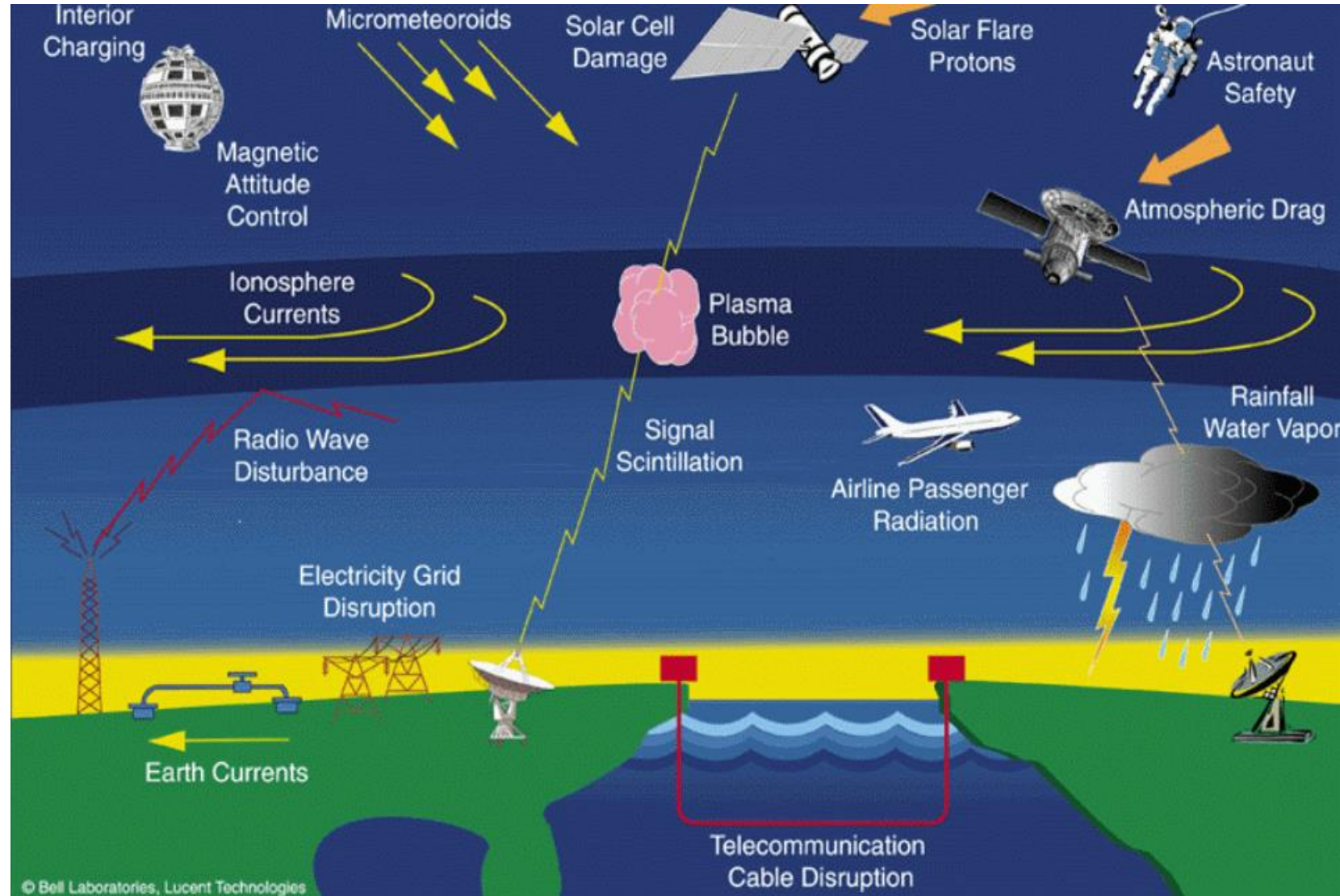
- **The radiation belt (dilute and hot) [Van Allen and Frank, 1959]** It consists of energetic electrons and ions which move along the field lines and oscillate back and forth between the two hemispheres.
- **plasma sheet (hot plasma )** most of the magnetotail plasma.
- **magnetotail lobe (dilute plasma):** The outer part of the magnetotail.
- **Plasmasphere (dense cold plasma)**





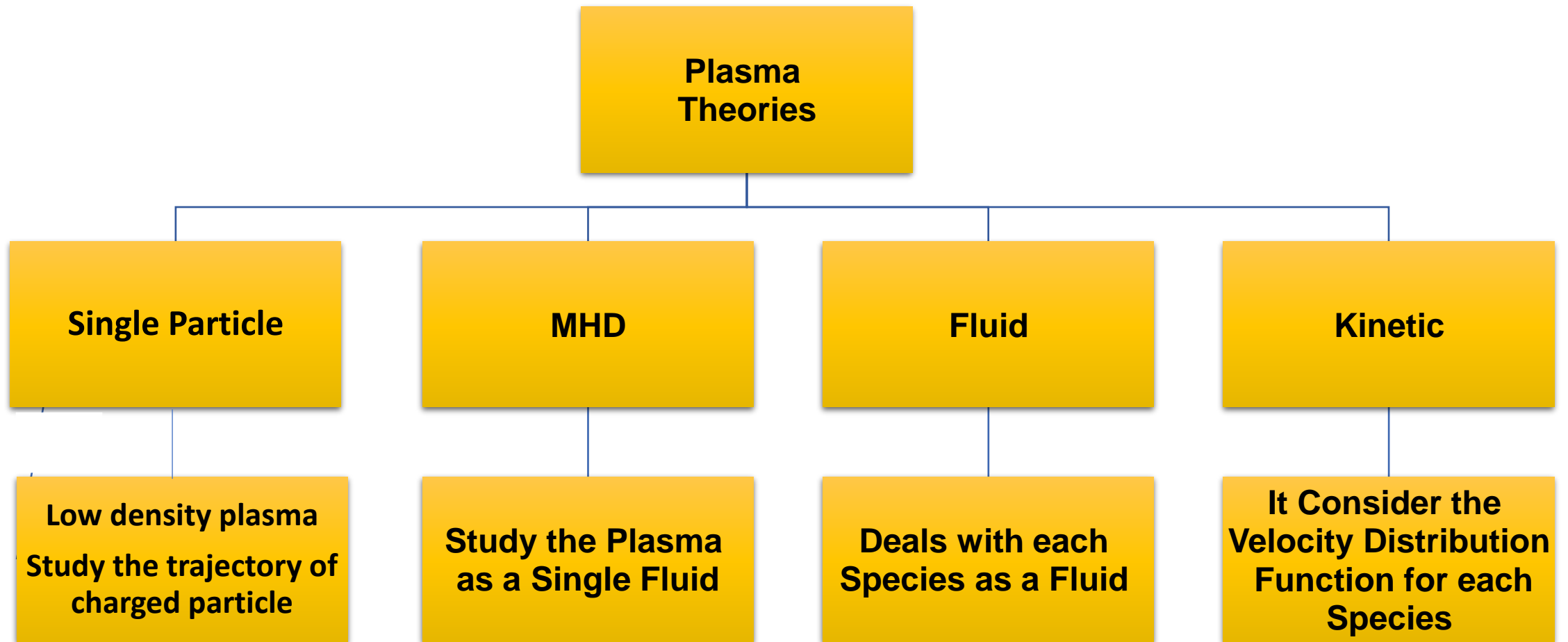
## The role of plasma in space weather

- **Has a significant impact on many things inside the Earth.**
- **Examples: air navigation, power plants, communications, and others.**



## Waves as diagnostic tools

- **Instability is accompanied by waves.**
- **Waves is considered as fingerprints of plasma.**
- **Plasma waves can be used to determine the composition through detection of characteristic frequencies.**
- **Wave observations made remote-sensing of the heliopause possible before other means of investigation were available.**



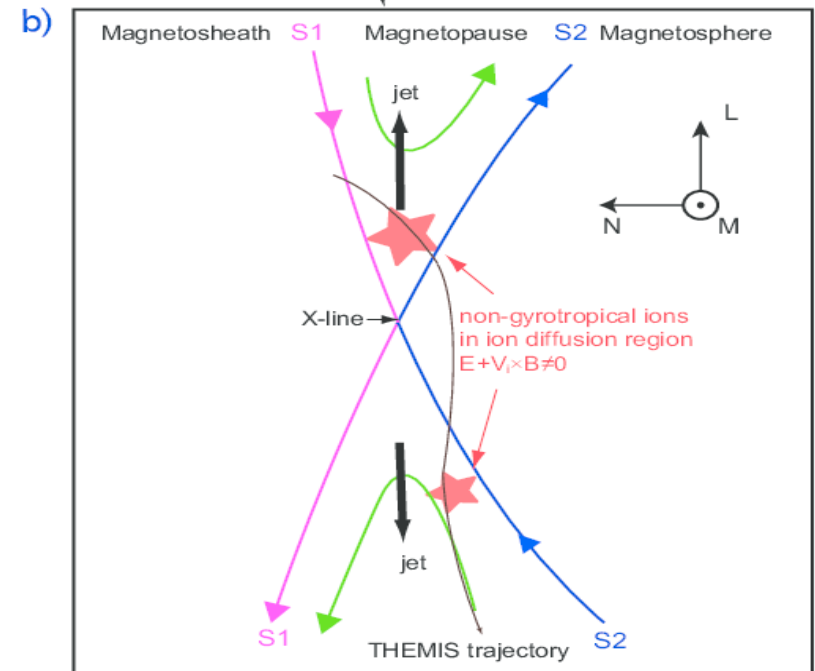
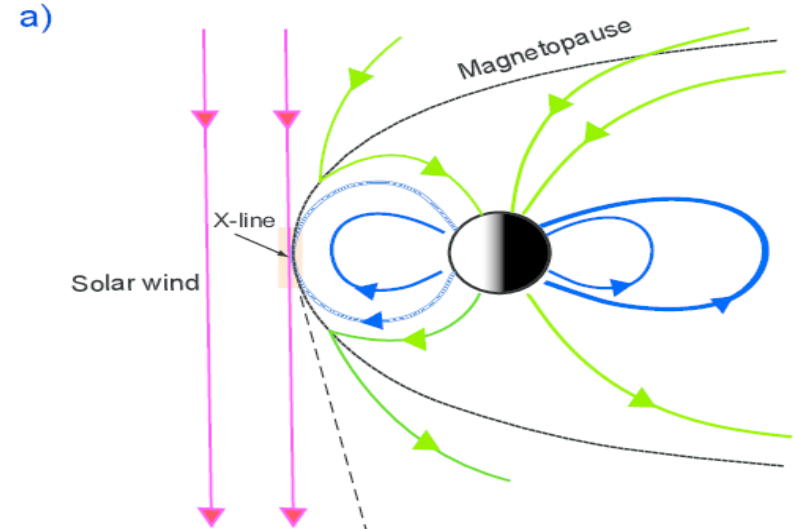
# Our model

## Solar wind:

1. Solar ions beam.
2. Solar electrons.

## Magnetopause:

1. Hot ions.
2. Cold ions.
3. Background electrons.



# Basic Equations

## Fluid Equations

$$\frac{\partial n_j}{\partial t} + \frac{\partial}{\partial x} \cdot (n_j \cdot u_j) = 0, \quad (1)$$

$$m_j n_j \left( \frac{\partial}{\partial t} + u_j \cdot \frac{\partial}{\partial x} \right) u_j = -e \frac{\partial \phi}{\partial x} - \frac{\partial P_j}{\partial x} \quad (2)$$

$$P_j = P_0 n_0^{-\gamma} \frac{\partial n_j}{\partial x}, \quad P_0 = n_0 K_B T$$

## Maxiwell distribution

$$n_j = n_{j0} \exp \left( \frac{e\phi}{K_B T_j} \right) \quad (3)$$



## Linearization

$$n = n_0 + n_1$$

$$u = u_0 + u_1$$

$$\phi = \phi_0 + \phi_1$$

## Fourier Transform

$$n_1(x, t) = n_1 \exp[i(kx - \omega t)]$$

$$u_1(x, t) = u_1 \exp[i(kx - \omega t)]$$

$$\phi_1(x, t) = \phi_1 \exp[i(kx - \omega t)]$$

## Dispersion Relation

$$1 + \frac{e^2 n_{es0}}{\epsilon_0 K_B T_{es} k^2} + \frac{e^2 n_{e0}}{\epsilon_0 K_B T_e k^2} - \frac{e^2 n_{ic0}}{\epsilon_0 m_{ic} \omega^2} - \frac{e^2 n_{is0}}{\epsilon_0 m_{is} [(\omega - k U_{is0})^2 - 3 \epsilon_0 K_B T_{is} k^2]} - \frac{e^2 n_{ih0}}{\epsilon_0 m_{ih} [\omega^2 - 3 K_B T_{ih} k^2]} = 0$$

Normalization of Dispersion Relation:

Frequencies are normalized by proton plasma frequency  $\omega_{pi} = \sqrt{\frac{e^2 n_{ic0}}{\epsilon_0 m_i}}$ .

Velocities are normalized by ion acoustic waves  $C_s = \sqrt{\frac{K_B T_e}{m_i}}$ .

Wave number (k) normalized by proton Debye length  $\lambda_{Di} = \sqrt{\frac{\epsilon_0 K_B T_e}{e^2 n_{ic0}}}$ .

$$1 + \frac{\delta_1}{\lambda_{Di}^2 k^2 \sigma_1} + \frac{\delta_2}{\lambda_{Di}^2 k^2} - \frac{\delta_3}{(x - \lambda_{Di} k v)^2 - 3\lambda_{Di}^2 k^2 \sigma_2} - \frac{1}{x^2} - \frac{\delta_4}{x^2 - 3\lambda_{Di}^2 k^2 \sigma_3} = 0$$

$$\delta_1 = \frac{n_{es0}}{n_{ic0}},$$

$$\delta_2 = \frac{n_{e0}}{n_{ic0}},$$

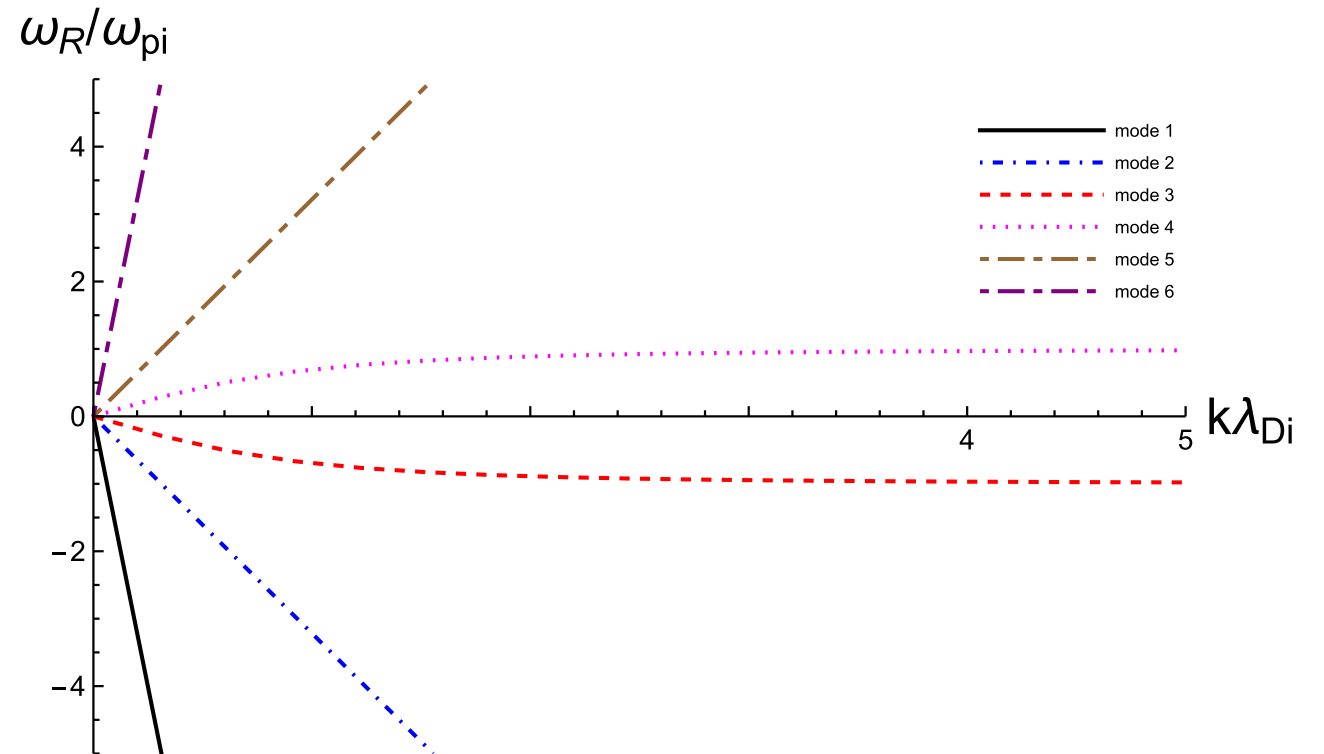
$$\delta_3 = \frac{n_{is0}}{n_{ic0}},$$

$$\delta_4 = \frac{n_{ih0}}{n_{ic0}}$$

$$\sigma_1 = \frac{T_{es}}{T_e},$$

$$\sigma_2 = \frac{T_{is}}{T_e},$$

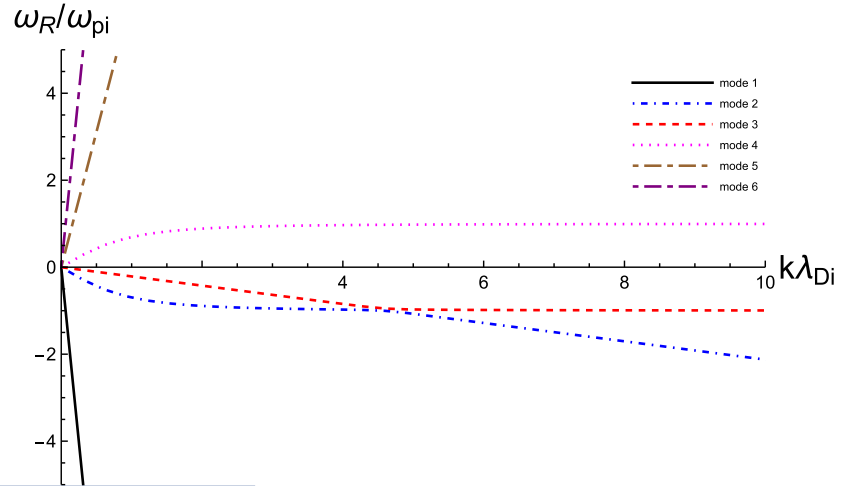
$$\sigma_3 = \frac{T_{eh}}{T_e}$$



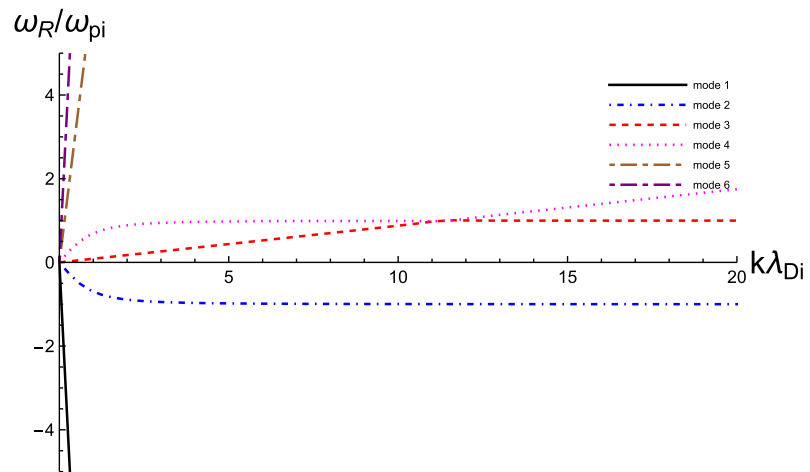
$$x = \frac{\omega}{\omega_{pi}}, \quad v = \frac{U_{is0}}{C_s}$$

# Influence of solar ion beam velocity

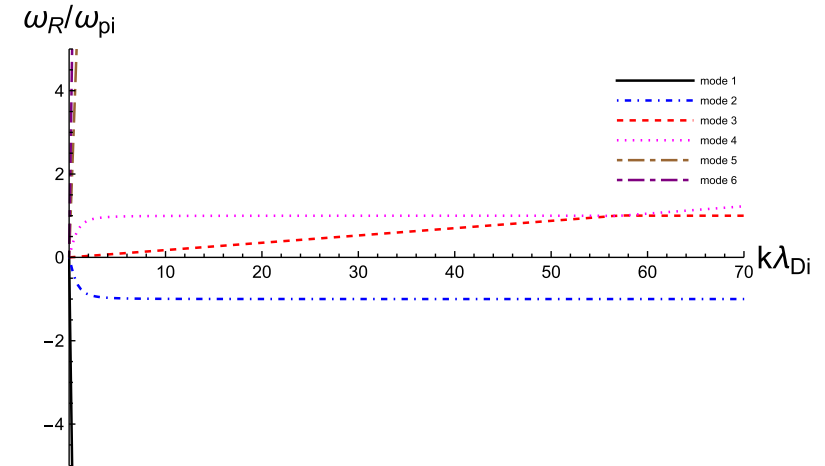
$v=3$



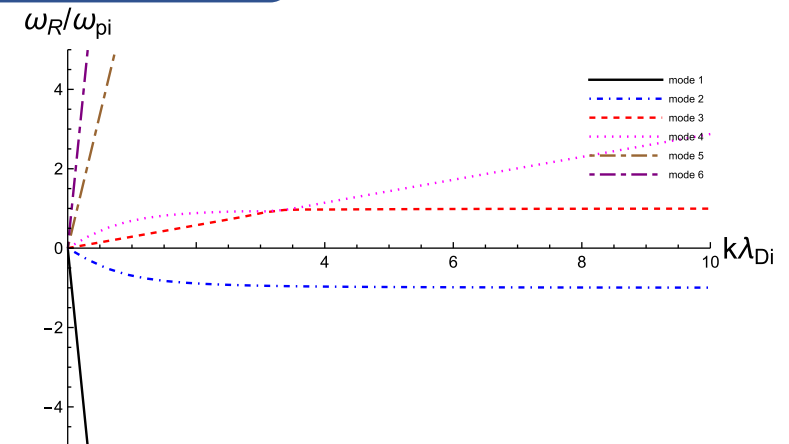
$v=3.3$



$v=3.23$

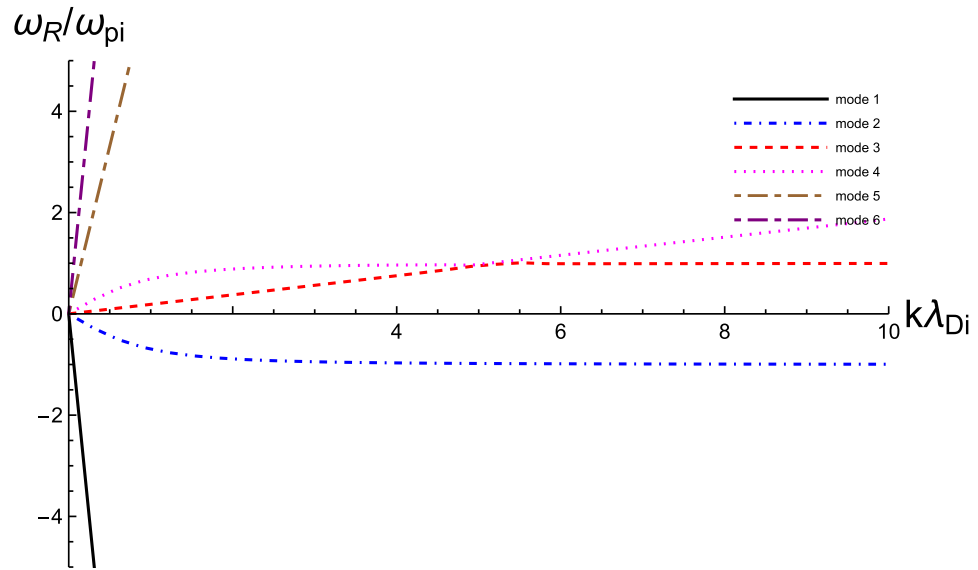


$v=3.5$

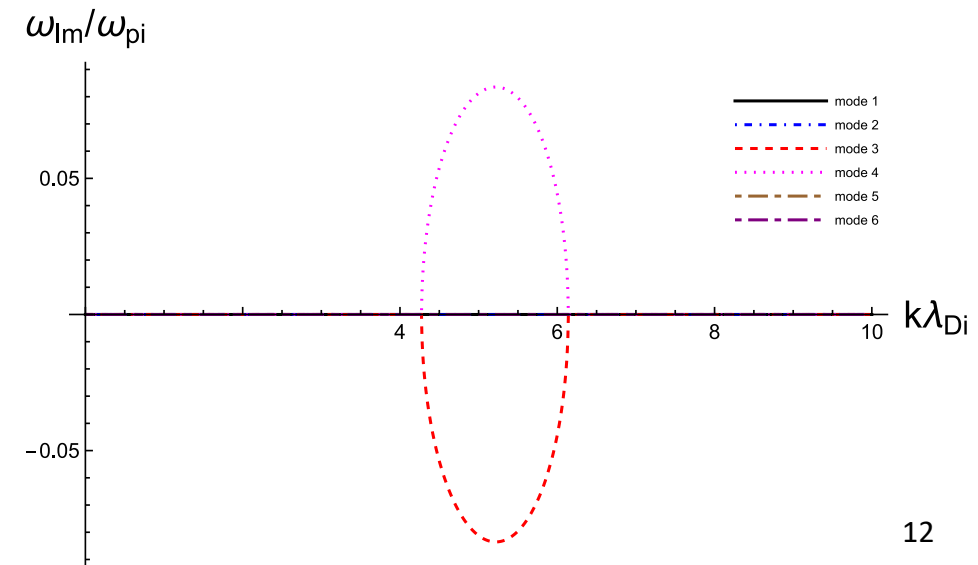
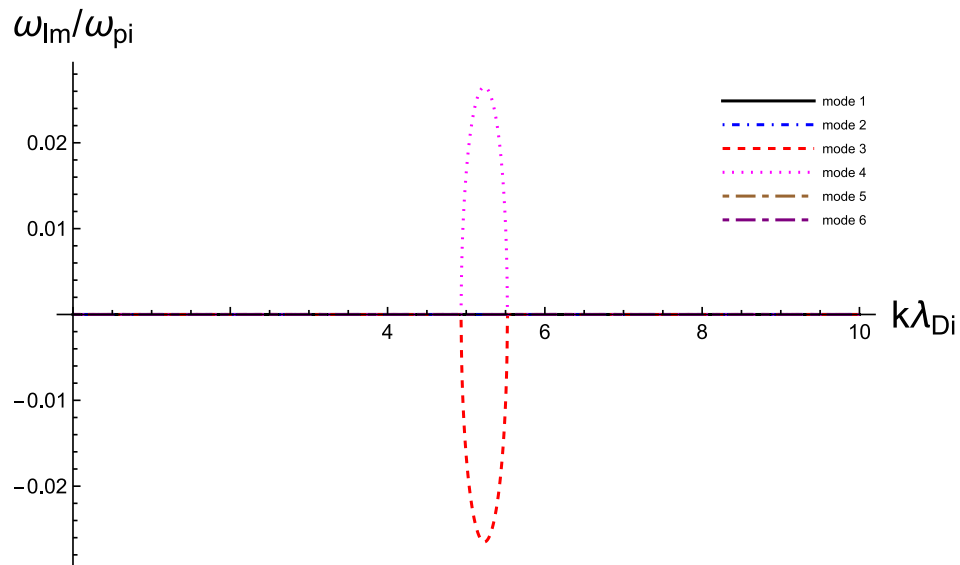
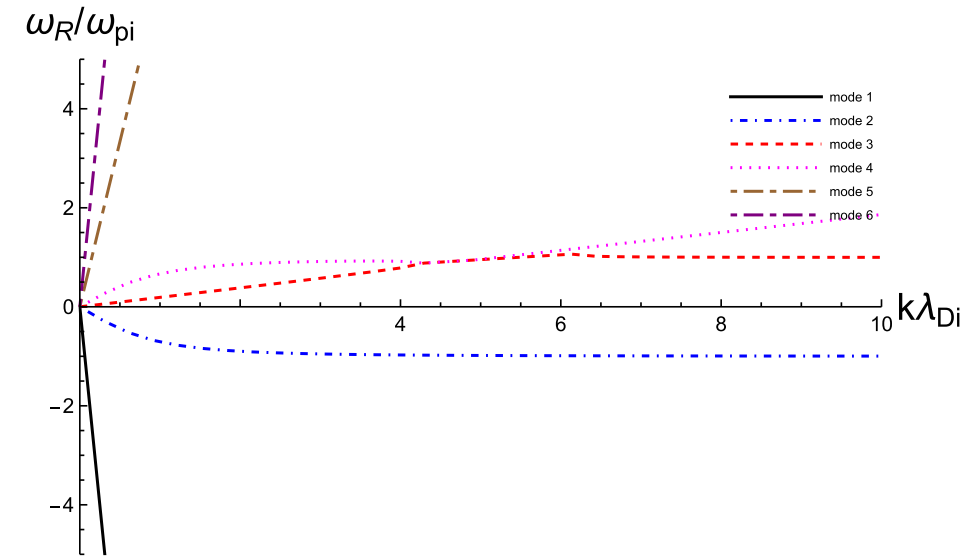


# Influence of density of solar ions

$$n_{is0}/n_{ic0} = 0.05$$



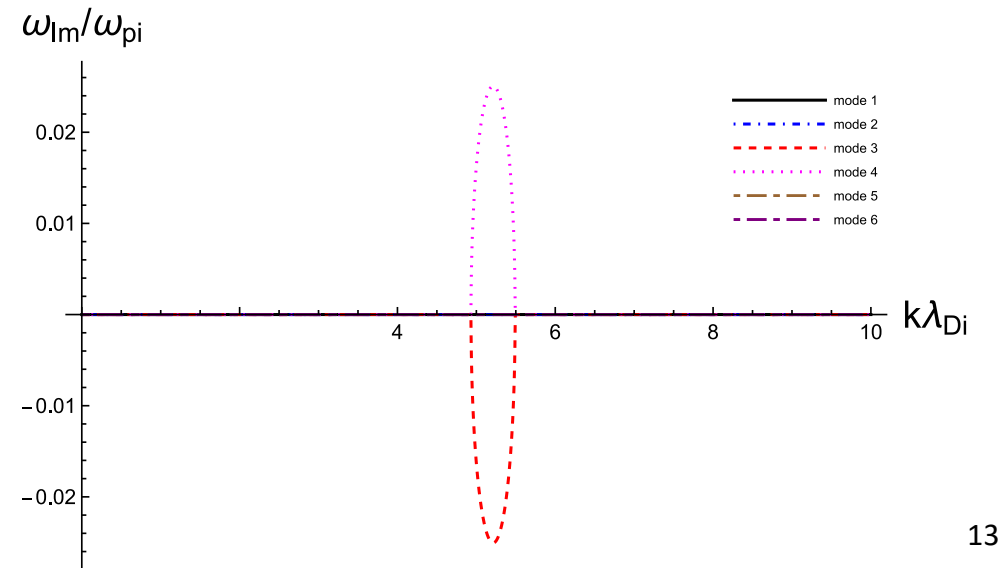
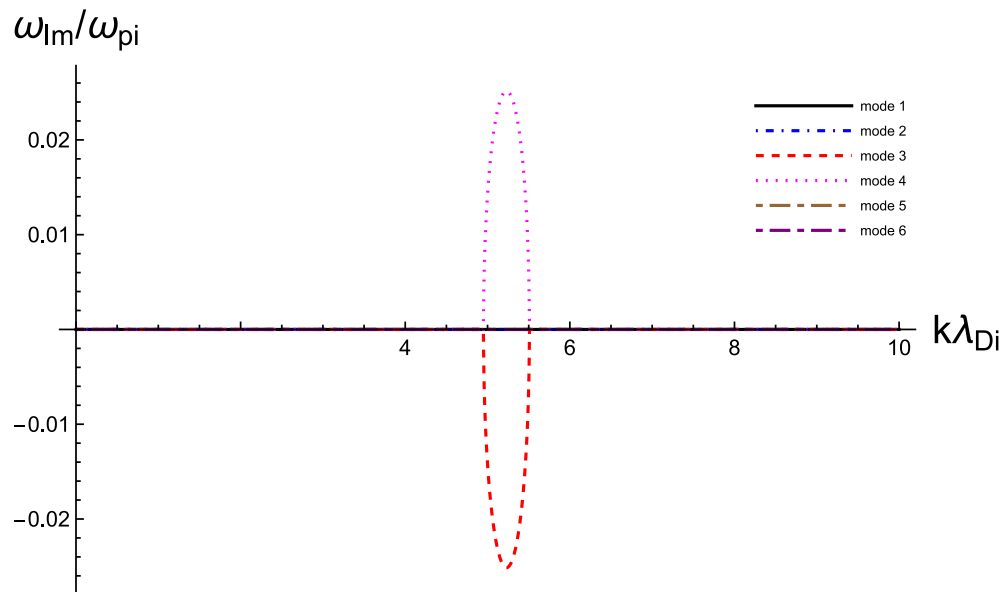
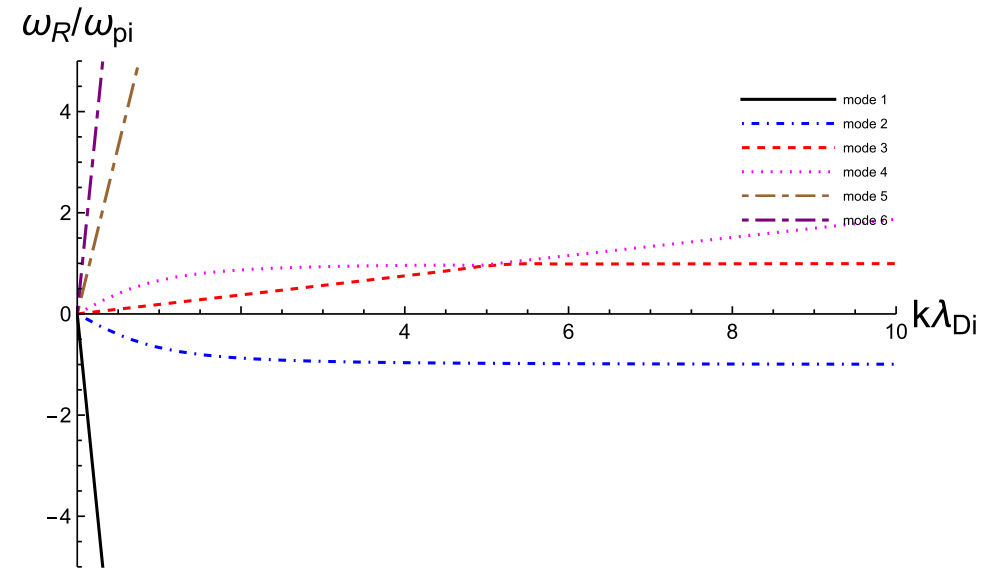
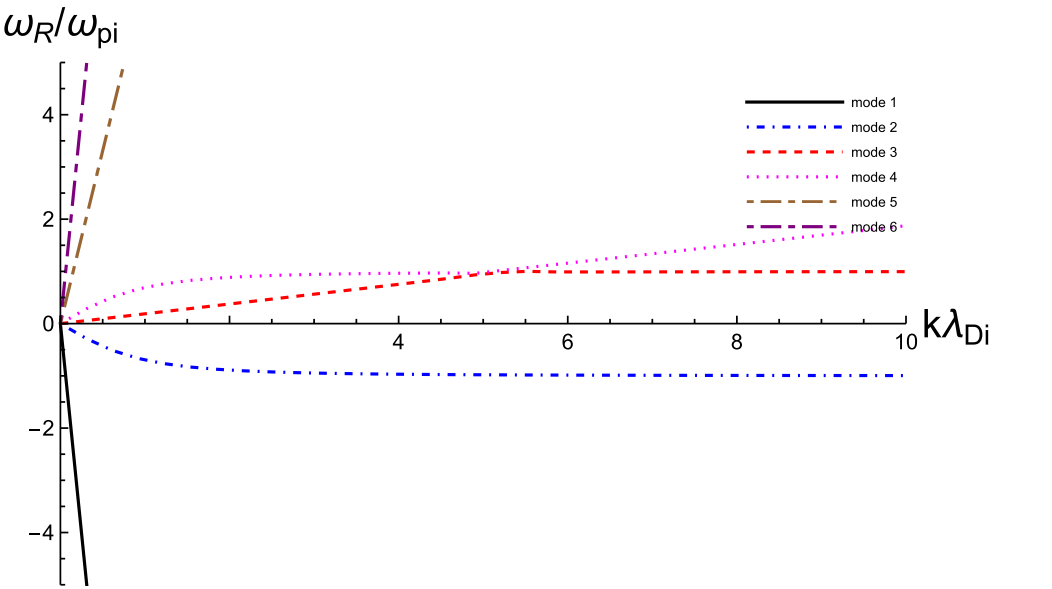
$$n_{is0}/n_{ic0} = 0.5$$



# Influence of density of solar electrons

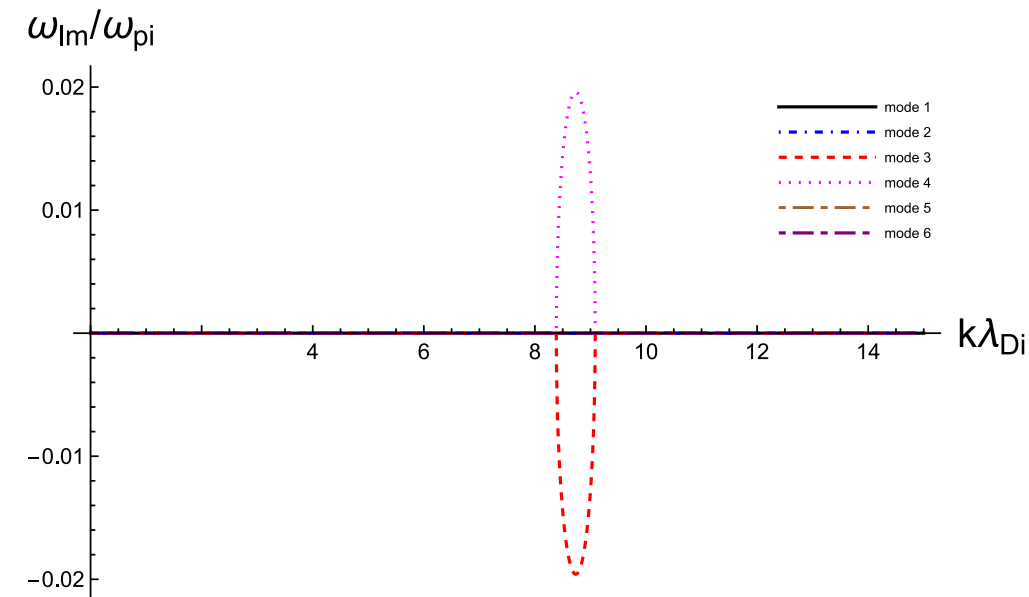
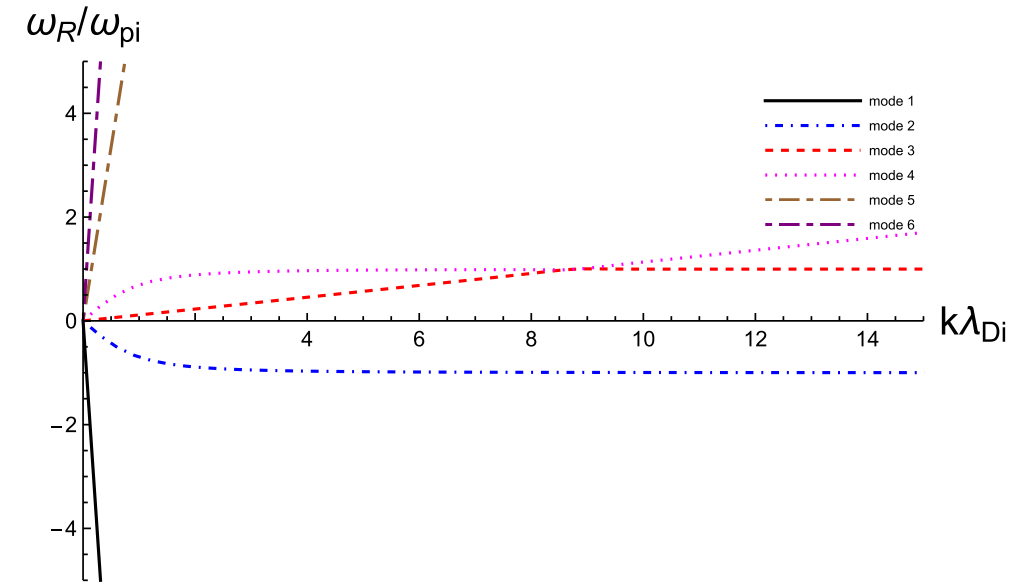
$n_{es0}/n_{ic0} = 0.01$

$n_{es0}/n_{ic0} = 0.1$

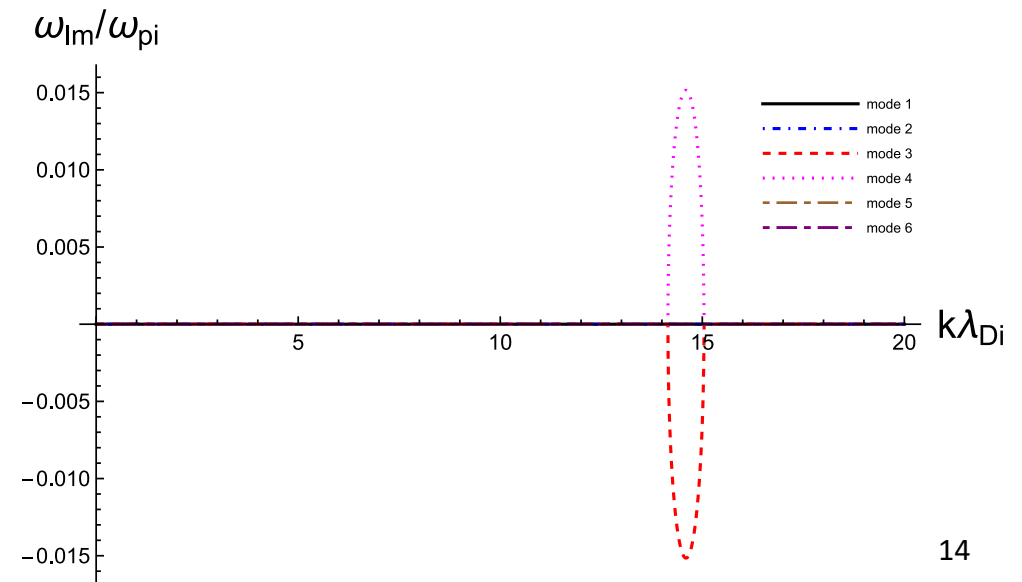
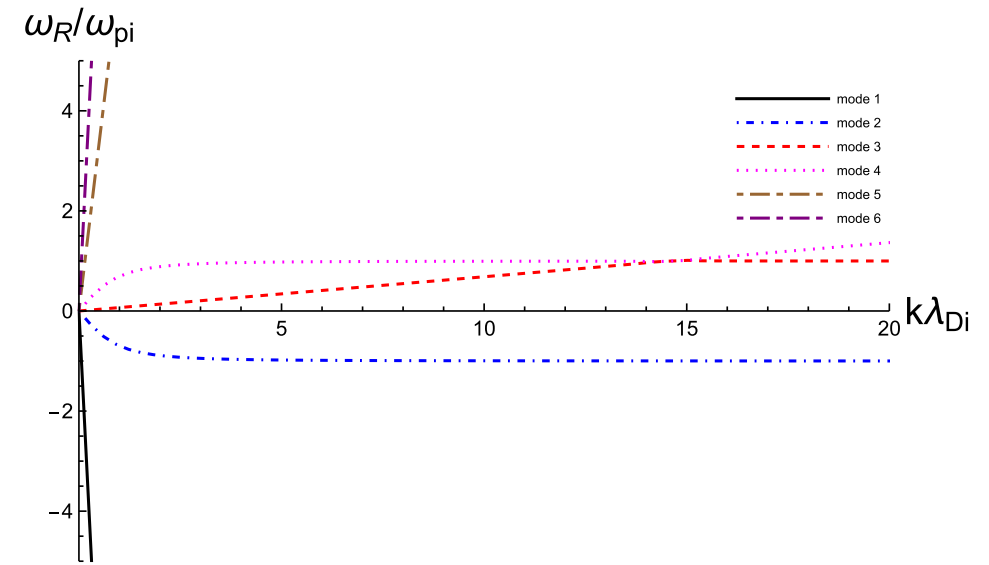


# Influence of temperature of solar ions

$$T_{is}/T_e = 3.6$$



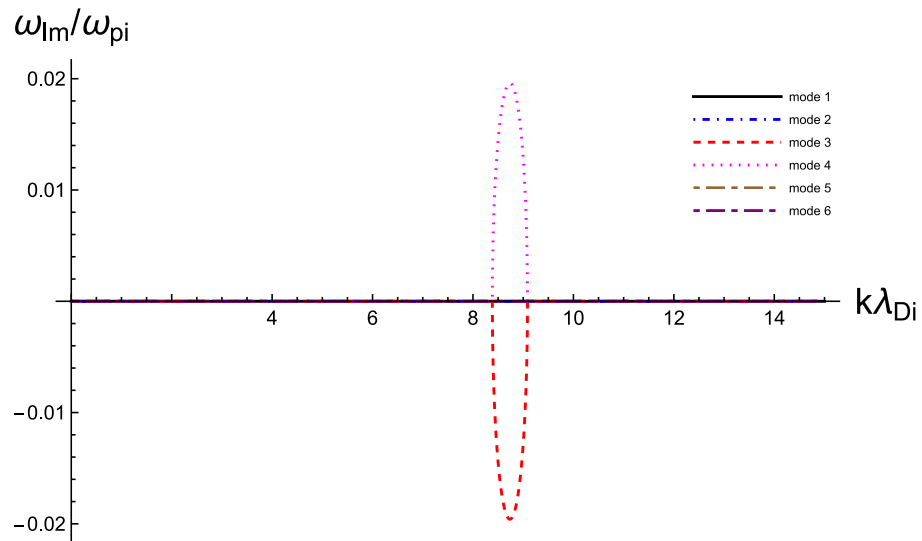
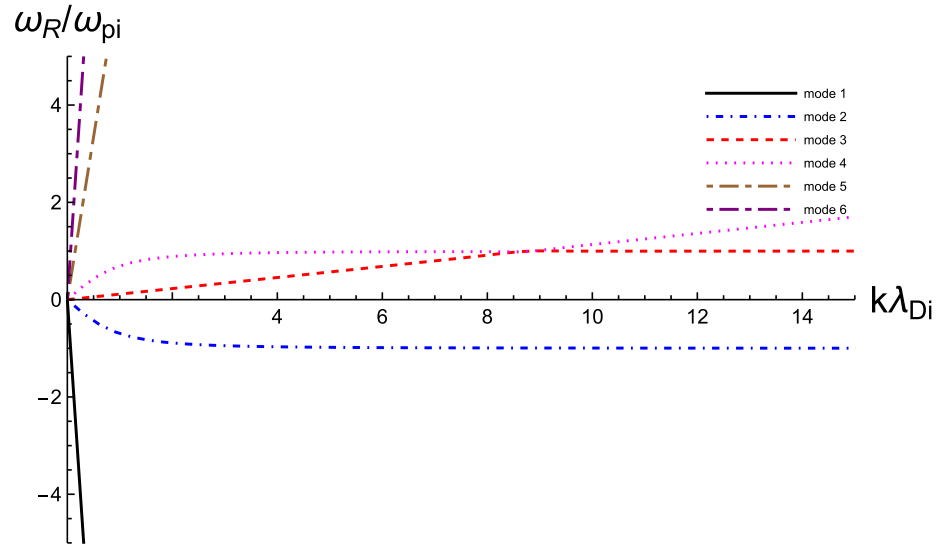
$$T_{is}/T_e = 3.7$$



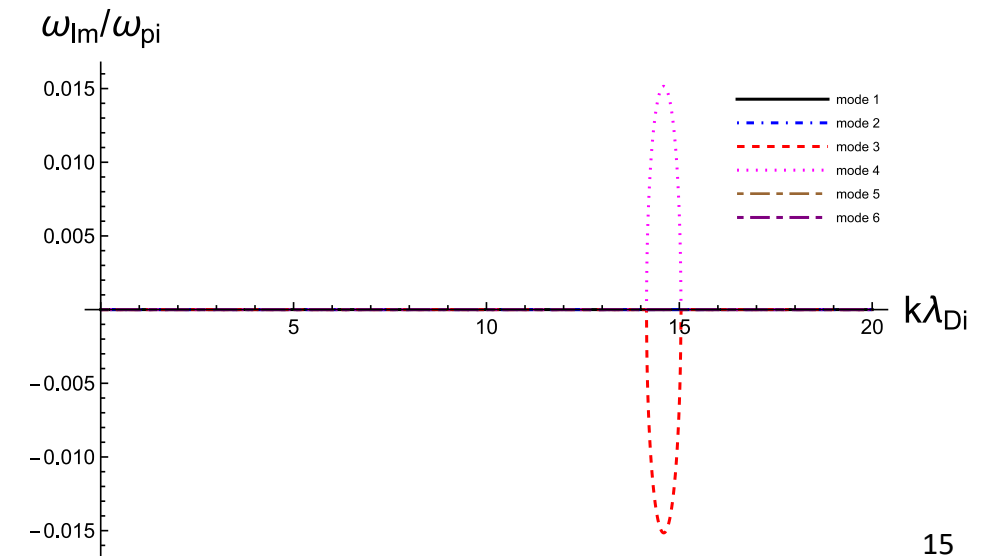
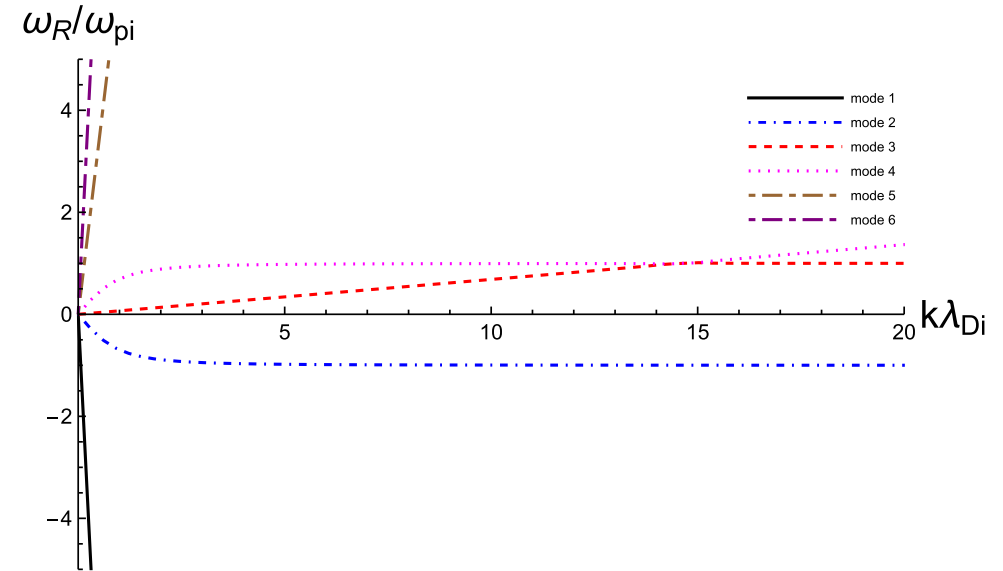


# Influence of temperature of hot ions

$$T_{ih}/T_e = 3.6$$



$$T_{ih}/T_e = 3.7$$



# Summary

- ❑ We had done a linear analysis of properties of electrostatic waves in a system of plasma.
- ❑ Plasma consisted of 5 components as solar ions beam, solar electrons, hot ions, cold ions and background electrons.
- ❑ Dispersion relation was obtained by solving fluid model equations. Six roots were gotten as two for solar ions, two for hot ions and two for cold ions.
- ❑ It is observed that by increasing solar ion beam velocity, phase velocity of mode 5 increased. At  $\frac{U_{iso}}{c_s} = 3$  mode 2 begin to merge with mode 3 to form an unstable region. Merging occurred at low wave number. As  $\frac{U_{iso}}{c_s}$  increased merging region shifted to high wave number. Also, frequency increased. Continuously increasing ion beam velocity mode 3 started to merge with mode 4 at  $\frac{U_{iso}}{c_s} = 3.22$  at high wave number. The merged region was almost fixed and frequency increased. Also, it is observed unstable region shift to low wave number as ion beam velocity increased until disappeared at  $\frac{U_{iso}}{c_s} = 4.3$ .

# Summary

- ❑ The effect of different species density was investigated:
  - For increasing density of solar ions beam, the merged region between modes 3 and 4 increased and frequency also increased.
  - The effect of density of solar electrons is not noted.
- ❑ The effect of temperature of different species was studied as:
  - Increasing solar ions beam temperature, the instability region between modes 3 and 4 was almost fixed and shifted to high wave number. However, frequency of wave decreased.
  - Same behavior for temperature of hot ions, where increasing temperature led to instability region shifted to high wave number and decreasing in frequency of wave.

